Two Under-Approximation Techniques for 3-Modal Abstraction Coverage of Event Systems: Joint Effort?

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Abstract

Model-based testing of event systems can take advantage of considering abstractions rather than explicit models, for controlling their size. A test is then a connected and reachable event sequence. This paper reports on experiments made when adapting for event systems two known under-approximation techniques of predicate tri-modal (may, must+, must-) abstractions. We first instantiate all the abstract may transitions, preferably as reachable instances. Second, we complete this under-approximation with instantiations of Ball chains, i.e., sequences in the shape of must-*.may.may+* transitions, as such sequences are guaranteed to have connected instantiations. We present a backward symbolic instantiation algorithm for connecting these two under-approximations. We experimentally address the question of their complementarity. Surprisingly, our results show that Ball chains have not enhanced the coverage already achieved by the first step of may-transitions instantiation. However, it has enhanced the number of test steps by prolonging the already existing tests.

Keywords. Predicate abstraction; under-approximation; event systems; may/must transitions; test generation

1 Introduction

Abstracting a program or its specification allows to control the size of its state space description, at the price of a loss in accuracy. That facilitates their algorithmic exploitation, otherwise limited by the huge if not infinite number of concrete states. The general idea of abstraction is to gather states that share common properties into super-states. In predicate abstraction [GS97] the concrete states are mapped onto a finite set of abstract ones, by means of a set of predicates that characterizes each abstract state. We are interested in generating model-based tests from a predicate abstraction of a system formally specified as an event system [Abr10], which is a special kind of action system [Dij75, Dij76]. Such tests will be computed as concrete instantiations of abstract transition sequences, which raises the two issues: to be used as model-based tests, these instantiations have to be 1) connected, and 2) reachable.

Concerning connectivity, an abstract transition links two abstract states when it has at least one concrete instantiation. Such transitions are called may [GJ03], meaning that they may be instantiated. But two consecutive may instantiations might be disconnected since the concrete transitions may not end and begin on the same concrete state. Reachability is also an issue with event systems: an event specifies state variable modifications by means of a guarded action. The actions are activated whenever their guard becomes true, so that contrarily to programs, there is no natural control flow that one could follow to guarantee
reachability. Hence we seek to under-approximate the abstraction by computing connected and reachable concrete instances of the abstract event sequences.

To this end, two under-approximations approaches from literature have been retained. The first one is by M. Veanes and R. Yavorsky [VY03] for under-approximating an Abstract State Machine specification by a Finite State Machine. It gradually explores the abstraction by widening a frontier of the visited states, while exhibiting concrete instances whose reachability is either guaranteed when possible, or uncertain otherwise. We call this approach concrete exploration (CXP). The second one is by T. Ball [Bal04], intended to predicate testing of C programs. It associates the abstract transitions with three possible modalities: may, must+ and must− for exploiting a structural property that the abstract sequences of the form (must−)* may (must+) are guaranteed to be connectedly instantiable. We call such sequences “Ball chains”. In the context of event systems, we still have to seek for their reachability.

We have recently adapted and applied these methods to event systems, but separately. Indeed, [JKMV17] provides an algorithm that adapts and applies the concrete exploration to event systems. In [BJM15, BJM16] forward symbolic exploration from the initial states to reach the Ball chains has been used. In this paper we build the bridge for combining the two methods, which allows us to implement and experiment with case studies. The main idea is to connect the Ball chains instantiations to the concrete reachable paths à la Veanes and Yavorsky, for ensuring their reachability. We present an algorithm that instantiates the Ball chains, and proceeds to a backward symbolic exploration of the must− transitions towards these reachable paths. Also, we experimentally investigate the complementarity of the two methods w.r.t. various abstractions of four realistic case studies. Surprisingly, our results show that the Ball chains do not provide additional coverage of the abstract states and transitions than the concrete exploration does. Nevertheless, they prolong the already existing concrete sequences, thus providing more test steps to explore the system.

The technical background of our paper regarding event systems, predicate abstraction and tri-modal transition systems is given in Section 2. Section 3 presents a simple coffee machine as an illustrative example. Our method, and in particular the algorithm for computing and instantiating the Ball chains with backward symbolic exploration towards the concrete exploration, is presented in Section 4. Our experimental results are presented in Section 5. Section 6 describes related work, and Section 7 concludes the paper.

2 Background

In this paper systems are specified by event systems (ES) described using the B syntax [Abr96, Abr10]. Notice however that our proposals and results are applicable to all models whose semantics is expressed by the concrete labelled transition systems.

In this section we first present the syntax and the semantics of the B event systems. Then we present the concept of predicate abstraction and formalize the abstraction of ES by means of Tri-modal Transition Systems (3MTS). Last, we present Ball’s universal under-approximation based on 3MTS.

2.1 Model Syntax and Semantics

We start by introducing B event systems in Def. 1. Let a be a guarded action, E, F be arithmetic expressions and P, P′ be predicates, the events are defined by means of guarded actions [Dij75] composing five primitive actions: skip an action with no effect, x, y := E, F a multiple assignment, P ⇒ a a guarded action, a1 || a2 a non-deterministic choice between a1 and a2, and @z.a an unbounded non-deterministic choice for all the values of z satisfying

\footnote{We could alternatively use a syntax with guarded commands [Dij75], such as Abstract State Machines [GKOT00, Gur00].}
the guard of a. Notice that \( a_1 \parallel a_2 \) as well as \( IF \ P \ THEN \ a \ END \) can be rewritten with the five primitives actions as explained in [Abr96].

**Definition 1 (Event System)** Let \( \text{Ev} \) be a set of event names. A B event system is a tuple \((X, I, \text{Init}, \text{EvDef})\) where \( X \) is a set of state variables, \( I \) is a state invariant, \( \text{Init} \) is a guarded action that initializes the system, such that \( I \) holds in any initial state, \( \text{EvDef} \) is a set of event definitions, each in the shape of \( e \overset{\text{def}}{=} a \) for any \( e \in \text{Ev} \), where \( a \) is a guarded action that preserves \( I \).

Figure 2 depicts an example of an event system that illustrates Def. 1. Following [BC00], Concrete labelled Transition System (CTS) describe the semantics of event systems.

The event systems have also an axiomatic semantics. An event \( e \overset{\text{def}}{=} a \) has a weakest precondition [Dij76] w.r.t. a set of target states \( Q' \) denoted as \( \text{wp}(a, Q') \). \( \text{wp}(a, Q') \) is the largest set of states from which applying \( a \) always leads to a state of \( Q' \). Let us now formally define \( \text{wp} \) following [BJM16]. Basically, we directly consider the set of states \( Q \) and \( Q' \) as predicates of the same name. We define the \( \text{wp} \) w.r.t. the five primitive actions as:

- \( \text{wp}(\text{skip}, Q') \overset{\text{def}}{=} Q' \),
- \( \text{wp}(x := E, Q') \overset{\text{def}}{=} Q'[E/x] \) that is the usual substitution of \( x \) by \( E \) as in [Hoa69],
- \( \text{wp}(P \Rightarrow a, Q') \overset{\text{def}}{=} P \Rightarrow \text{wp}(a, Q') \),
- \( \text{wp}(a_1[a_2, Q') \overset{\text{def}}{=} \text{wp}(a_1, Q') \land \text{wp}(a_2, Q') \),
- \( \text{wp}(\forall z.a, Q') \overset{\text{def}}{=} \forall z.\text{wp}(a, Q') \) where \( z \) is not free in \( Q' \).

### 2.2 Predicate Abstraction and Tri-modal Transition Systems

Predicate abstraction [GS97] is a special instance in the framework of abstract interpretation [CC92] that maps the potentially infinite state space \( C \) of a CTS onto the finite state space \( A \) of an abstract transition system via a set of \( n \) predicates \( \mathcal{P} \overset{\text{def}}{=} \{ p_1, p_2, \ldots, p_n \} \) over the state variables. The set of abstract states \( A \) contains \( 2^n \) states. Each state is a tuple \( q \overset{\text{def}}{=} (q_1, q_2, \ldots, q_n) \) with \( q_i \) being equal either to \( p_i \) or to \( \neg p_i \), and we also consider \( q \) as the predicate \( \bigwedge_{i=1}^{n} q_i \). We define a total abstraction function \( \alpha : C \rightarrow A \) such that \( \alpha(c) \) is an abstract state \( q \) where \( c \) satisfies \( q_i \) for all \( i \in 1..n \). By a misuse of language, we say that \( c \) is in \( q \), or \( q \) contains \( c \), or that \( c \) is a state of \( q \).

Let us now define the abstract transitions as \textit{may} ones. Consider two abstract states \( q \) and \( q' \), and an event \( e \). There exists a \textit{may} transition from \( q \) to \( q' \) by \( e \), denoted by \( q \xrightarrow{e} q' \), iff there exists at least one concrete transition \( c \rightarrow c' \) where \( c \) and \( c' \) are concrete states with \( \alpha(c) = q \) and \( \alpha(c') = q' \).

As in [Bal04], we define \textit{must+} and \textit{must−} transitions in addition to \textit{may} ones. The \textit{must+} transitions are \textit{may} transitions that are triggerable from any concrete state of the abstract source state. The \textit{must−} transitions are \textit{may} transitions that can reach any concrete state of the abstract target state. The modalities are evaluated resolving SAT formulas. As abstraction we define Tri-modal Transition Systems (3MTS) in Def. 2. They are transition systems with abstract states and abstract transitions characterized as \textit{may}, \textit{must+} or \textit{must−} labelled transition relations.

**Definition 2 (Tri-modal Transition System)** Let \( \text{Ev} \) be a finite set of event names and \( \mathcal{P} \) be a set of \( n \) predicates. Let \( A \) be a finite set of \( 2^n \) abstract states. A 3MTS is a tuple \((Q, Q_0, \Delta, \Delta^+, \Delta^-)\) where \( Q(\subseteq A) \) is a finite set of states, \( Q_0(\subseteq Q) \) is a set of abstract initial states, \( \Delta(\subseteq Q \times \text{Ev} \times Q) \), \( \Delta^+(\subseteq \Delta) \) and \( \Delta^-(\subseteq \Delta) \) are respectively a \textit{may}, \textit{must+} and \textit{must−} labelled transition relations.
The 3MTS definition above is inspired by the corresponding notion in [Bal04], in its turn coming from the Modal Transition Systems defined in [LT88, GHJ01]. A 3MTS can be associated with every event system (cf. [BJM16] for a formal definition).

An example of a 3MTS, whose ES is described in Fig. 2, is provided in Fig. 3. The four abstract states, named \( q_1 \) to \( q_4 \), appear as circle boxes. The predicates \( p_0, p_1 \) and \( p_2 \) from which they are defined are given explicitly in Section 3. The abstract transitions of \( \Delta \) are represented as arrows labelled with an event name, and the possible mentions \(+\) and/or \(−\) indicating respectively when they are in \( \Delta^+ \) or \( \Delta^- \).

### 2.3 Over-/Under-Approximations Based on 3MTS

We denote by \( q_0 \xrightarrow{e_0} q_1 \xrightarrow{e_1} \ldots \) where \( q_i \xrightarrow{e} q_{i+1} \in \Delta \) for \( i \geq 0 \) an abstract execution, and by \( c_0 \xrightarrow{e_0} c_1 \xrightarrow{e_1} \ldots \) a concrete execution. We say that \( q_0 \xrightarrow{e} q_1 \xrightarrow{e} \ldots \) and \( c_0 \xrightarrow{e} c_1 \xrightarrow{e} \ldots \) are similar when for all \( i \), \( c_i \) is a state of \( q_i \).

An abstraction is an over-approximation of a model when, for every execution of the model, there is a similar execution of the abstraction. In other words, the abstraction may define more and/or longer executions than the model but not less. Any safety properties that hold on such an abstraction also hold on the model, which allows for verifying any safety properties on the abstraction rather than on the model. But for testing, since an over-approximation may define more executions than the model, a test extracted as an execution path of the abstraction may possibly not be instantiable as a model execution.

So testing can take advantage of considering under-approximations rather than over-approximations. An abstraction is an under-approximation of a model when for every execution of the abstraction, there is a similar execution of the model. In other words, the abstraction may define less and/or shorter executions than the model but not more. Thus every test extracted from such an abstraction is guaranteed to be instantiable on the model, to give rise to a concrete test.

In [Bal04] the authors have defined a method to compute an under-approximation by means of the \( \Delta, \Delta^+ \) and \( \Delta^- \) abstract transition relations of a 3MTS.

In [Bal04] it is proven that a sequence of \textit{must−} transitions, followed by at most one \textit{may} transition, followed by a sequence of \textit{must+} transitions, is guaranteed to be instantiable as a connected sequence of concrete transitions. Indeed, as illustrated by the bold sequence in Fig. 1, any concrete state of a \textit{must−} target is reached from some concrete source state, while whatever concrete state is reached by a \textit{must+} transition is possible to leave from. A \textit{may} transition in between joins a necessarily reached state to a necessarily left one. We call such a sequence a \textit{Ball chain}, and we denote it by a regular expression\(^2\) \((\text{must−})^+.\text{may}.(\text{must+})^*\).

### 3 Illustrative Example

Our illustrative example is a simple coffee vending machine (see the ES in Fig. 2). It has a \textit{Balance}, which can be augmented by putting coins of value either 50 or 100 (events

\(^2\)Since a \textit{must} transition is also \textit{may}, we see the central \textit{may} transition as mandatory.
insert50 and insert100 in Fig. 2). Balance may not exceed an arbitrary fixed constant named $MAX_{Bal}$. There are also arbitrary constants for the maximal number of coffees stored in the machine ($MAX_{Cof}$), and the maximal value ($MAX_{Pot}$) of the Pot (the money kept by the machine). Notice that Balance and Pot are multiples of 50. The machine has a Status which indicates if it is switched on (1) or off (0), or out of order (2). When switched on, the machine can serve coffees, after a request by the user (event cofReq that corresponds to pressing the “request coffee” button), at the price of 50 each (event serveCof): this price is retrieved from the Balance and sent to the Pot. The number of available coffees is modelled by the CofLeft variable. The user can ask for its change (event changeReq that corresponds to pressing the “give change” button). The events changeReq and cofReq are mutually exclusive. The user can then get its unused balance back (event backBalance). When switched off, the machine can be refilled with coffee (event addCof), and its Pot retrieved (event takePot). The events powerUp and powerDown are for switching the machine respectively on or off. Finally, a special event (autoOut) sets the machine out of order: it models the unexpected occurrence of a failure while the machine is in use. It also occurs when either there is no more coffee, or the Pot is full (see serveCof). Figure 3 represents the 3MTS of the ES in Fig. 2 for the three following predicates $p_0$, $p_1$, and $p_2$ that are respectively the guards of the events takePot, autoOut and powerDown.

4 Ball Chains Computation and Instantiation

This section presents our method for computing both an abstraction that is a 3MTS, and an under-approximation.
4.1 Approximated Transition System ATS

The reunion of both the abstraction and its under-approximation we call an Approximated Transition System (ATS), defined in Def. 3.

**Definition 3 (Approximated Transition System)** Let \( \langle Q, Q_0, \Delta, \Delta^+, \Delta^- \rangle \) be an 3MTS. A tuple \( \langle Q, Q_0, \Delta, \Delta^+, \Delta^- \rangle \) is an ATS whose \( \langle C, C_0, \Delta^c, \alpha, \kappa \rangle \) is a concretization of the 3MTS where:

- \( C, C_0 \) are sets of respectively concrete states and concrete initial states,
- \( \Delta^c(\subseteq C \times \text{Ev} \times C) \) is a concrete labelled transition relation,
- \( \alpha \) is a total abstraction function from \( C \) to \( Q \),
- \( \kappa \) is a total coloration function from \( C \) to \{green, blue\}.

The concrete part \( \langle C, C_0, \Delta^c \rangle \) is an under-approximation of the labelled transition system that is the semantics of the event system from which the 3MTS is deduced. In the rest of the paper, for the abstract states, we distinguish between the *may-reachability* and the *reachability*. The former is the reachability by the abstract *may* transition relation \( \Delta \), and the latter is the reachability by the concrete transition relation \( \Delta^c \) in the ATS. We say that an abstract state \( q \) is reachable if there exists at least one concrete instance of \( q \) that is reachable thanks to the transition relation \( \Delta^c \). By extension, an abstract transition is reachable if there exists at least one concrete instance in \( \Delta^c \) whose source state is reachable. The concretization of the *may* transitions is performed on the fly during the computation of the 3MTS. The algorithm for doing this is given in [JKMV17], and is summarized as follows. It guarantees that every *may* transition between two abstract states is concretized.

A total abstraction function \( \alpha \) maps each concrete state of \( C \) to an abstract state of \( Q \). Adapted from [VY03], a coloration function \( \kappa \) maps each concrete state of \( C \) to a colour: green for the reachable states, and blue for those whose reachability is unknown. It allows colouring the concrete transitions to reflect how they are known to be reachable: green for certain reachability, blue for uncertain.

4.2 Ball Chains Instantiations

In this paper, we complete the under-approximation computed by the algorithm (summarized above) of [JKMV17], with a concretization of the Ball chains defined by the *must*+ and *must*− transitions. We proceed separately with the *must*+ and the *must*− chains. For the former we concretize forwardly, by simple DFS, any *must*+ chain of each *must*+ structure (see Fig. 4(c) and Fig. 4(a)). The DFS is launched from any *must*+ transition.
without predecessor. If all \textit{must}+ transitions have a predecessor, the DFS is launched from a transition arbitrarily chosen in a strongly connected component. The algorithm is straightforward and is not presented in this paper. In order to reconnect when possible the (as yet) unreached transitions, it connects in priority a green instance of the source state if available, to a blue instance of its target state. Exemplified with Fig. 4(a), it tries to connect a green instance of state 1 to a blue instance of state 2. If no such blue target instance is available, a green one is used instead. And if none of the source instances is green, the transition is concretized in blue.

Figure 4. Examples of \textit{Must} Structures and their Concretizations

4.3 Concretization Algorithm of the \textit{must}− Transitions

The concretization of the \textit{must}− structure (see Fig. 4(d) and Fig. 4(b)) is performed as described by Alg. 1. It proceeds in two steps. First, it explores–backwardly and symbolically–a path of the \textit{must}− structure from its final state (state 1 in Fig. 4(d) and Fig. 4(b)). So it computes the weakest precondition $wp_\ q$ of the initial state of the path (for example, either state 4, 6 or 7 in Fig. 4(d)), that allow reaching the final state. Second, it chooses if available a green state in $wp_\ q$, and executes–this time forwardly and concretely–the path until the final state, which it colours in green in this case. If none of the states in $wp_\ q$ is green, the path is coloured in blue.

Algorithm 1 concretizes \textit{must}− structures that are either trees (see Fig. 4(d)) or strongly connected components having possibly a tail (see Fig. 4(b)). The concretization is performed from a “root” transition $qr_\ e \rightarrow qr_\ e'$: actually it is a transition with no successor, such as transition $2 \rightarrow 1$ in Fig. 4(b), called root because the exploration is performed backwardly. In a strongly connected component without tail, the root is chosen arbitrarily. The outer \textit{while} loop, in line 3, enumerates a set of paths spanning the \textit{must}− structure. The paths are computed backwardly from the root. A path in the algorithm is a sequence of \textit{must}− transitions, where each transition $t = q \rightarrow q'$ is stacked as a pair $\langle t, wp_\ q \rangle$ that associates the transition itself with the weakest precondition w.r.t. $q'$ of the event $e$ it applies. At each transition branching, one of the transition is explored and added to the path, while the other ones are backed up with the current state of the path into a stack $pb$, for a future exploration (\textit{while} loop, lines 4 to 14). This being done, the current path is recorded in the stack $p$, ready for forward concretization, and the other paths are backed up in the stack $pb$. Concretization starts in line 15 by choosing a state in the current $wp_\ q$ (that of the start of the path), possibly green if any and blue otherwise. Then the \textit{while} loop in lines 16 to 21 concretizes forwardly the current path by pooping out from $p$ the transitions one by one, each time applying the event to the last obtained state instance, and propagating the green or blue colour. Last, the conditional lines 22 to 28 backtrack to the nearest backed up branch, for exploring the next path of the tree.
Algorithm 1: ATS Computation of Must- Ball Chains

<table>
<thead>
<tr>
<th>Inputs</th>
<th>: $qr \xrightarrow{t} qr'$: the root transition of a Must- tree $(X, I, Init, EvDef)$: an Event System where $EvDef \stackrel{def}{=} {e \stackrel{def}{=} a \mid e \in Ev}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Variables</td>
<td>: $t$: the current transition in the Must- tree $q \xrightarrow{t} q'$ $wp_{-q}$: $wp(e,q')$ $p$: path traveled, stored as a stack; from the root $pb$: stack of the branchings remaining to handle $B$: set of the branches that reach the current state $q$ $M^- \rightarrow boolean$ transitions marking function ($\rightarrow boolean$)</td>
</tr>
</tbody>
</table>

1. $pb := \emptyset$; $p := \emptyset$; $t := qr \xrightarrow{t} qr'$; $wp_{-q} := wp(e,q') \land qr$;
2. $B := \{qr \xrightarrow{t} qr'\}$; $M^- := \Delta^- \times \{false\}$; $push(p,(t,wp_{-q}))$;
3. while $B \neq \emptyset$ do /* spanning path whose root is in $B$ */
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Figure 5 shows the reachable (i.e. green) concrete part of the ATS of the 3MTS of Fig. 3 that was obtained by our method. The full experimental results for this example can be found in Table 1 in Section 5.2 on implementation and experiments: see the CM case, line AP=2 (i.e. 2nd set of abstraction predicates). The 3MTS is constituted of 4 abstract states and 17 abstract transitions, amongst which 1 is both must– and must+, 1 is must− only, 6 are must+ only and 9 are may only. All the abstract states are covered and 15 out of the 17 abstract transitions are covered (only the transitions $q_2 \xrightarrow{serveCof} q_1$ and $q_2 \xrightarrow{serveCof} q_3$ are not covered). We obtain 18 reachable concrete transitions, 15 of which coming from the concrete exploration (CXP) as performed by the algorithm of [JKMV17], and 3 of which being added by the Ball chains instantiations (BCI, in bold in Fig. 5). These 3 concrete transitions are additional instances of abstract transitions already covered by CXP. But contrarily to the CXP instances, they are connected: in Fig. 5 the bold sequence $q_2 \xrightarrow{autoOut} q_1 \xrightarrow{powerDown} q_4 \xrightarrow{takePot} q_4$ was not covered as a sequence by CXP.

5 Implementation and Experiments

This section introduces in Section 5.1 our proof-of-concept tool used to evaluate the impact of must transitions concretization on the under-approximation. The experimental results
are then provided in Table 1 in Section 5.2, with their analysis in Section 5.3.

5.1 Tool Description

This section describes the general process of test generation using our proof-of-concept tool combining both algorithms. The process is displayed in Fig. 6.

![Figure 6. Tool Process](image)

The model, expressed in the event-B language, and the set of abstraction predicates are given as inputs to the tool. With the help of an SMT solver, the abstract transitions modalities as well as a concrete instance of each may transition are computed. This gives a first ATS (see ATS 1 in Fig. 6). Afterwards, again thanks to a solver, a concrete instance of each $\text{must}^+$ structure and each $\text{must}^-$ structure in the 3MTS is computed. This produces a possibly enriched concretization which, together with the previously computed 3MTS, constitutes an enhanced ATS (see ATS 2 in Fig. 6). The tests generation uses a JAVA implementation of the Chinese Postman algorithm proposed in [Thi03]. The output of this algorithm is the shortest path (a sequence of transitions) covering all reachable transitions in the CTS at least once, therefore constituting instantiable tests whose steps are concrete transitions.

Developed in JAVA version 8, the tool is designed as a multipurpose library for event oriented systems analysis and simulation. Among other features, this library proposes pre-implemented easy-to-use functions to compute the abstraction of a system along with its transitions modalities (a 3MTS), compute concrete instances of abstract states or transitions, compute the reachable states and transitions of a CTS, apply a substitution to a state, etc. The library can also be used as a binding for SMT-Lib 2.0 standard compliant SMT solvers (such as Z3 [dMB08]), since it allows building first order logic formulas, translating them into a SMT-Lib 2.0 program, and checking for their satisfiability and looking for a concrete model if applicable.

The complete source code can be downloaded at https://github.com/stratosphr/_StraTest_. A complete tutorial about how to install and use the tool can be found at https://github.com/stratosphr/_StraTest_/wiki.
5.2 Experimental Results

This section provides the experimental results obtained with the two approaches. We compare the results on a set of four realistic event systems, with three to five different sets of abstraction predicates for each of them. The set of examples is composed of an electrical system (EL) taken from [BJM11], a car alarm system (CA) taken from [ABJK11], the coffee machine system (CM) presented in Section 3, and a phone book system (PH) taken from [UL06]. Note that the results for the set of abstraction predicates used for the CM system in Section 3 are highlighted using a bold font in Table 1.

The description of the columns appearing in Table 1 is the following: **Sys** indicates the system under test, **#Ev** is the number of events in the system, **AP** is the index of the set of abstraction predicates, **#AS** and **#AT** are respectively the number of abstract states and transitions in the 3MTS, **#M** is the number of may transitions having neither the must—a nor the must+ modality, **M**— and **M+** are respectively the number of must—a and must+ transitions, **Alg**. is the algorithm used (CXP for the concrete exploration method presented in [JKMV17] and BCI for the Ball chains instantiation method presented in this paper, that completes CXP), **#ASreach** is the number of abstract states covered by the tests, **#ATreach** is the abstract states coverage (in %), i.e. **#ASreach / #AT**, **#ATreach** is the number of abstract transitions covered by the tests, **#CTreach** is the number of concrete transitions in the 3MTS, **#CTreach** is the number of concrete transitions appearing in the tests, **#Steps** is the number of tests steps, **Time** is the ATS computation time (in seconds).

The main results reside in the **τ reach** and **τ AS** columns of Table 1. They show that the Ball chains concretization tends to concretize indeed reachable concrete transitions and to increase the tests steps.

All experiments have been led using the Z3 SMT solver [dMB08] on an Intel(R) Core(TM) i7-4710MQ CPU @ 2.50GHz, with 16GB of RAM.

5.3 Analysing the Results

This section analyses the results presented in Table 1.

Except for two cases (see the **PH** system with the second and third **AP**), the con-
cretization of \textit{must}− and \textit{must}+ transitions does not increase the abstraction coverage. This result shows that either all computed \textit{must} transitions were already covered by the CXP method, because they also are \textit{may} transitions, or that the Ball chains concretization did not successfully connect the concretized transition to the reachable part of the first ATS.

While the abstract states and transitions coverage are not improved by the Ball chains concretization, the number of reachable concrete transitions is increased for thirteen cases out of sixteen by 28% on average. This means that, on average, 72% of the total number of reachable transitions in the final CTS where concretized by the CXP algorithm. The difference between the \#CT\textsubscript{reach} row for the BCI method and the \#CT\textsubscript{reach} row for the CXP method gives the number of new reachable transitions brought by the BCI method. Even if this number may seem low, the contribution brought by the BCI still results in an increased number of test steps by 38.8% on average. Note that on some cases, the Ball chains concretization allows to cover concrete transitions which were previously not reachable in the ATS obtained with the CXP method. This is the case for instance for the PH system with the second set of abstraction predicates where twenty-nine concrete transitions were reachable out of the thirty-one. With the Ball chains concretization, fourteen new concrete transitions are computed, which results in sixteen transitions becoming reachable. This means that two previously unreach able transitions concretized by the CXP method are reached thanks to the concretization of the Ball chains.

The BCI computation time is correlated with both the number of \textit{must} transitions and the number of branches in the \textit{must} structures (see Fig. 4, Section 4). This correlation clearly appears for the PH system with the fourth set of abstraction predicates, where most of the sixty-two abstract transitions have at least one \textit{must} modality, and most have both the \textit{must}− and \textit{must}+ modalities. In this case, the \textit{must} concretization is much slower than the CXP ATS computation. This is due to the complexity of the BCI algorithm, that is time exponential in the number of branchings of the \textit{must}− tree.

Finally, let us notice that the progression of reached concrete transitions brought by BCI (i.e. the difference between two successive \#CT\textsubscript{reach} rows) is roughly correlated to the number of \textit{must}− transitions (with about 1 or 2 units of difference). This might result from the backward symbolic exploration over the \textit{must}− transitions, that tends to create new start states for the concrete sequences. By now, confirming this point would require further experiments.

As a conclusion, these experimental results show that, although the BCI does not noticeably improve the coverage of the states and transitions of the abstraction, it enhances the concrete exploration of the system by adding new test steps.

6 Related Work

In [NK00] as well as in [PPV07], the set of abstraction predicates is iteratively refined in order to compute a model bisimilar to the initial semantic model when it exists. None of these two methods is guaranteed to terminate, because of the refinement step that sometimes needs to be repeated endlessly. SYNERGY [GHK+06] and DASH [BNR+10] combine under-approximation and over-approximation computations to check safety properties on programs. As we aim to provide an efficient method to build a \textit{reachable} under-approximation of a system that covers all abstract states and all abstract transitions w.r.t. a specification and a set of predicates, our algorithm does not refine the approximation and, consequently, it always terminates.

The closest methods to the algorithm of [JKMV17] are those that are proposed in [GGSV02] and in [VY03]. For Alg. 1 we combine them with those proposed in [Bal04]. These approaches propose algorithms that compute an under approximated concretization of a predicate abstraction covering its abstract states and transitions. Both these methods are exploited for generating tests. In this paper we are particularly concerned with the differences
between Alg. 1 and the method presented in [Bal04]. The main difference consists of the
fact that the reachability of the under-approximation is guaranteed in [Bal04] and applied
to C programs without abstracting the program counter. In contrast, with ES the control
flow can be abstracted being implicit and depending of many state variables. To address
this problem we propose an heuristics thanks to the coloration method inspired of the algo-
rithm in [VY03]. Our algorithm emphasizes the concretization of Ball’s chains from green
states, i.e. reached concrete states, computed by the first step (algorithm in [JKMV17]).
This heuristics is implemented thanks to an original backward symbolic execution of must−
chains.

Some other work compute under-approximations for generating tests from an abstrac-
tion. The tools Agatha [RGLG03], DART [GKS05], CUTE [SMA05], EXE [CGP+06] and
PEX [TdH08] also compute abstractions from models or programs, but only by means of
symbolic executions [PV09]. This data abstraction approach computes an execution graph.
Its set of abstract states is possibly infinite whereas it is finite with our method.

Our method can be applied to generate tests as the concolic execution of [SMA05]. The
concolic method allows the user to generate structural tests of systems covering partially
the control flow that must be elaborated. Our approach allows us to generate tests covering
the paths defined by the set of abstraction predicates for systems whose control flow is
implicitly defined.

7 Conclusion and Perspectives

We have presented a method that computes instantiated model-based tests from a tri-
modal abstraction of an event system. It proceeds by adapting to event systems two under-
approximation approaches issued from literature: the concrete exploration of [VY03] and
the instantiation of the Ball chains of [Bal04]. We have experimented with combining both
methods, and evaluated their complementarity. Our experimental results show that the
Ball chains instantiations do not improve the coverage of the abstract states and transi-
tions already achieved by the concrete exploration. But they explore more of the concrete
system by prolonging the tests sequences issued from the concrete exploration. The added
computing cost remains negligible, despite the must− instantiation’s complexity, as long as
the number of must transitions is reasonable.

This work opens up a number of perspectives. In particular, the coverage achieved by
the added test steps in other terms than abstract states and transitions coverage remains
to be evaluated. As presented in [BJM16], the abstraction predicates in our work originate
from a test purpose, i.e. a peculiar sequencing of some selected event applications. That
favours these events to apply as must+ or must− transitions, and thus appearing in the
Ball chains. As a result, the additional test steps by our method could cover those peculiar
event sequences as defined by the test purpose. This is illustrated by the example in Fig. 5,
where the three transitions added by the concretization of the Ball chains are applications
of the three events of the test purpose, the guards of which being the abstraction predicates.

More generally, by controlling the size of the abstractions, our method could aim at
using k-path coverage criteria for generating tests, rather than abstract state and transition
coverage. Finally, among all the Ball chains computed, only those that connected directly
to the concrete exploration have been kept in our under-approximation, the reachability of
the others being uncertain. Still, seeking for indirect connections towards those uncertain
chains could be a valuable effort, since this could provide bridges towards previously ignored
connected instance sequences. For example, for the CM example of Fig. 5, there are sev-
enteen unreached concrete transitions, and nine of which are in a connected structure (not
showed in the figure). Connecting this structure to the one that appears in Fig. 5 would
significantly improve the quality of the under-approximation.
References


