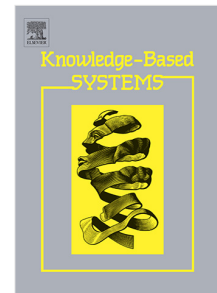


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# Adaptive early classification of temporal sequences using deep reinforcement learning

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## Abstract

In this article, we address the problem of early classification (EC) of temporal sequences with adaptive prediction times. We frame EC as a sequential decision making problem and we define a partially observable Markov decision process (POMDP) fitting the competitive objectives of classification earliness and accuracy. We solve the POMDP by training an agent for EC with deep reinforcement learning (DRL). The agent learns to make adaptive decisions between classifying incomplete sequences now or delaying its prediction to gather more measurements. We adapt an existing DRL algorithm for batch and online learning of the agent's action value function with a deep neural network. We propose strategies of prioritized sampling, prioritized storing and random episode initialization to address the fact that the agent's memory is unbalanced due to (1): all but one of its actions terminate the process and thus (2): actions of classification are less frequent than the action of delay. In experiments, we show improvements in accuracy induced by our specific adaptation of the algorithm used for online learning of the agent's action value function. Moreover, we compare two definitions of the POMDP based on delay reward shaping against reward discounting. Finally, we demonstrate that a static naive deep neural network, i.e. trained to classify at static times, is less efficient in terms of accuracy against speed than the equivalent network trained with adaptive decision making capabilities.

*Keywords:* early classification, adaptive prediction time, deep reinforcement learning, temporal sequences, Double DQN, trade-off between accuracy vs. speed

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## 1. Introduction

Early classification (EC) of temporal sequences with measurements collected dynamically over time is of prime importance in time-sensitive applications. When each measurement can be costly or when it is critical to act as early as possible, there is a need for methods to make fast online predictions. This is for example the case in the field of health, where it is necessary to provide a medical diagnosis as soon as possible from the sequence of medical observations collected over time. Another example is predictive maintenance with the objective to anticipate a machine's breakdown from its sensor signals.

Taking into consideration that some incomplete sequences can be classified using fewer measurements than more complex ones, an EC method should make decisions with adaptive prediction time. It should adaptively decide to classify an incoming yet incomplete sequence now or to delay the prediction to gather more measurements. The method should balance its decision between two competitive objectives: classification earliness and accuracy.

### 1.1. Related work

As opposed to static data, temporal sequences are dynamic data that can be sequentially completed with new measurements over time. In the literature, classification on other types of dynamic data has been proposed by several authors which turned this problem as a sequential decision problem.

Formulated as "learning when to stop thinking and do something" in [1], this problem was tackled by reinforcement learning (RL). The authors were interested in "anytime algorithms" that can be interrupted at any time and for which we assume that the longer they "think", the better the quality of their response. In particular, the authors seek to build a policy that decides if an anytime algorithm should continue thinking or if it should return its current best answer. Their approach is policy-gradient-based and uses REINFORCE algorithm from [2].

In [3], a Markov decision process (MDP) is formulated for the problem of text classification for which it is not always necessary to read an entire document to classify its content. By RL using approximate policy iteration, the authors propose a method that either continues reading a document sentence by sentence, or classifies it (using a support vector machine). Their method is shown to better accommodate to small training datasets than standard non-sequential classifiers.

The approach proposed in [3], working on a single feature (the sentence), was extended to multiple features by the same authors in [4]. The key idea is that some data points can easily be classified using few features while others would require more features to achieve an accurate classification. This can be of practical interest in various domains. In medicine for example, online symptom checking for disease diagnosis requires such an algorithm to find key positive symptoms. REFUEL algorithm proposed in [5] is a policy-based method using REINFORCE which encourages a RL agent to discover positive symptoms more quickly. The authors incorporated a potential-based reward shaping in order to

45 adapt the reward according to the observations collected by the agent before and after making an action.

The problem of costly feature acquisition in the medical domain was also addressed in [6] who proposed to optimize the trade-off between classification accuracy and the total feature cost with deep reinforcement learning (DRL) based on Double Deep-Q-Network (DDQN) algorithm from [7]. The authors demonstrated the capability of their algorithm to solve binary classification problems efficiently.

The trade-off between classification accuracy and the prediction time is also of paramount importance in EC applications. Also called early prediction, this problem has been solved using sequential decision methods by various non-DRL approaches in [8, 9, 10, 11, 12, 13].

We proposed in [14] a recent previous work on a DRL approach using online Deep-Q-Network (DQN) algorithm for the multi-class EC problem. Compared to standard EC approaches, this approach offers an end-to-end learning of both the features in the sequences and the decision rules. The end-user thus does not need to perform feature engineering. The simultaneous optimization of both classification accuracy and earliness relies on a trade-off specified by the user in terms of a reward function dedicated to the EC problem.

The framework proposed in [14] applies DQN algorithm in its original form, i.e. in online learning with successive repetitions of 1) interaction collection between the agent and the environment, and its storing in the agent's memory, and 2) update of the agent's policy. It makes the agent's memory unbalanced. Indeed, after each acquisition of a new measurement, the agent can either predict a label or wait for more data. For a classification decision at time  $k$ , the agent collected  $k$  measurements in the sequence and the memory has been filled with  $k - 1$  delay actions against one classification action. The delay action is over-represented. Moreover, since most actions terminate the acquisition process, it is generally unlikely for the agent to reach the end of a sequence. Early prediction times are over-represented as well. The unbalanced memory in both prediction times and actions can lead the agent to learn on sub-optimal interactions and disturb or slow down its overall training.

### 1.2. Contributions

The contributions we detail in the present paper are the following.

(1) We frame EC as a POMDP fitting the two competitive objectives of classification earliness and accuracy. We experimentally compare two definitions of the POMDP based on delay reward shaping against reward discounting.

(2) In order to solve the POMDP and train an EC agent, we adapt DDQN algorithm from [7] in two versions, online learning and batch learning, depending on whether the EC application comes with a finite training dataset or can collect new training data over time.

We introduce three modifications to cope with the aforementioned unbalanced memory issue. The modifications are the following: we make use of an adapted prioritized sampling and prioritized storing when performing experience replay and we simply redefine episode initialization.

90 We experimentally show that these modifications improve the agent’s training in terms of accuracy against speed and make the proposed algorithm more robust to hyper-parameters setting.

(3) In experiments, we demonstrate that static naive deep neural networks trained to classify at static times are less efficient in terms of accuracy against speed than equivalent networks trained with RL and benefiting from decision 95 making capabilities on adaptive prediction times.

The remainder of the paper is organized as follows. Sec. 2 gives background knowledge of RL terminologies and algorithms. In Sec. 3, we define the EC problem. Sec. 4 and Sec. 5 introduce the method by defining and solving a 100 partially observable Markov decision process dedicated to EC. In Sec. 6, we carry out experimental evaluations on the method. Sec. 7 concludes the paper.

## 2. Background of deep reinforcement learning

### 2.1. Reinforcement learning

In RL, the objective is to solve a decision making process characterized by 105 an agent interacting in an unknown environment through trial and error. In each state  $s$  from the state space  $\mathcal{S}$ , the agent can pick some action  $a$  in the set of possible actions  $\mathcal{A}$ . The choice of action  $a$  is dictated by its policy  $\pi$  such that  $a = \pi(s)$ . As a response, the agent receives a reward  $r = R(s, a)$  and moves toward next state  $s' = T(s, a)$  with  $R$  the reward function from the environment and  $T$  its transition model. The interactions  $\langle s, a, r, s' \rangle$  between the agent 110 and the environment go on until the agent reaches a terminal state leading to the end of an episode.

At all time steps  $t \in \mathbb{N}^+$ , the agent seeks to choose actions leading to maximal return defined as the sum of future discounted rewards  $\sum_{k=0}^{\infty} \gamma^k r_{t+k}$ .  $\gamma \in [0, 1]$  115 is a discount factor valuing immediate rewards rather than future rewards. The optimal policy  $\pi^*$  leads to the maximal return.

*State value.* The value of a state  $s \in \mathcal{S}$  is defined as the expectation of return the agent can hope to get starting from that particular state  $s$  and following its policy  $\pi$ .

$$V_{\pi}(s) = \mathbb{E}_{\pi} \left[ \sum_{k=0}^{\infty} \gamma^k r_{t+k} \mid s_t = s \right]$$

*Action value.* The action value (or Q-value) of a state  $s \in \mathcal{S}$  conditioned on an action  $a$  is defined as the expectation of return the agent can hope to get by picking action  $a$  in state  $s$  and then following its policy  $\pi$ .

$$Q_{\pi}(s, a) = \mathbb{E}_{\pi} \left[ \sum_{k=0}^{\infty} \gamma^k r_{t+k} \mid s_t = s, a_t = a \right]$$

Bellman equation allows to decompose the action value as the sum of immediate reward plus discounted action value of the following state.

$$Q_{\pi}(s, a) = \mathbb{E}_{\pi} [r_t + \gamma Q_{\pi}(s_{t+1}, a_{t+1}) \mid s_t = s, a_t = a]$$

If the optimal action value function defined as  $Q^*(s, a) = \max_{\pi} Q_{\pi}(s, a)$  is known, then an optimal policy can be inferred by acting greedily over the Q-function such that  $\pi^*(s) = \arg \max_a Q^*(s, a)$ .

120 To find an optimal policy, we can use two families of methods [15]: policy-based methods approximate the policy function  $\pi$  directly while value-based methods approximate the action value function  $Q_{\pi}(s, a)$  and act greedily over it to derive the policy.

### 2.2. Deep-Q-Network

125 In [16], the authors seek to approximate the optimal action value function  $Q^*$  by a deep neural network  $Q(s, a, \Theta)$  with parameters  $\Theta$ . Through a gradient descent on mini-batches of interactions  $\{< s, a, r, s' >\}$  and using Bellman equation, the DQN algorithm minimizes the loss function from Eq. 1 using two strategies:

$$L(\Theta) = (r + \gamma \arg \max_a Q(s', a, \Theta^-) - Q(s, a, \Theta))^2 \quad (1)$$

- 130 • Experience replay allows to sample mini-batches of past interactions  $\{< s, a, r, s' >\}$  from a replay memory to perform stochastic gradient descent. Samples within a batch are likely to come from independent or remote interactions further reducing correlations in the neural network updates than the original Q-learning algorithm.
- 135 • Q-learning targets are computed with a separate Q-network  $Q(s, a, \Theta^-)$  whose parameters  $\Theta^-$  are updated periodically to remove correlations and improve convergence of the algorithm.

140 *Double Deep-Q-Network.* In order to overcome DQN overestimations of the action values, the authors in [7] introduce DDQN algorithm and modify the loss function to optimize in Eq. 2.

$$L(\Theta) = (r + \gamma Q(s', \arg \max_a Q(s', a, \Theta), \Theta^-) - Q(s, a, \Theta))^2 \quad (2)$$

### 3. Problem definition

Let  $X = (x_1, \dots, x_T) \in \mathbb{R}^{p \times T}$  be a temporal sequence with maximal length  $T \in \mathbb{N}^+$ . At each time step  $t \in [1, T]$ , the measurement  $x_t$  is a vector of  $p \in \mathbb{N}^+$  features. When the temporal sequence is not fully acquired, we say that we  
 145 observe a partial temporal sequence  $X_{:t} = (x_1, \dots, x_t) \in \mathbb{R}^{p \times t}$  with  $t \leq T$ . We suppose we have a training dataset  $\mathcal{D} = \{(X^j, l^j)\}_{j=1..n}$  with  $n$  pairs of complete temporal sequences  $X$  and their associated label  $l \in \mathcal{L}$ , with  $\mathcal{L}$  the set of labels.

*Classification.* A (static) classifier is a mathematical function  $f_{classif}$  mapping from a temporal sequence  $X$  to its label  $l$  such that  $f_{classif} : \{X\} \rightarrow \mathcal{L}$ .

*Early classification.* We define an early classifier as a mathematical function  $f_{\text{early}}$  mapping from a temporal sequence  $X$  to a label  $l$  and predicting the optimal earliest time step  $t^* \in [1, T]$  to perform classification, such that  $f_{\text{early}} : \{X\} \rightarrow \mathcal{L} \times [1, T]$ . The early classifier seeks to optimize the two competing scores of classification accuracy and earliness:

$$t^* = \arg \max_{t \in [1, T]} \text{Acc}(f_{\text{early}}(X_{:t}), l) + \text{Earliness}(t)$$

150 These two objectives are often competitive since for two time steps  $t_1, t_2 \in [1, T]$ , an earlier time step  $t_1 < t_2$  gets a larger score of *Earliness* while its score of *Acc* can decrease due to the lack of information in  $X_{t_1}$  in comparison to  $X_{t_2}$ .

#### 4. Early classification as a Partially Observable Markov Decision Process

155 We defined an early classifier as a model mapping from a temporal sequence  $X$  to a label  $l$  and predicting the optimal earliest time step  $t^* \in [1, T]$  to perform classification. In real-life applications, we do not observe the complete sequence  $X$  but rather sequentially collect new measurements  $x_t \in \mathbb{R}^p$  at each time step  $t \in [1, T]$ . We focus on applications which do not seek to directly predict optimal  
160 time step  $t^* \in [1, T]$  for classification but rather decide online, at each time step  $t$ , to perform classification on the partial sequence  $X_{:t}$  or to delay classification in order to get additional measurements.

To move closer to this objective, we frame EC as a sequential decision making problem represented by a POMDP. We define the POMDP by the tuple  
165  $\{\mathcal{S}, \mathcal{A}, T, R, \mathcal{O}, \gamma\}$  where  $\mathcal{S}$  is the state space,  $\mathcal{A}$  is the action space,  $T$  is the transition model,  $R$  is the reward function,  $\mathcal{O}$  is the observation space and  $\gamma$  is the discount factor. Each element of the tuple is introduced below.

*Agent.* The mathematical function for EC that we seek to optimize becomes the policy of an agent which will interact and train within the POMDP.

170 *States.*  $\mathcal{S}$  is the state space. A state  $s \in \mathcal{S}$  is characterized by the tuple  $s = (X, l, t)$  with  $(X, l) \in \mathcal{D}$  a pair of complete temporal sequence  $X$  and its associated label  $l$  from the training dataset and with  $t \in [1, T]$  the number of time steps observed in the sequence. Since the objective is to predict labels  $l \in \mathcal{L}$  as early as possible, in real-life applications we do not have access to the  
175 full state information. The label and future measurements are unknown and the Markov decision process is said to be partially observable. Such models assume that we cannot directly observe the underlying state but instead receive an incomplete or noisy observation of that state.

*Observations.*  $\mathcal{O}$  is the observation space. An observation  $o$  of a state  $s =$   
180  $(X, l, t)$  is the partial sequence of measurements from  $X$  collected until time  $t$  such that  $o = X_{:t}$ .

*Actions.*  $\mathcal{A}$  is the action space:  $\mathcal{A} = \mathcal{A}_c \cup a_d$ , with  $a_d$  the action of delaying the prediction and with  $\mathcal{A}_c$  the set of classification actions:  $\mathcal{A}_c = \mathcal{L}$ .

*Dynamics.*  $T : \mathcal{S} \times \mathcal{A} \rightarrow \mathcal{S}$  is the transition model. In real-life EC applications, the acquisition of observations is often costly and has to be shortened as much as possible. Once the system decides to perform classification, observations are no longer collected. The transition model  $T$  is defined by:

$$T((X, l, t), a) = \begin{cases} \text{terminal} & \text{if } \{a \in \mathcal{A}_c\} \cup \{a = a_d \cap t = T\} \\ (X, l, t + 1) & \text{if } a = a_d \end{cases}$$

*Rewards.*  $R : \mathcal{S} \times \mathcal{A} \rightarrow \mathbb{R}$  is the reward function. Let  $R(s, a)$  be the reward for taking action  $a$  in state  $s$ . Rewards should encode the objective we want the model to reach, specifically earliness and accuracy in the EC problem.

We choose to reward classification actions according to the accuracy of the predicted label. When the predicted label matches the reference label, we give a positive reward  $R((X, l, t), a = l) = +1$ . On the contrary when the predicted label differs from the reference label, we give a negative reward  $R((X, l, t), a \neq l) = -1$ .

We point out that an objective can be encoded by several reward functions. For a same objective of fast prediction using as few features as possible, the agent is rewarded positively with a score +1 if the classification is correct in [5] while it receives null reward for correction classification and negative rewards for incorrect classifications in [6].

To encode the objective of earliness, the following strategies are possible:

- We could reward the agent based on classification actions only and use a discount factor  $\gamma < 1$  to motivate the agent to get early rewards. The reward function is then defined by

$$R((X, l, t), a) \mapsto \begin{cases} +1 & \text{if } a \in \mathcal{A}_c \text{ and } a = l \\ -1 & \text{if } a \in \mathcal{A}_c \text{ and } a \neq l \\ 0 & \text{if } a = a_d \end{cases}$$

- Or we could shape the rewards for delay with a score depending on time. If the rewards for delay are given all at once at the time of classification, the agent will get sparse rewards which are often difficult to train on as explained in [15]. To avoid sparse rewards, the agent will be given negative rewards at each decision of delay instead of a single reward at the end of delay:  $R((X, l, t), a_d) = -\lambda \times c(t)$  with  $c : [0, T] \rightarrow \mathbb{R}^+$  the cost function of delaying the prediction at time  $t$ , a monotonic non-decreasing function of time.  $\lambda \in \mathbb{R}^+$  is a parameter setting the trade-off between the two objectives. The more important earliness is in comparison to accuracy, the larger  $\lambda$  should be. The will to compromise is application-dependent and the user can set  $\lambda$  to his preference.

We want the penalization for delay to take into account the amount of information the agent has collected so far. The idea is that the more



observations and knowledge the agent has about the sequence, the worst it is to delay. We want a penalty increasing in time  $t$ , in the form of  $\kappa^t$  with  $\kappa > 1$ . We normalize the reward function for delay so that it is bounded independently of the sequence maximal length  $T$ .

The reward function is then defined by:

$$R((X, l, t), a) \mapsto \begin{cases} +1 & \text{if } a \in \mathcal{A}_c \text{ and } a = l \\ -1 & \text{if } a \in \mathcal{A}_c \text{ and } a \neq l \\ -\lambda * \kappa^t / (\kappa^T - 1) & \text{if } a = a_d \end{cases}$$

215 If available, including domain knowledge into the reward function can guide the agent towards a better or faster learning.

*Discount factor.*  $\gamma \in [0, 1]$  is the discount factor. When  $\gamma < 1$ , rewards are discounted and more importance is given to immediate rewards. For episodic environments with short horizons, the cumulative reward is finite and  $\gamma$  can be  
220 set to 1. Environments for EC have horizon of size  $T$  which is the maximal length of sequences.

#### 4.1. POMDP models

We define two models of POMDP for EC, based on delay reward shaping or reward discounting:

- 225 •  $M_{shaping} = \{\mathcal{S}, \mathcal{A}, T, R, \mathcal{O}, \gamma\}$  is a POMDP where delay actions are rewarded negatively over time with  $R((X, l, t), a_d) = -\lambda * \kappa^t / (\kappa^T - 1)$ ,  $\forall t \in [1, T]$  and rewards are not discounted with  $\gamma = 1$ .
- $M_{discount} = \{\mathcal{S}, \mathcal{A}, T, R, \mathcal{O}, \gamma\}$  is a POMDP where rewards are discounted with  $\gamma < 1$ . The action of delay is not rewarded and the agent collects rewards (positive or negative) from classification actions only with  
230  $R((X, l, t), a_d) = 0, \forall t \in [1, T]$ .

#### 4.2. Specificities of the POMDP models

*All but one of the actions terminate the episode.* As defined above, actions are either to predict a label  $l \in \mathcal{L}$  or to delay prediction:  $\mathcal{A} = \mathcal{A}_c \cup a_d$ . Since we terminate the acquisition of new observations once the classification is performed,  
235 all but one of the actions lead to a terminal state. The probability of reaching time  $t$  in an episode tends to zero as  $t$  increases:

$$P(s_t \neq \text{terminal}) = \underbrace{P(a_1 = a_d)}_{\leq 1} \underbrace{P(a_2 = a_d)}_{\leq 1} \dots \underbrace{P(a_{t-1} = a_d)}_{\leq 1} = \prod_{j=1}^{t-1} \underbrace{P(a_j = a_d)}_{\leq 1}$$

*Actions of classification are the rarest.* When the agent classifies at time  $t$ , the episode is composed of  $t-1$  actions of delay for one action of classification. This  
240 results in getting interactions that are mostly composed of delay action.

## 5. Learning the action value with a deep neural network

The action space being finite and small, we choose to learn the action value function and define the agent’s policy  $\pi$  by acting greedily over the action values. The observation space composed of temporal sequences is continuous and therefore the action value function cannot be represented by a finite table with  
 245 action values on all pairs of observations and actions.

We approximate the action value function  $Q(s, a)$  with a deep neural network  $Q(o, a, \Theta)$  with parameters  $\Theta$  defined over the set of observations  $\mathcal{O}$ . From the POMDP definition and by approximating the action value with a deep neural  
 250 network, the method simultaneously learns optimal classification patterns in the sequences and optimal strategic decisions for the time of prediction. The end-to-end learning capabilities of neural networks set the user free from a prior step of feature engineering and definition of prediction rules.

We train the neural network  $Q(o, a, \Theta)$  with DDQN algorithm from [7] to  
 255 find optimal parameters  $\Theta$ . In the following we propose two versions of the algorithm to address the specificities of the EC POMDP, in online learning and batch learning, depending on whether the EC application comes with a finite training dataset or can collect new training data over time.

### 5.1. Batch learning

Since many real-life EC applications come with a finite training dataset, their underlying POMDPs can generate a finite number of episodes to train on. Unlike video games traditionally used in DRL and for which the emulator can generate an infinite number of episodes, these applications cannot collect new data along training. For example, in microbiological diagnostics, data acquisition  
 265 is expensive because of the experiments it requires to conduct, and it is common to be limited in the amount of data that can be collected.

For those applications with a relatively small training dataset, we propose to adapt DDQN algorithm in batch learning, i.e. by decoupling data collection from the agent’s training. We argue that all possible training interactions  
 270 between the agent and the environment can be simulated and stored in an exhaustive replay memory before updating the agent’s policy.

We present in Algo. 1 the adaptation of DDQN to EC in batch learning. The idea is to first build an exhaustive replay memory with all possible interactions and then use prioritized sampling proposed in Sec. 5.1.1 to cleverly learn from it.  
 275 The advantage of a batch version of the DDQN algorithm is to set the agent free from its traditional exploration-exploitation dilemma, leading to fewer hyper-parameters to tune.

#### 5.1.1. Prioritized sampling

DDQN uses a stochastic gradient descent where a mini-batch of interactions  
 280 is uniformly sampled from the replay memory to update the neural networks parameters and minimize the loss function from Eq. 2. A specificity of the POMDP for EC is the over-representation of the delay action  $a_d$  compared to prediction actions  $\mathcal{A}_c$ . With DDQN uniform sampling in the replay memory,

285 batches of interactions will be highly unbalanced and the agent will hardly learn from prediction interactions.

*Related work.* Some work in the literature propose a more efficient management of the agent's replay memory. In [17], the authors propose prioritized experience replay (PER), a method which seeks to sample "important" interactions more frequently than "non important" interactions. The latter allows to learn on 290 difficult or rare interactions on which the agent struggles to predict accurate Q-values, by re-sampling them more often.

In [18], the authors force that a fraction of the mini-batch is associated to interactions with positive rewards. In others words, they give higher priority to interactions with positive rewards and they seek to learn more efficiently from 295 these rewarding interactions.

In this work, we leave aside PER [17] and we propose a less expensive solution inspired by [18]. We choose to exploit the fact that the interactions between the agent and the environment can be easily categorized into subgroups, according to the type of actions selected.

300 Contrary to [18] where sampling is prioritized according to the scalar rewards received in the interactions, we propose to use prioritize sampling by focusing on particular state-action pairs.

*Strategy.* We adapt DDQN with a simple strategy where a fraction of interactions within a mini-batch are forced to come from prediction actions and where 305 the sampling is forced to be balanced among different labels in order to be robust to unbalanced training datasets.

From a replay memory  $\mathcal{M}$  and for each label  $l \in \mathcal{L}$ , we sample a random mini-batch of interactions  $\{ \langle o, a, r, o' \rangle \} \sim \mathcal{M}$  such that the observation  $o$  is associated to a temporal sequence  $X$  of label  $l$ , with fraction  $\mu$  having  $a \in \mathcal{A}_c$ . 310  $\mu \in [0, 1]$  is the sampling parameter.

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**Algorithm 1** DDQN algorithm applied to early classification in batch learning

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**Require:** Environment described by a POMDP  $\{\mathcal{S}, \mathcal{A}, T, R, \mathcal{O}, \gamma\}$  as defined in Sec. 4.1 and corresponding training dataset  $\mathcal{D} = \{(X^j, l^j)\}_{j=1..n}$ .

Sampling parameter  $\mu \in [0, 1]$  and DDQN hyperparameters from [7].

**Ensure:** Action value function  $Q(o, a, \Theta)$  with optimal weights  $\Theta^*$

Store all possible interactions in replay memory  $\mathcal{M}$ :

**for**  $j = 1 \dots n$  **do**

    Sample a training pair  $(X^j, l^j) \sim \mathcal{D}$ .

**for**  $t = 1 \dots T$  **do**

        Compute observation  $o = X_{:t}^j$

**for**  $a \in \mathcal{A}$  **do**

            Compute reward  $r = R((X^j, l^j, t), a)$

            Compute next observation  $o' = T((X^j, l^j, t), a)$ .

            Store interaction  $\langle o, a, r, o' \rangle$  into replay memory  $\mathcal{M}$ .

**end for**

**end for**

**end for**

Randomly initialize weights  $\Theta$ . Set  $\Theta^- = \Theta$ .

**for** step = 1 ... M **do**

    Sample mini-batch of interactions  $\{\langle o, a, r, o' \rangle\} \sim \mathcal{M}$  using *prioritized sampling* from Sec. 5.1.1 with sampling parameter  $\mu$ .

    Update weights  $\Theta$  with gradient descent on loss function from Eq. 2 computed on the mini-batch  $\{\langle o, a, r, o' \rangle\}$ .

    Periodically update  $\Theta^- = \Theta$

**end for**

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### 5.2. Online learning

Solving EC with RL can also be performed in online learning with successive repetitions of data collection and optimization of the policy. This is suitable for EC application allowing for streaming or multi-phases data collection. For example in predictive maintenance, the machine sensor signals are daily monitored and the training dataset for this application could regularly be increased.

To fit to the EC POMDP specificities, we propose in Algo. 2 an adaptation of DDQN algorithm in online learning, with a simple episode initialization strategy (Sec. 5.2.2), prioritized sampling (Sec. 5.1.1) and prioritized storing (Sec. 5.2.1).

#### 5.2.1. Prioritized storing

To avoid possible overwriting of the delay action  $a_d$  in the replay memory, we propose to allocate a fraction of the memory to prediction actions. With this strategy, delay actions will not be stored with the same importance than prediction actions and will be more often replaced.

### 5.2.2. Episode initialization

To answer our objective of fast decision making, the agent has little interest in postponing prediction and reaching the end of temporal sequences. Therefore a static episode initialization at time  $t = 1$  would cause early prediction times to be over-represented in the replay memory. In Algo. 2, we adapt DDQN with a random episode initialization. We start an episode at random time in the temporal sequence to compel the agent to explore and train on all times of the sequence acquisition.

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**Algorithm 2** DDQN algorithm applied to early classification in online learning

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**Require:** Environment described by a POMDP  $\{\mathcal{S}, \mathcal{A}, T, R, \mathcal{O}, \gamma\}$  as defined in Sec. 4.1 and corresponding training dataset  $\mathcal{D} = \{(X^j, l^j)\}_{j=1..n}$ .

Sampling parameter  $\mu \in [0, 1]$  and DDQN hyperparameters from [7].

**Ensure:** Action value function  $Q(o, a, \Theta)$  with optimal weights  $\Theta^*$

Randomly initialize weights  $\Theta$ . Set  $\Theta^- = \Theta$ . Initialize replay memory  $\mathcal{M}$ .

**for** episode = 1 ... M **do**

Initialize episode observation  $o_t$  with *episode initialization* from Sec. 5.2.2

**while** episode not *terminated* **do**

The agent receives observation  $o_t$  and picks action  $a_t = \arg \max_{a \in \mathcal{A}} Q(o_t, a, \Theta)$  with probability  $\epsilon$  or random action with probability  $1 - \epsilon$ .

The environment computes reward  $r_t = R((X, l, t), a_t)$  and next observation  $o_{t+1} = T((X, l, t), a_t)$ .

Store interaction  $\langle o_t, a_t, r_t, o_{t+1} \rangle$  into replay memory  $\mathcal{M}$  according to *prioritized storing* from Sec. 5.2.1.

Sample mini-batch of interactions  $\{\langle o, a, r, o' \rangle\} \sim \mathcal{M}$  according to *prioritized sampling* from Sec. 5.1.1 with sampling parameter  $\mu$ .

Update weights  $\Theta$  with gradient descent on loss function from Eq. 2 computed on the mini-batch  $\{\langle o, a, r, o' \rangle\}$ .

Periodically update  $\Theta^- = \Theta$

Increment time  $t = t + 1$

**end while**

**end for**

---

*Batch learning or online learning?* We point out that the two versions of the algorithm can be combined in the specific case where the user has a finite training dataset at first and will later collect additional training samples. It is possible to first build an exhaustive memory from the finite available training dataset, learn a policy in batch learning, and then update the policy in online learning while processing newly collected data as they arrive.

## 340 6. Experimental evaluation

The experimental objectives are threefold: (1) We evaluate the effect of delay reward shaping against reward discounting in the definition of the POMDP.

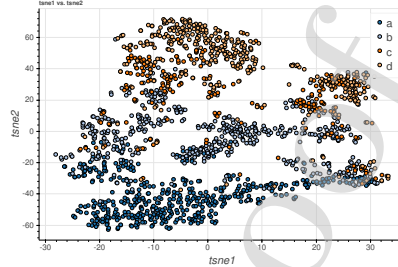
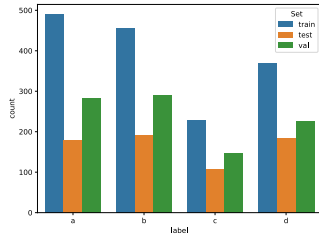


Figure 1: Distribution of labels  $a$ ,  $b$ ,  $c$ , and  $d$  among the sets of training, validation and testing. Figure 2: Two-dimensional t-SNE embedding of the temporal sequences from the training set.

(2) We compare early classifiers with adaptive prediction time capabilities to equivalent naive deep neural networks trained to classify at static times. (3) We assess performance gain brought by our specific adaptation of DDQN algorithm.

### 6.1. Dataset

*Data.* We conduct experimental evaluations on a dataset collected from a private project carried out by bioMérieux company. Data are multivariate time series derived from living organisms. The EC application is related to an in-vitro microbiological diagnostic and seeks for rapid categorization of the living organisms described by MTS. The 3155 temporal sequences  $X = (x_1, \dots, x_T)$  have length  $T = 77$  and each measurement  $x_{i \in [1, T]}$  is a 5-dimensional array. With previous notations from Sec. 3,  $X \in \mathbb{R}^{5 \times 77}$ .

This real-life example can be generalized to industrial problems with the same EC objective on multivariate or univariate temporal sequences. In previous work [14], we compared the RL framework to state-of-the-art methods on the UCR archive from [19] which is widely used as benchmark for classification and clustering of time series. We point out that the autonomous learning of features for decision-making and classification makes the proposed method applicable to data on which we have no features expertise. Indeed, we did not have any prior knowledge on these public datasets.

*Labels.* Sequences are associated to labels  $a$ ,  $b$ ,  $c$ , and  $d$  depicting four classes of living organisms. Fig. 1 gives the distribution of the labels among the training, validation and testing sets.

*t-SNE projection.* In Fig. 2, we represent the training set with a two-dimensional t-SNE embedding of the (complete) temporal sequences using algorithm from [20]. We observe overlapping clusters of points from different labels. Samples from class  $b$  and  $c$  are often mixed among the same clusters of points. This illustrates the complexity of the dataset in which sequences from different classes are very similar due to the biological variability in the dataset.

## 6.2. Evaluation pipeline

In Sec. 4, we framed EC as a sequential decision making problem defined by a POMDP. We proposed to solve the POMDP by training an agent with RL in Sec. 5. In this section, we introduce metrics and procedures used to train the agent, select optimal policies and compare performance between trainings.

### 6.2.1. Hyper-parameter setting

In Sec. 5, the agent is defined by its policy whose model is a deep neural network  $Q(o, a, \Theta)$  with weights  $\Theta$  trained with DDQN algorithm. The deep neural network training depends on a set of hyper-parameters to define. The combinatorial space of the hyper-parameters being too large, we cannot perform an exhaustive search.

To fine-tune the method, we randomly select a set of hyper-parameters in a restricted combinatorial space near optimal parameters presented in [16]. We dedicate one agent per setting of hyper-parameters. Agents are trained separately between all settings.

### 6.2.2. Training procedure

When trained under supervision (for static classification or regression tasks), deep neural networks are updated until the loss function stops decreasing on the validation set. The selection of the best deep neural network model is also straightforward: the selected model is the one with highest performance on the validation set. When trained with reinforcement, the loss function is based on an approximation of future cumulated rewards and is typically not used to stop the training procedure or to select optimal policies either.

Instead, for each hyper-parameter setting of the method, we independently train an agent for a fixed number of episodes in the environment, until it reaches 100000 updates of its deep neural network weights  $\Theta$ . We simultaneously evaluate the agent of each setting on the validation set every 1000 updates of  $\Theta$ . Fig. 3 reports the evaluations performed during an agent's training.

### 6.2.3. Evaluation metrics

*Accuracy.* We define the agent accuracy  $Acc$  on a dataset  $\mathcal{D} = \{(X^j, l^j)\}_{j=1..n}$  as

$$Acc = \sum_{j=1}^n \mathbb{1}(f_{classif}(X^j) = l^j) / n$$

*Time of prediction.* The prediction time  $t_{j,pred}$  of the agent on a sequence  $(X^j, l^j) \in \mathcal{D}$  is defined as the earliest time step for which the action value of a classification action outreaches the action value of delay, such that:

$$t_{j,pred} = \min_{t \in [1, T]} \{ \arg \max_{a \in \mathcal{A}} Q(X_{:t}^j, a) \in \mathcal{A}_c \}$$

The prediction time  $t_{pred}$  of the agent on a dataset  $\mathcal{D}$  is the mean of prediction times on all sequences from the dataset, such that:

$$t_{pred} = \sum_{j=1}^n t_{j,pred}/n$$

#### 400 6.2.4. Optimal policy selection

In [16], the authors evaluate the agent’s policies over training and select the optimal policy as the one with the highest score of reward. In the special case of EC for which two competitive objectives are optimized one against the other, the optimal policy selection can be application-dependant.

405 Among all trainings, each one being dedicated to a set of hyper-parameters, we select the policy with highest *Acc* on the validation set for several ranges of  $t_{pred}$  (as illustrated in Figs. 4, 6 and 7 where the top-5 optimal policies are represented). We then have as many optimal policy candidates as ranges of  $t_{pred}$  considered. Among all candidates, we can then choose the optimal  
410 policy as the one satisfying the most our will to compromise between accuracy and speed. The optimal policy reflects the best performance achieved by the method during its fine-tuning.

#### 6.2.5. Training evaluation

*Best performance.* To assess an agent best performance during its training, we  
415 compute max *Acc*, as illustrated in Fig. 3.

*Mean performance.* To globally assess an agent performance over its entire training, we compute mean *Acc* and mean  $t_{pred}$  over all the agent’s evaluations, that is to say on the 100 policies that were evaluated every 1000 updates of  $\Theta$ , as illustrated in Fig. 3. A large score of mean *Acc* means that the agent  
420 was globally highly accurate all along its training.

*Stability.* We measure the stability of a training through the variation in *Acc* and  $t_{pred}$  with the standard deviation metric (stdev), as illustrated in Fig. 3. A high score of stdev *Acc* means that the policies evaluated along training were not equally accurate and very unstable.

#### 425 6.2.6. Methods comparison

*Best performance.* When comparing several methods, we seek to identify which one gave the best results. Thus we compare the optimal policies results between each method, as illustrated in Figs. 4, 6 and 7.

*Robustness.* We are also interested in assessing the robustness of each method  
430 regarding the hyper-parameter setting. We compare each method through the distribution of max *Acc*, mean *Acc*, stdev *Acc*, mean  $t_{pred}$  and stdev  $t_{pred}$  computed on each training. For each metric, we report the p-values of Mann-Whitney rank statistical tests on the null hypothesis that the two versions are equivalent.



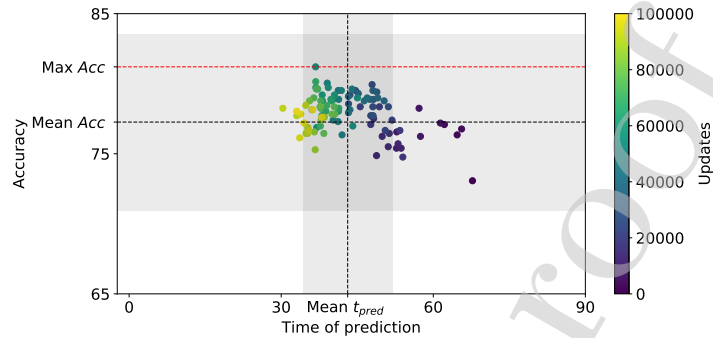


Figure 3: An agent training with 100000 updates of its deep neural network parameters  $\Theta$ . The agent's policy is evaluated every 1000 updates on the validation set. Policies performances are represented with dot points in terms of  $Acc$  vs.  $t_{pred}$ . Dots points are colored according to the updates. The black vertical line (resp. band) gives the agent's mean (resp. stdev)  $t_{pred}$  over training. The black horizontal line (resp. band) gives the agent's mean (resp. stdev)  $Acc$  over training. The red horizontal line gives the agent's maximal  $Acc$  over training.

### 435 6.3. Experimental comparison between two models of POMDP: reward discounting and delay reward shaping

We carry out an experiment to assess the impact of delay reward shaping against rewards discounting in the definition of the POMDP. We compare the two POMDP models  $M_{discount}$  and  $M_{shaping}$  from Sec. 4.

440 *Experimental setting.* We solve each POMDP with DDQN algorithm in batch learning, adapted with prioritized sampling, as introduced in Algo. 1. We perform 50 trainings on each POMDP model (Sec. 6.2.2) by varying the deep neural network architecture and respective specific hyper-parameters. We vary  $\gamma \in [0.3, 1]$  for  $M_{discount}$ ,  $\lambda \in \{0.05, 0.1, 0.25, 0.5, 1, 2\}$  and  $\kappa \in \{1.06, 1.09, 1.1, 1.2\}$   
 445 for  $M_{shaping}$ . Other shared DDQN hyper-parameters are fine-tuned (Sec. 6.2.1).

*Experimental comparison.* To evaluate if both POMDP models achieve comparable best classification accuracy under different trade-offs, we report in Fig. 4 the top-5 optimal policies within ranges of prediction times (Sec. 6.2.4) for both  $M_{shaping}$  and  $M_{discount}$  models.

450 For each model, accuracy rapidly increases when the prediction time reaches  $t_{pred} = 30$  and then increases only very slightly with the acquisition of more measurements in the sequences.

Experiments show that  $M_{shaping}$  results in top-5 policies with higher  $Acc$  than  $M_{discount}$  under all trade-off of prediction time  $t_{pred}$ .

455 We compare the robustness between the two POMDP models by computing metrics from Sec. 6.2.6 which are shown in Fig. 5 and statistically compared in Tab. 1. Tests allow to reject the null hypothesis that both POMDP models achieve comparable max  $Acc$  along training. Fig. 5 shows that  $M_{shaping}$  reaches higher max  $Acc$ .

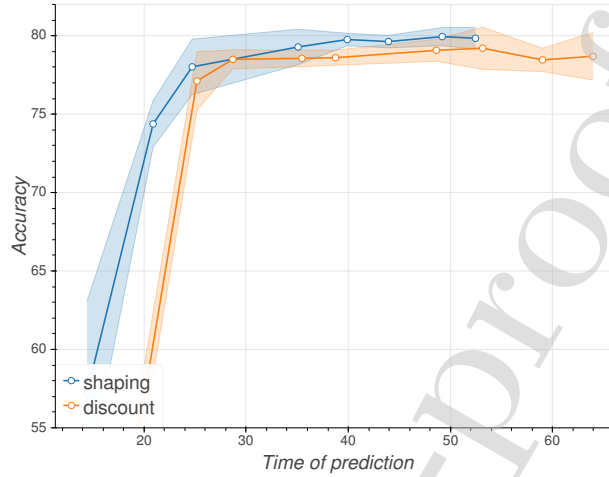


Figure 4: Top-5 policies from  $M_{shaping}$  and  $M_{discount}$ . We select the top-5 policies in  $Acc$  on the validation set for several ranges of  $t_{pred}$ . We evaluate those policies on the test set. The full line represents mean  $Acc$  and the band is the stdev  $Acc$ .

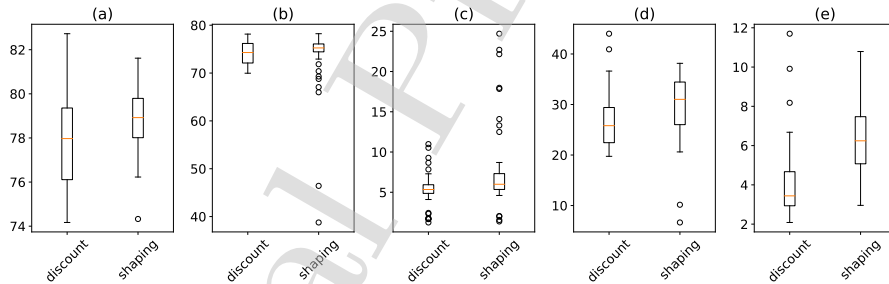


Figure 5: Performance metrics on  $M_{shaping}$  and  $M_{discount}$  on the validation set. (a) Max  $Acc$ . (b) Mean  $Acc$ . (c) Stdev  $Acc$ . (d) Mean  $t_{pred}$ . (e) Stdev  $t_{pred}$ .

460 Also, tests on the stdev  $Acc$  and stdev  $t_{pred}$  lead to the conclusion that  $M_{shaping}$  is more variable than  $M_{discount}$  during its fine-tuning.

#### 6.4. Experimental comparison between early classifier and naive static classifiers

We seek to experimentally measure the added value of our method for EC in comparison to static classification. More precisely, for an agent that would predict on average at  $t_{pred}$ , we seek to evaluate whether a static DNN classifier  
 465 that would make the prediction with the same average speed (but always at the same time step  $t_{pred}$ ) would achieve a better classification quality than the agent.

To perform the evaluation, we deactivate the decision making capability of  
 470 our algorithm, i.e. the RL part, and train the equivalent naive deep neural network to classify at a list of predefined (static) time steps.

Performance			Stability	
Max $Acc$	Mean $Acc$	Mean $t_{pred}$	Std $Acc$	Std $t_{pred}$
<b>0.0228</b>	0.1962	<b>0.0018</b>	<b>0.0016</b>	<b>1.3162e-8</b>

Table 1: **Statistical comparison between  $M_{shaping}$  and  $M_{discount}$  performance metrics.** The table reports p-values of Mann-Whitney rank tests on the null hypothesis that  $M_{shaping}$  and  $M_{discount}$  have comparable metric score for each performance metric (max  $Acc$ , mean  $Acc$ , stdev  $Acc$ , mean  $t_{pred}$  and stdev  $t_{pred}$ ) from Fig. 5. The null hypothesis is rejected in favor of the alternative hypothesis on tests with a p-value below 0.05, shown in bold. The alternative hypothesis is that the metric performance is different between the different POMDP models. Fig. 5 shows which POMDP model has the greatest score.

*Experimental setting.*

**Early classifier** We use experiments from 6.3 on  $M_{shaping}$  solved with Algo. 1 to obtain early classifiers enhanced with decision making capabilities.

475 **Static classifier** For regular time steps  $t \in [1, T]$ , we train equivalent deep neural networks to map between the partial temporal sequences and the labels. We use the training pairs from dataset  $\mathcal{D} = \{(X^j, l^j)\}_{j=1..n}$  and we train deep neural networks as a mathematical function  $f_{classif}$  such that  $f_{classif} : \{X_{:t}\} \rightarrow \mathcal{L}$ . For each regular time step  $t \in [1, T]$ , the deep neural networks are trained  
480 separately until the loss function stops decreasing on the validation set (Sec. 6.2.2).

The neural networks used for both static classification and the agent’s policy are similar except from the output layer. The output layer of the agent’s policy is linear and has an additional neuron for the delay action compared to the  
485 static classifier which has as many neurons as labels and a softmax activation.

*Experimental comparison.* In Fig. 6, we report top-5 policies performance for different ranges of  $t_{pred}$  (Sec. 6.2.4). Both static deep neural network and early classifier have poor  $Acc$  in early times ( $t_{pred} < 20$ ) due to lack of information in the partial temporal sequences.

490 Then the early classifier provides top-5 policies with higher  $Acc$  than static classifiers. The improvement in  $Acc$  for equivalent  $t_{pred}$  is due to the capability of the agent to adapt its classification individually on each temporal sequence. The agent can choose to quickly classify sequences that can easily be categorized or to require more observations on sequences lacking discriminant patterns.  
495 The early classifier’s will to individually compromise makes the classification more efficient than static networks using the same amount of observations in all sequences independently of their complexity.

Interestingly, we cannot evaluate the early classifier in late prediction times ( $t_{pred} > 55$ ). To reach its objective of fast decision making, the agent did not  
500 choose to classify at the end of the sequences and it always provided fastest policies.

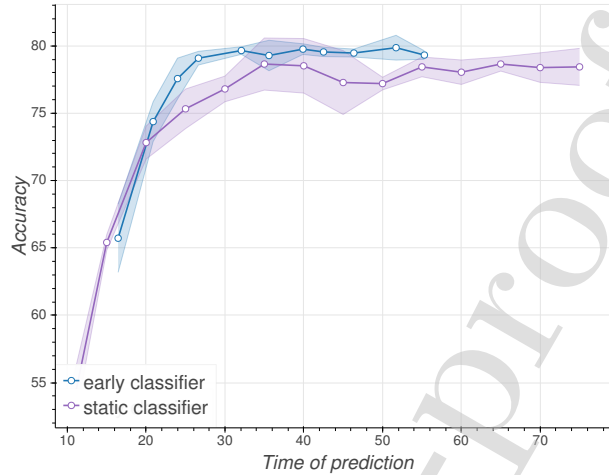


Figure 6: Top-5 policies from  $M_{shaping}$  and top-5 static deep neural network classifiers. We select the top-5 policies and classifiers in  $Acc$  on the validation set for several ranges of  $t_{pred}$ . We evaluate those policies and classifiers on the test set. The full line represents mean  $Acc$  and the band is the stdev  $Acc$ .

#### 6.5. Online learning: Experimental evaluation of prioritized sampling, prioritized storing and episode initialization in DDQN algorithm

We carry out an experiment to assess the impact of prioritized sampling (Sec. 5.1.1), prioritized storing (Sec. 5.2.1) and random episode initialization (sec 5.2.2) when training early classifiers with DDQN algorithm in online learning. We compare four versions of DDQN algorithm to solve  $M_{shaping}$ :

- *DDQN-baseline* refers to original DDQN algorithm [7].
- *DDQN-ps* refers to DDQN with prioritized sampling and prioritized storing proposed in Sec. 5.1.1 and Sec. 5.1.1.
- *DDQN-ei* refers to DDQN with random episode initialization proposed in Sec. 5.2.2.
- *DDQN-ps-ei* refers to DDQN with simultaneously prioritized sampling, prioritized storing and random episode initialization as synthesized in Algo. 2.

*Experimental setting.* All shared DDQN hyper-parameters are first manually fine-tuned (Sec. 6.2.1). On each version of DDQN algorithm, we perform 100 trainings (Sec. 6.2.2). We vary rewards for correct classification  $R((X, l, t), a = l) \in \{0, +1\}$  in order to obtain policies with slow decision making and to be able to compare the four versions of DDQN in late prediction times.

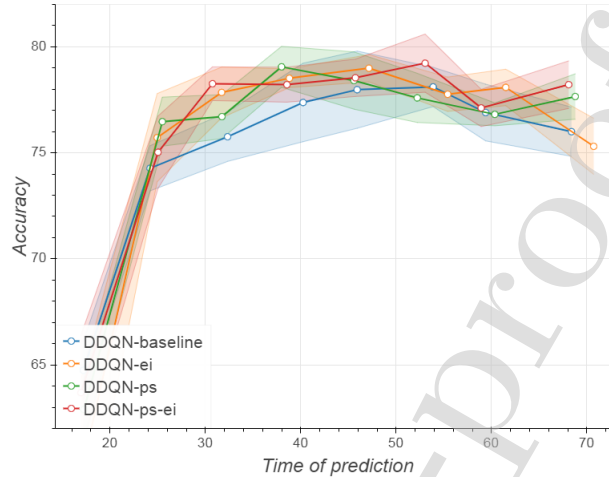


Figure 7: Top-5 policies from *DDQN-baseline*, *DDQN-ei*, *DDQN-ps* and *DDQN-ps-ei* evaluated on the test set. The full line represents mean accuracy and the band is the accuracy standard deviation.

*Experimental comparison.* Top-5 policies (Sec. 6.2.4) on all four versions of DDQN algorithm are shown in Fig. 7.

For each version, accuracy rapidly increases when the prediction time reaches  $t_{pred} = 30$ . Then, accuracy slightly gets better when the prediction time increases up to  $t_{pred} = 40$ . We can observe that accuracy stops increasing (and even slightly decreases in some cases) when the prediction is performed at  $t_{pred} > 50$  approximately. This is due to the particularity of the application for which more time passes and more the biological process associated with different classes will have similar states.

*DDQN-baseline* top-5 policies are globally the least accurate under all trade-offs of  $t_{pred}$ . Top-5 policies with highest *Acc* for different trade-off of  $t_{pred}$  are produced by *DDQN-ei* and *DDQN-ps-ei*. We can see that the different proposed strategies lead to optimal policies which are at least as good or better than those obtained with the original DDQN algorithm.

The distributions of performance metrics from Sec. 6.2.5 are shown in Fig. 8 and statistically compared in Tab. 2.

We first compare the best classification performance achieved by the agent during each of its training sessions, on each version of the algorithm. That is to say, on each of training of the agent, we keep the policy that was the most accurate in classification. Tests from Tab. 2 show that both *DDQN-ei* and *DDQN-ps-ei* improve max *Acc* over *DDQN-baseline*. In other words, these versions of the algorithm result in policies with the best classification quality.

Then, we compare the average performance of the agent during each of its training sessions, by averaging the performance of each of its policies from the same training session. This allows to illustrate the overall performance of the agent throughout its training, and not at a specific moment of its training. Tests

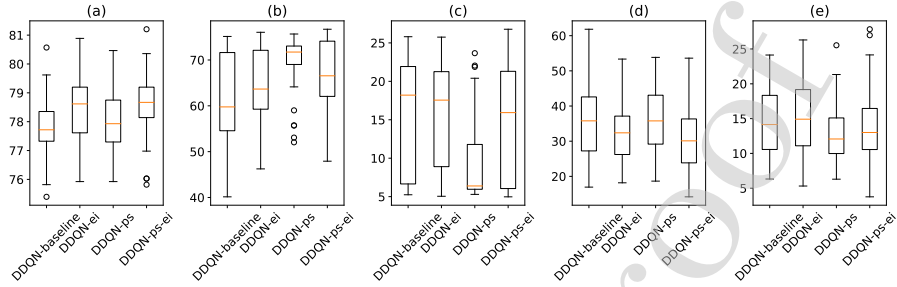


Figure 8: Performance metrics on *DDQN-baseline*, *DDQN-ps*, *DDQN-ei* and *DDQN-ps-ei* on the validation set. (a) Max  $Acc$ . (b) Mean  $Acc$ . (c) Stdev  $Acc$ . (d) Mean  $t_{pred}$ . (e) Stdev  $t_{pred}$ .

from Tab. 2 show that both *DDQN-ps* and *DDQN-ps-ei* improve mean  $Acc$  over *DDQN-baseline* which means that these versions of the algorithm improve the overall classification quality of the agent compared to the baseline.

550 Also, both *DDQN-ei* and *DDQN-ps-ei* shorten mean  $t_{pred}$  over *DDQN-baseline* which means that these versions of the algorithm result in earliest classification times compared to the baseline.

In brief, *DDQN-ps-ei* is then the version of the algorithm that leads to both best classification quality and earliest prediction times simultaneously. Both 555 competitive EC objectives are improved with this version.

In terms of stability, measured through the metrics of stdev  $t_{pred}$  and stdev  $Acc$ , the different versions of the algorithm are comparable except for *DDQN-ps* which is statistically less variable in terms of accuracy compared to *DDQN-baseline*.

560 As a conclusion, *DDQN-ps-ei*, which refers to DDQN combined with all of the proposed strategies (prioritized sampling, prioritized storing and random episode initialization), is the best memory and episode management method because it simultaneously improves the classification performance of the agent and fastens its prediction time.

## 565 7. Conclusion

We defined a POMDP to train an agent for EC with RL. We modelled the agent's policy by a deep neural network and we adapted the DDQN algorithm in order to address the specificities of the POMDP that could lead to unbalanced memory of the agent if applied without modifications. The validity of the 570 method was shown experimentally on a complex multi-class classification problem on a dataset of multivariate temporal sequences with natural variability. We experimentally demonstrated that:

- Shaping the environment reward signal for delay leads to higher accuracy at all prediction times than sparse discounted rewards.

Methods	Performance			Stability	
	Max <i>Acc</i>	Mean <i>Acc</i>	Mean $t_{pred}$	Stdev <i>Acc</i>	Stdev $t_{pred}$
<i>DDQN-baseline</i> vs. <i>DDQN-ei</i>	<b>0.0023</b>	0.1467	<b>0.0430</b>	0.8227	0.6270
<i>DDQN-baseline</i> vs. <i>DDQN-ps</i>	0.2464	<b>0.0001</b>	0.8067	<b>1.7212e−5</b>	0.1090
<i>DDQN-baseline</i> vs. <i>DDQN-ps-ei</i>	<b>0.0001</b>	<b>0.0036</b>	<b>0.0286</b>	0.2263	0.5418

Table 2: **Statistical comparison between *DDQN-baseline*, *DDQN-ps*, *DDQN-ei* and *DDQN-ps-ei* performance metrics.** The table reports p-values of Mann-Whitney rank tests on the null hypothesis that *DDQN-baseline* have a score comparable to *DDQN-ps* and *DDQN-ps-ei* for each performance metric (max *Acc*, mean *Acc*, stdev *Acc*, mean  $t_{pred}$  and stdev  $t_{pred}$ ) from Fig. 8. The null hypothesis is rejected in favor of the alternative hypothesis on tests with a p-value below 0.05, shown in bold. The alternative hypothesis is that the metric performance is different between the different versions of the algorithm. Fig. 8 shows which version has the greatest score.

- 575
- Improvements to DDQN online algorithm such as prioritized sampling, prioritized storing and random episode initialization increase the classification accuracy of the agent while boosting the rapidity of its decision making.
- 580
- The method empirically results in an agent with adaptive fast-classification capabilities which achieves higher accuracy performance than an equivalent neural network trained for static classification.

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