Abstract — The best plano-convex quartz crystals resonators can have quality factors up to a few billion at low temperature, which makes them interesting for ultrastable clocks. For this application, it’s best they are optomechanically actuated. The first step towards this is to demonstrate they can be used as optical Fabry-Perot cavities with almost no change to their typical piezoelectric building. This paper is focused on the feasibility of such optical use.

Keywords — Optics, Quartz Resonator, Fabry-Perot, Optical Cavity, Acoustic Cavity, Optomechanics

I. Introduction, Background

Quartz crystals are used in time standards routinely. Moreover, the quality of synthetic materials have been improved up to the point where the product $Q \times f$ gets to $10^{13}$ for the best ones at room temperature.

Furthermore, such quartz resonators (QR) in the cryogenic 4K region can have quality factors ($Q$) as high as a few billion [1].

Earlier studies [2] have shown that the flicker frequency level of the power spectral density of the fractional frequency fluctuations behaves as $S_y(1 \text{ Hz}) \propto \frac{1}{Q^a}$ with $a \approx 4$. Very good performances can therefore be achieved, with possible fractional frequency deviation floor, or Allan deviation floor, as low as $10^{-16}$.

All these considerations qualify cryo-cooled quartz as a candidate for ultra-stable clock. We need to implement some vibration control and a way to impede performance-limiting frequency instabilities due to temperature fluctuations. The latter problem has been solved [3] by the finding of a specific compensated cut for the quartz crystal in this temperature region.

To be able to actuate the quartz crystal, piezoelectricity is usually called upon. In our setup however, this would bring further noise to account for, because of variable temperature fluctuations at different stages of the solid link between the oscillation sustaining system (at room temperature) and the QR which sits on the cold finger of the cryorefrigirator.

II. Quartz Crystal as a Fabry-Perot Cavity

Typical QR manufactured for frequency references here at FEMTO-ST are plano-convex crystal cavities, with a thickness of few mm with a thin layer (around 5 – 15 nm) of Chromium on the quartz on top of which a much larger layer of Gold (around 200 nm) is deposited. The reason for the Chromium layer is that it sticks well to the quartz, whereas the Gold does not. Gold, in turn, sticks well onto the Chromium layer.

The particular QRs we use are plano-convex 1 mm thick lenses, with a radius of curvature of 250 mm. Figure 1 shows such a metallized QR which does not seem of surface quality incompatible with our uses. In these conditions, the $g$ stability factor for a Fabry-Perot cavity is $g = 0.996$, very close to 1 when instability for optical cavities starts[5].

A way to circumvent this is to actuate the quartz optically instead. Indeed, if we are able to use the radiation pressure, we can avoid thermal dilation fluctuations in the excitation link. Because the radiation pressure is very weak, we use the fact that the two electrodes used for actuating the quartz piezoelectrically also are two mirrors “glued” together with the QR. By sending a laser on these, we can use the radiation pressure of the hence amplified light intensity inside the cavity to create vibrations of our QR. For this, we should modulate the laser intensity at the acoustic frequency[4]. We will first demonstrate the feasibility of using such QR as Fabry-Perot cavities.
Gold, in the infrared region, is reflective to about 98% for ≈ 100 nm layers. It is generally considered that films more than ≈ 200 nm are certain to behave just like their bulk counterpart whereas quantum effects need to be taken into account for films thinner than 20 nm.

All these considerations lead us to believe that a common metallized QR could be used in a straightforward manner as an optical Fabry-Perot cavity. From these, we expect a finesse

\[ F = \pi \sqrt{R} \]

with \( R \) the intensity reflection coefficient of the whole Fabry-Perot cavity. In our case, the finesse should amount to about \( F = 155 \). Furthermore, the typical Fabry-Perot cavity gives a transmission maximum and a reflection minimum for the resonance condition

\[ \lambda = \frac{2m}{n} \]

with \( m \in \mathbb{N}^* \).

III. Experiment, Results

In our experimental setup, the laser, optical isolator and EOM are all fibered as seen in figure 2. We have put a \( \lambda/2 \) plate before the beam splitter to be able to compensate for the birefringence of the QR, and align the polarization of our beam to one of the QR’s fast or slow axes.

Because of the quartz having an index of refraction \( n_{\text{quartz}} \approx 1.54 \), the wavelength inside is modified with respect to that of vacuum. This phenomenon accounted for, the mode-matching demands that we have a waist of 71 \( \mu m \) at the (entrance) plane side, so that the beam’s radius of curvature matches that of the end mirror.

Our first results with Chromium-Gold coated QR were discouraging, and it was found that Chromium was a poor candidate for making a mirror\[7\]. It is indeed the Chromium that the light inside the quartz first “sees”. Eliminating altogether the Chromium layer was investigated, but did not turn out well, as a “blistering”\[8\] effect does not seem to happen as much.

This lead us to use Silver instead, whose intensity reflection coefficient is comparable to that of Gold at our wavelengths, and whose main defect with respect to gold is that it gets oxydated whereas gold does not. On the other hand, Silver sticks better to the quart and the “blistering” effect does not seem to happen as much.

The results obtained for a 60-60 nm Silver metallized QR were surprising, as there was a frequency shift between the extrema of the transmitted and the reflected peaks. As it turns out, this is in fact a known phenomenon\[9\] and it is due to the absorption of the mirrors. The measured difference between the peaks is 58 MHz and the theoretical value is 37.5 MHz.

Contrary to the typical case, the theoretical extrema of transmission and reflection are limited. In our case, the transmission and reflection maxima are theoretically limited to \( T = 4\% \) and \( R_{\text{min}} = 12\% \). We measure, however, a reflection visibility of \( \approx 3\% \) and a transmission of \( \approx 3.10^{-4} \).

IV. Conclusions

The common QR can be used as a Fabry-Perot cavity, by adapting the metallization. Investigation is under progress to better understand the discrepancies between the theoretical and experimental values. A systematic investigation of the bandwidths for the transmission and reflection peaks will be lead.

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REFERENCES


