

Multi-objective Energy Management for Fuel Cell Electric Vehicles using Online-Learning Enhanced Markov Speed Predictor

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Abstract

As one of promising solutions towards future cleaner transportation, fuel cell electric vehicles have been widely regarded as an attractive technology in both academia and industry. To enhance the vehicle's operation efficiency, this paper proposes a multi-criteria power allocation strategy for a fuel cell/battery-based plug-in hybrid electric vehicle. Firstly, an adaptive online-learning enhanced Markov velocity-forecast approach is proposed. Its predictive behaviors can be adjusted accordingly under various driving scenarios through the real-time-identified transition probability matrices. Subsequently, based only on the previewed trip duration information and the speed prediction results, a state-of-charge (SOC) reference planning approach is designed to guide the allocation of battery energy. Combining with the velocity-forecast results and the reference SoC, model predictive control derives the optimal power-allocation decision through minimizing the multi-purpose objective function in a finite time horizon. It has been verified that (1) the presented power allocation strategy can reduce over 12.05% H2 consumption and over 94.40% fuel cell power spikes against the commonly used Charge-Depleting/Charge-Sustaining strategy; (2) despite the existence of mission time estimation errors, the presented control strategy could still bring performance enhancement over the benchmark strategy, thus demonstrating its feasibility for real-world implementations.

Key Words: *Energy Management Strategy, Fuel Cell, Plug-in Hybrid Electric Vehicles, Speed Forecasting Technique, State-of-Charge Reference Generation.*

Nomenclature

Nomenclature		SYMBOLS	
PHEV	Plug-in Hybrid Electric Vehicle	P_d	DC bus Power demand
ICE	Internal Combustion Engine	P_{fc}	PEMFC system net power
FCPHEV	Fuel Cell Plug-in Hybrid Electric Vehicle	P_b	Battery Power
PEMFC	Proton Exchange Membrane Fuel Cell	m_{H_2}	Actual Hydrogen Mass Consumption
FCS	Fuel Cell System	m_{equH_2}	Equivalent Hydrogen Mass Consumption
EMS	Energy Management Strategy	SoC	Battery State-of-Charge
CD-CS	Charge-Depleting Charge-Sustaining	U_{dc}	DC Bus Voltage
SoC	State-of-charge	π_1, π_2, π_3	MPC Penalty Factors
DP	Dynamic Programming	H_p	Prediction Horizon
GA	Genetic Algorithm	T_l	l -step Transition Probability Matrix
PMP	Pontryagin's Minimum Principle	s	Total Number of Markov State
ECMS	Equivalent Consumption Minimization Strategy	μ	Forgetting Coefficient
MPC	Model Predictive Control	D_μ	Markov Chain Effective Memory Depth
DPR	Driving Pattern Recognition	$ \overline{\Delta P_{fc}} $	Root-mean-square of FC Power Transients
GPS	Global Positioning System	SoC_0	Initial Battery SoC
ITS	Intelligent Transportation System	SoC_N	Final Battery SoC
MC	Markov Chain	T_{trip}	Estimated Trip Duration
BPNN	Back Propagation Neural Network	α	Adjusting Factor
TPM	Transition Probability Matrix	r_{soc}/r'_{soc}	Reference/Actual SoC Depletion Rate
PEMS	Predictive Energy Management Strategy	\overline{RMSE}	Average Root Mean Square Error
MPC	Model Predictive Control	v_{ave}	Average of Forecasted Speed Sequence
QP	Quadratic Programming	v_{std}	Standard Deviation of Forecasted Speed Sequence

29 I. Introduction

30 For mitigating the dependency on fossil fuels, plug-in hybrid electric vehicles (PHEV) are widely
31 considered as one of key technologies towards future cleaner mobility [1]. Owing to its zero-emission
32 property, the fuel cell system (FCS) is capable of directly converting chemical energy into deliverable
33 electrical energy, making it the ideal substitution to internal combustion engines (ICE) [2]. In accordance
34 with such trend, fuel cell/battery-based PHEV (abbreviated as FCPHEV) has attracted substantial
35 research attentions in green transport field most recently [3]. However, numerous un-well-solved issues,
36 like the fuel cell durability and the shortage of hydrogen refueling infrastructures, significantly hinder
37 the commercialization of fuel cell vehicles [4]. Therefore, to reduce the operation costs of FCPHEVs, a
38 robust energy management strategy (EMS), which can achieve the reliable energy distribution by
39 regulating the output behaviors of multiple energy sources within the hybrid powertrain, should be
40 further investigated.

41 1.1. Literature review

42 The power splitting strategies for PHEVs can be cataloged into Charge-Depleting/Charge-Sustaining
43 (CD-CS) strategy and blended strategy. The principle of CD-CS strategy is to operate the vehicle as a

44 pure EV until the State-of-Charge (SoC) of power battery reaches a preset lower threshold. Afterwards,
45 the primary energy source switches on to maintain the SoC level [5]. However, the predefined control
46 parameters in CD-CS strategy cannot fully ensure the performance optimality under various driving
47 conditions, especially when the trip length exceeds the all-electric-range of PHEVs. Alternatively,
48 several blended EMSs using dynamic programming (DP) [6], [7], genetic algorithm (GA) [8], [9] and
49 Pontryagin's minimum principle (PMP) [10], [11] can acquire the global optimal performance by
50 minimizing the predefined objective functions. However, these strategies can only be deemed as the
51 offline benchmarks due to the requirement on the complete route information as well as the unavoidable
52 huge computation costs.

53 As a substitute solution, real-time optimization-based strategies become appealing to researchers,
54 including equivalent consumption minimization strategy (ECMS) [12], [13] and model predictive
55 control (MPC) [14]-[19]. As the decision maker within the EMS framework for PHEVs, MPC is capable
56 of anticipating future system behaviors and takes control actions accordingly by optimizing the
57 performance index in a finite time horizon [14]. To be specific, the performance of MPC-based EMS is
58 largely dependent on two essential factors. The first one is battery SoC reference trajectory. In fact, the
59 fuel economy of PHEVs is closely related to the way of battery energy usage during a trip. Therefore,
60 an explicit SoC reference trajectory is indispensable as a guidance for planning battery energy
61 distribution to approximate the global optimality [15]. The second one is the forecasted speed profile
62 over each rolling optimization horizon. In MPC control framework, the upcoming vehicle speed is often
63 regarded as the disturbances and the quality of speed prediction directly affects the MPC performance
64 [16]. However, under realistic driving conditions, the vehicle's velocity could be affected by many
65 uncertainties (e.g. the stochastic distribution of traffic lights and the unexpected pedestrian movement,
66 etc.), and thus is very hard to forecast.

67 Consequently, to provide with accurate reference and predictive information for MPC decision-making,
68 it is meaningful to investigate the battery SoC reference generation methods and the vehicle speed
69 forecasting techniques, which is the major research focus of this paper. In fact, large number of
70 researches has been conducted on these topics [20]-[26]:

71 Generally, the methods for SoC reference generation can be roughly classified into three types. The first
72 type is based on linear SoC reference model. With the estimated trip length [20] (or duration [14]), the
73 reference SoC is designed to linearly decline from the initial (maximum) value to the terminal (minimum)
74 one. Moreover, to improve the rationality in battery energy planning, authors in [15], [16] have added
75 some adaptation laws to the original linear model, making the SoC declining rate change with the
76 realistic driving conditions, thus leading to better EMS performance against the original linear model.
77 The second type of SoC reference planning method takes advantage of the real-time updated route-based
78 information from intelligent transportation system (ITS) or global positioning system (GPS) [21]-[23].
79 For instance, in [21], DP extracts the optimal SoC traces from the real-time traffic flow speed profiles.
80 Afterwards, the obtained SoC references are given to the MPC controller for guiding the energy
81 distribution. In this way, nearly 95% fuel optimality compared to DP benchmark is achieved by the
82 proposed hierarchical EMS. The third type of method benefits from data-driven approaches [18], [24]-
83 [26]. For instance, based on the abundant historical driving database of plug-in hybrid electric buses, a
84 multi-variant regression model is developed to generate the SoC reference trajectories [18], where the
85 fitting coefficients are obtained from the DP-optimized SoC traces. In this way, compared with a rule-
86 based benchmark, the proposed strategy can improve fuel economy by 42.46%.

87 To characterize the upcoming velocity trajectories over each preview horizon, two types of data-driven
88 methodologies are widely employed in previous researches, namely the Markov Chain (MC) models
89 [14], [15], [18] and neural network (NN) models [16], [21], [23]. For example, authors in [15] have built
90 a multi-step MC velocity predictor based on real bus driving database, which outperforms the back
91 propagation NN (BPNN) predictor in terms of the computation efficiency and the overall forecasting
92 precision. Besides, a deep neural network based speed-forecast method is reported in [23], which can
93 respectively enhance the forecast precision by 26.8% and 22.4% compared to the traditional MC and
94 BPNN predictor.

95 **1.2. Motivations and Innovations**

96 Despite large amount of MPC-based EMSs have been devised for PHEVs in previous researches, there
97 still exists plenty room for improvement in following aspects:

98 • In our previous works, an Elman NN predictor [17] and a fuzzy C-means enhanced Markov
99 predictor [19] are built using the offline historical driving database. Nevertheless, their prediction
100 quality would be greatly challenged if the discrepancy between the realistic driving scenarios and
101 the historical ones were significant [27]. To compensate for this defect, the online learning
102 mechanism should be introduced to update the speed predictors and help them adapt to new driving
103 scenarios in a stepwise manner. Through such adaptation law, the precision and reliability of the
104 speed predictors in our previous works can be further enhanced.

105 • The single SoC declining rate of linear SoC reference model [14] may be improper for realistic
106 cycles with changeable driving patterns. To overcome this defect, we propose an adaptive method
107 for SoC reference planning in our previous work [19], but its effectiveness is only verified under
108 urban driving scenario. Besides, the requirement on real-time traffic information and the bulky
109 computational burden greatly hinder the real application of telematics-based approaches [21]. Hence,
110 an integrable solution for SoC reference generation should be further explored, which can
111 effectively guide battery energy depletion in face of the changes in driving patterns.

112 • H₂ consumption saving and FCS lifetime prolongation by avoid harsh transients are two essential
113 EMS objectives in our previous work [17]. However, the SoC reference estimation errors caused by
114 future driving uncertainties would compromise the EMS performance. Hence, how to ensure fuel
115 economy, FCS durability and SoC regulation capacity, while compensating for the EMS
116 performance losses caused by SoC reference estimation errors still needs to be intensively studied.

117 To compensate for these deficiencies, a power allocation strategy considering velocity prediction is
118 developed in this study, which contains the following contributions:

119 • An adaptive online-learning enhanced Markov speed forecasting method is proposed. Two features
120 make the proposed method distinct from the ones in our previous works: (i) without using offline-
121 driving database, the self-learning MC is capable of stepwise renewing its transition probability
122 matrices (TPM) through the real-time obtained driving samples; (ii) with the real-time renewed
123 TPMs, the proposed method can adjust its predictive behaviors towards different driving patterns,
124 thus enhancing the prediction robustness.

- 125 • Only based on the estimated trip duration information, a SoC reference generator is developed,
126 which can be integrated into the EMS and is capable of regulating the SoC declining ratio in multiple
127 driving scenarios with the help of the real-time updated speed forecasting results.
- 128 • Combining the velocity-forecast results and the reference SoC traces, a multi-criterion MPC-based
129 EMS is devised, aiming at enhancing the FCS's operation efficiency and prolonging the FCS's
130 service time, while compensating for the potential EMS performance losses caused by SoC
131 reference estimation errors.

132 **1.3. Article overview**

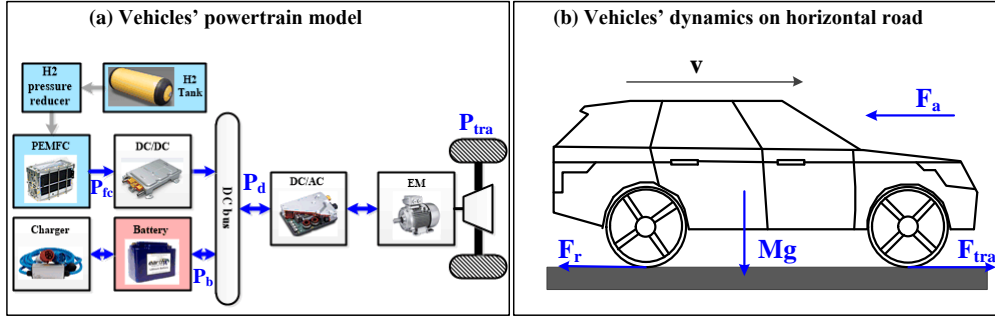
133 The sequel of this article is sketched as below. The studied vehicle model is established in section II.
134 The design of the self-learning MC prediction approach, the SoC reference planning approach and the
135 MPC control strategy are detailed in Section III. The devised strategy is thoroughly validated in section
136 IV. Key findings and future research directions are summarized in section V.

137 **II. Modelling of a middle-sized vehicle**

138 **2.1. Vehicle dynamics and powertrain topology**

139 From the vehicular simulator ADVISOR, a middle-sized car model is picked for control strategy
140 development. As depicted in Fig. 1(a), the PEMFC and battery work cooperatively to response the power
141 demand from the electric machine, where PEMFC is attached to the DC bus through a DC/DC converter
142 and battery is straight attached to the DC bus. Benefiting from an available component-sizing
143 configuration for middle-sized FCPHEVs in [16], the specifications of the studied hybrid powertrain are
144 given in TABLE I. In such powertrain topology, only the FCS output power can be actively controlled
145 [28].

146 In addition, the vehicular power requirement in motion as a function of its weight M and desired speed
147 v can be expressed by (1) [29]. Please note the gravitational acceleration $g = 9.81 \text{ m/s}^2$. Besides, as a
148 horizontal road-vehicle configuration (see Fig. 1(b)) is used for calculating the external power demands,
149 the angle of road inclination θ takes zero. Meanwhile, the net power of PEMFC system (P_{fc}) and battery
150 power (P_b) together response to the equivalent power demand (P_d) on DC bus, as indicated in (2) [30].



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Fig. 1. Schematic diagram of (a) hybrid powertrain structure and (b) forces on a vehicle in motion.

$$153 \quad P_{tra} = v \cdot \left(\underbrace{c_r Mg \cos(\theta)}_{F_r} + \underbrace{\frac{1}{2} \rho_{air} S_f c_d v^2 + M \dot{v}}_{F_a} \right) \quad (1)$$

$$154 \quad P_d = \frac{P_{tra}}{\eta_{tra} \cdot \eta_{DC/AC} \cdot \eta_{EM}} = P_b + P_{fc} \cdot \eta_{DC/DC} \quad (2)$$

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Where c_r represents the rolling resistance coefficient, ρ_{air} the air density, S_f the area of front surface,

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c_d the aerodynamic drag coefficient, η_{tra} the driveline efficiency, $\eta_{DC/AC}$ and $\eta_{DC/DC}$ the power

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converters' efficiencies.

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TABLE I. Vehicular Powertrain Specifications

Component	Description	Value	Unit
Sedan Structural Parameters from ADVISOR	Curb Weight	1360	kg
	Frontal Area	1.746	m^2
	Density of Air	1.21	kg/m^3
	Coefficient of Aerodynamic drag	0.3	N/A
	Coefficient of Rolling Resistance	0.0135	N/A
	Efficiency for driveline	0.91	N/A
PEMFC System	Peaking power	30	kW
	Peaking Efficiency	50.3%	N/A
Lithium-ion battery	Nominal Energy Capacity	12.8	kWh
Traction Motor	Allowable max. Power	75	kW
	Allowable max. Torque	271	$N \cdot m$
	Allowable max. Speed	10000	rpm
Power Converter Efficiency	DC - DC	0.90	N/A
	DC - AC	0.95	N/A

159 2.2. Fuel Cell Model

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As one of widely used fuel cells in automotive industry, the PEMFC is embedded in the studied

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powertrain. Under the specific working conditions (e.g. humidity, partial pressure etc.), the cell voltage

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can be written as a function of the current density [29]. Additionally, given the lower heating value of

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H2 (LHV_{H_2} in MJ / kg), the mass of hydrogen (m_{H_2}) utilized over a trip is derived by [31]:

$$m_{H_2} = \int_0^t \frac{P_{fc}(t)}{\eta_{FCS} \cdot \text{LHV}_{H_2}} dt \quad (3)$$

Note η_{FCS} is the efficiency of fuel cell system. Actually, two major components can be found within a typical PEMFC system, including the fuel cell stack (which transforms the hydrogen energy into the electricity power through chemical reactions) and the auxiliary devices (which guarantee the normal operation of fuel cell stack). Consequently, η_{FCS} can be defined by:

$$\eta_{FCS} = \frac{P_{fc}}{P_{chemical}} = \frac{P_{stack} - P_{AUX}}{P_{chemical}} \quad (4)$$

Where P_{stack} represents the fuel cell stack output electrical power, P_{AUX} the power dissipated in the auxiliaries and $P_{chemical}$ the energy flux contained in reactants [30]. Hence, P_{fc} represents the net power output from PEMFC system. Specifically, Fig. 1(c) depicts the relationship between P_{fc} and η_{FCS} in the studied powertrain. The system peaking efficiency $\eta_{max} = 50.3\%$ is associated with the most efficient fuel cell power point P_{η}^{max} . Besides, $P_{fc} \in [P_{\eta}^{LOW}, P_{\eta}^{HIGH}]$ defines the high efficiency area ($\eta_{FCS} \geq 47.0\%$) of the FCS.

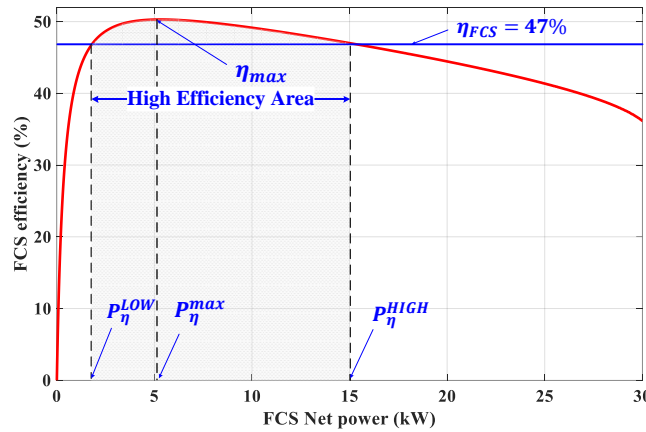


Fig. 1(c). The relationship between FCS net power (P_{fc}) and FCS efficiency (η_{FCS}).

2.3. Battery Model

As shown in Fig. 1(d), the internal-resistance model is adopted in this work to characterize the lithium-ion battery. In addition, let I_b denotes the battery current, R_b the battery resistance, Q_b the nominal

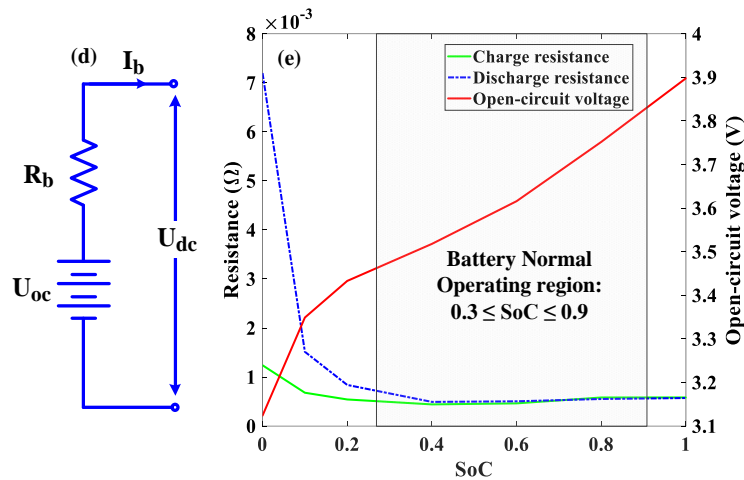
181 capacity, U_{oc} the open-circuit voltage (OCV) and η_b the battery efficiency, the battery state-of-charge
 182 as well as the DC bus voltage U_{dc} are derived by Eq. (5).

$$SoC(t) = SoC_0 - \frac{\int_0^t \eta_b \cdot I_b(t) dt}{Q_b} \quad (a)$$

$$183 \quad I_b = \frac{U_{oc}(SoC) - \sqrt{U_{oc}(SoC)^2 - 4 \cdot R_b(SoC) \cdot P_b}}{2 \cdot R_b(SoC)} \quad (b) \quad (5)$$

$$U_{dc} = U_{oc}(SoC) - I_b \cdot R_b(SoC) \quad (c)$$

184 Where SoC_0 denotes the initial SoC state. It should be mentioned that the values for U_{oc} and R_b of a
 185 battery cell vary with its SoC. To characterize such nonlinear relationship, an experimentally validated
 186 lithium-ion battery model is picked from the database of vehicular simulator ADVISOR [32]. As
 187 illustrated in Fig. 1(e), when $0.3 \leq SoC \leq 0.9$, the OCV of battery cell declines linearly and the variation
 188 of internal resistance is insignificant. Hence, in light of battery working safety and efficiency issues,
 189 restricting SoC in its normal operating region is commonly recommended.

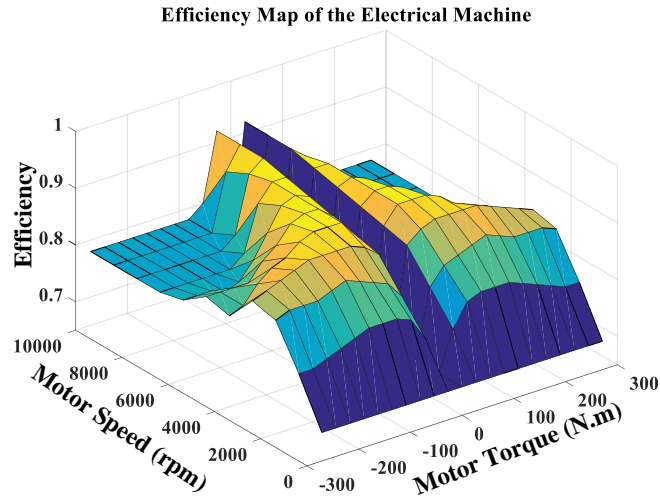


190
 191 Fig. 1. (d) Battery internal-resistance model and (e) battery cell parameters variation with SoC.

192 2.4. Electric Machine Model

193 Electric machine (EM) is the provider of vehicle propulsion power. According to the maximum power
 194 and torque demands required by the driving cycles, a 75-kW AC induction motor is picked as the
 195 computation model in this work. Please note this experimentally validated EM model is selected from
 196 ADVISOR database, whose permissible torque and rotation speed ranges are $T_{motor} \in$
 197 $[-271, 271]$ N·m and $\omega_{motor} \in [0, 10000]$ rpm, respectively. Besides, the EM efficiency

198 η_{motor} changes with the motor working states specified by T_{motor} and ω_{motor} . Consequently, given the
199 desired vehicular speed and torque requests, the motor working efficiency can be looked up through the
200 efficiency map (Fig. 1(f)).



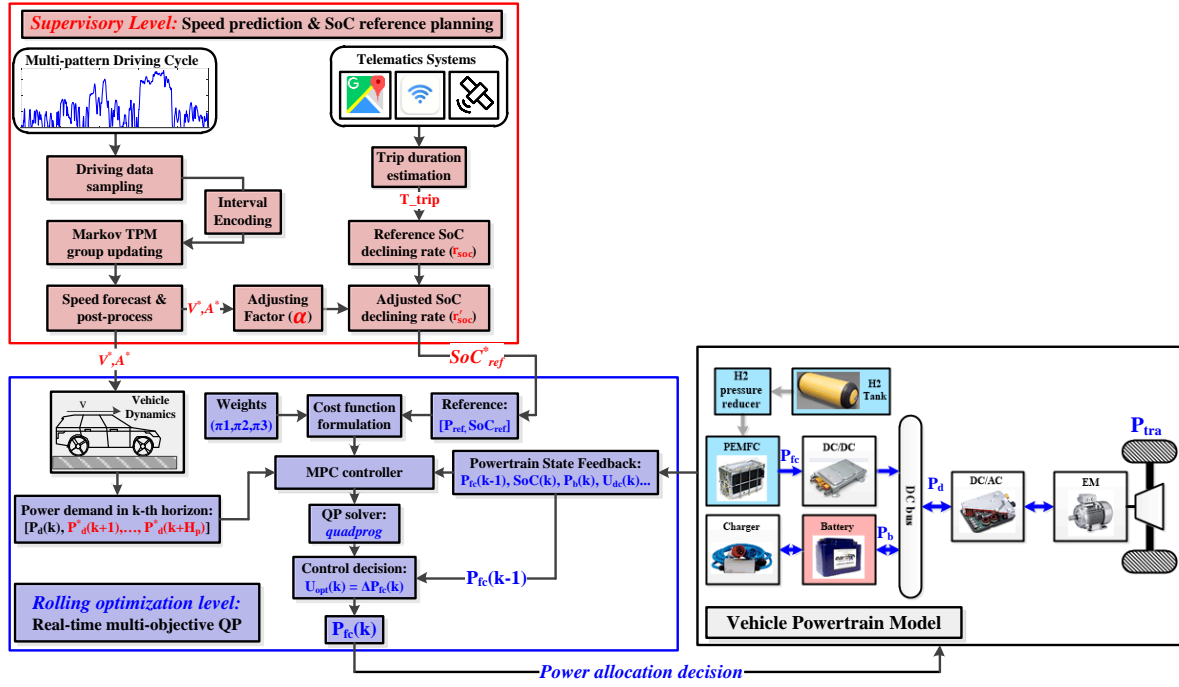
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Fig. 1(f). Motor efficiency as a function of T_{motor} and ω_{motor} .

203 III. Predictive Energy Management Strategy Design

204 Fig. 2 schematically presents the control framework for the devised predictive energy management
205 strategy. In the supervisory level, the self-learning MC predictor can forecast the speed profiles with the
206 real-time updated TPM group. Afterwards, the declining rate of battery SoC is regulated according to
207 the partial trip information and speed forecasting results. In the rolling optimization level, combining
208 the velocity-forecast results, the reference SoC traces and the current vehicle states, MPC derives the
209 optimal control action through minimizing the multi-purpose objective function at each time step. The
210 development of PEMS is thoroughly illustrated afterwards.



211

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Fig. 2. Control framework for the devised predictive energy management strategy.

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3.1. Speed Forecasting Technique

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The quality of velocity prediction would largely affect the MPC decision-making process. To enhance the forecast precision under rapid-changing driving scenarios, the design of an adaptive self-learning enhanced Markov speed predictor is detailed in the remaining part of subsection 3.1.

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3.1.1. Markov Chain and online-learning technique

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The future acceleration distribution is taken as a stochastic process, which is modeled by Markov Chain.

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Under the interval-encoding framework [33], the continuous acceleration domain is discretized by

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numerous disjoint intervals $I_j, j \in \{1, \dots, s\}$, where every interval midpoint is tagged by a single Markov

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state, marked as $a_j \in I_j$. Subsequently, a countable set $X_a = \{a_1, \dots, a_s\}$ containing all feasible

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acceleration states defines the state space of Markov model. For multi-step prediction purpose, a TPM

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group $T_G = \{T_1, \dots, T_{H_p}\}$ should be built. Note the l -th TPM in T_G is an s -order square matrix denoting

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the l -step ($l \in \{1, \dots, H_p\}$, H_p is the prediction horizon) ahead probability distribution. Its element in the

225

i -th row and j -th column, denoted as $[T_l]_{ij}$, indicates the probability of a state transition from a_i to

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$a_j, i, j \in \{1, \dots, s\}$, where the value of $[T_l]_{ij}$ can be derived by Eq. (6).

227 $[T_l]_{ij} = \Pr \{ a(k+l) = a_j | a(k) = a_i \} \approx \text{Num}_{ij}^l / \text{Num}_{oi}^l, l \in \{1, \dots, H_p\}, i, j \in \{1, \dots, s\}. \quad (6)$

228 Please note Num_{ij}^l and Num_{oi}^l are the numbers of Markov state transition, with the superscript l denoting
 229 the time step and the subscript denoting the indices of transition incidents (ij for the transitions from a_i
 230 to a_j , whereas oi for the transitions originating from a_i).

231 To estimate the TPM group through the online measurements, the state transition number **Num** is
 232 substituted to the state transition frequency **Fre**. Consequently, the transition probability estimation
 233 model (6) can be rewritten as [33]:

$$[T_l(L)]_{ij} \approx \frac{\text{Num}_{ij}^l(L)/L}{\text{Num}_{oi}^l(L)/L} = \frac{\text{Fre}_{ij}^l(L)}{\text{Fre}_{oi}^l(L)} \quad (a)$$

234 $\text{Fre}_{ij}^l(L) = \text{Num}_{ij}^l(L)/L = \frac{1}{L} \sum_{t=1}^L \text{flag}_{ij}^l(t) \quad (b) \quad (7)$

$$\text{Fre}_{oi}^l(L) = \text{Num}_{oi}^l(L)/L = \frac{1}{L} \sum_{t=1}^L \text{flag}_{oi}^l(t) \quad (c)$$

235 Where L denotes the observation length. Moreover, **flag** indicates the occurrence of related transition
 236 incidents. For instance, at time step t ($t \in [1, L]$), $\text{flag}_{ij}^l(t) = 1$ or $\text{flag}_{oi}^l(t) = 1$ only when the related state
 237 transition incidents happen, where $\text{flag}_{oi}^l(t) = \sum_{j=1}^s \text{flag}_{ij}^l(t)$. If the related transition incidents do not
 238 happen, they both equal to zero. Moreover, the transition frequency $\text{Fre}_{ij}^l(L)$ and $\text{Fre}_{oi}^l(L)$ can be
 239 expanded in the following recursive form:

$$\begin{aligned} \text{Fre}_{ij}^l(L) &= \frac{1}{L} \sum_{t=1}^L \text{flag}_{ij}^l(t) = \frac{1}{L} \cdot [(L-1)\text{Fre}_{ij}^l(L-1) + \text{flag}_{ij}^l(L)] \\ &= \text{Fre}_{ij}^l(L-1) + \frac{1}{L} \cdot [\text{flag}_{ij}^l(L) - \text{Fre}_{ij}^l(L-1)] \\ &\approx \text{Fre}_{ij}^l(L-1) + \boldsymbol{\mu} \cdot [\text{flag}_{ij}^l(L) - \text{Fre}_{ij}^l(L-1)] \end{aligned} \quad (7d)$$

$$\begin{aligned} \text{Fre}_{oi}^l(L) &= \frac{1}{L} \sum_{t=1}^L \text{flag}_{oi}^l(t) = \frac{1}{L} \cdot [(L-1)\text{Fre}_{oi}^l(L-1) + \text{flag}_{oi}^l(L)] \\ &= \text{Fre}_{oi}^l(L-1) + \frac{1}{L} \cdot [\text{flag}_{oi}^l(L) - \text{Fre}_{oi}^l(L-1)] \\ &\approx \text{Fre}_{oi}^l(L-1) + \boldsymbol{\mu} \cdot [\text{flag}_{oi}^l(L) - \text{Fre}_{oi}^l(L-1)] \end{aligned} \quad (7e)$$

242 Furthermore, the forgetting coefficient μ ($0 < \mu < 1$) is introduced in (7d) and (7e), which is equivalent
 243 to erasing the impact of older measurements through exponentially decreasing their weights. Hence, the
 244 probability $[T_l(L)]_{ij}$ can be renewed online by [34]:

$$245 \quad [T_l(L)]_{ij} \approx \frac{\text{Fre}_{ij}^l(L-1) + \mu \cdot [\text{flag}_{ij}^l(L) - \text{Fre}_{ij}^l(L-1)]}{\text{Fre}_{oi}^l(L-1) + \mu \cdot [\text{flag}_{oi}^l(L) - \text{Fre}_{oi}^l(L-1)]}, i, j \in \{1, \dots, s\}, l \in \{1, \dots, H_p\}. \quad (8)$$

246 Through (8), the MC predictor can converge to the recent driving changes by stepwise updating its
 247 transition probabilities using the incrementally obtained driving information.

248 3.1.2. Speed Forecasting Using Self-Learning Enhanced Markov Chain

249 Benefiting from the online TPM updating technique, a novel speed forecasting method is proposed,
 250 whose three working phases are detailed as below.

251 **(1) Parameter initializing phase.** Before online TPM estimation, the size of Markov state space s , the
 252 forgetting coefficient μ and the preview length H_p are specified. Afterwards, the MC state space X_a and
 253 the initial TPM group $T_{\text{ini}} = \{T_1(0), \dots, T_{H_p}(0)\}$ are built. Note the l -th element in T_{ini} is an s -by- s matrix,
 254 with all elements equaling to $1/s$, and s is set to 40 in this study.

255 **(2) TPM updating phase.** Sample the most recent acceleration states: $a(L) = a_j$ and $a(L-l) = a_i$, where
 256 $a_j, a_i \in X_a$. Calculate $\text{flag}_{ij}^l(L)$ and $\text{flag}_{oi}^l(L)$ based on the state transition incidents from a_i to
 257 $a_j, l=1, \dots, H_p$. Then, the L -th transition frequency $\text{Fre}_{ij}^l(L)$, $\text{Fre}_{oi}^l(L)$ can be computed using the
 258 $(L-1)$ -th transition frequency $\text{Fre}_{ij}^l(L-1)$, $\text{Fre}_{oi}^l(L-1)$ as indicated by (7d) and (7e). Afterwards, each
 259 element within the i_l -th row of the l -step TPM $T_l(L)$ is renewed by (8), thus leading to the evolution of
 260 $T_G(L) = \{T_1(L), \dots, T_{H_p}(L)\}$. Specially, if there is not enough historical driving data for TPM estimation
 261 ($L \leq H_p$), initial TPM group T_{ini} is adopted for velocity prediction.

262 **(3) Prediction and post-processing phase.** Given the updated TPM group $T_G(L)$ and the
 263 L^{th} acceleration state $a(L) = a_j$, the acceleration in next l steps is obtained by the probability-weighted

264 average (expected value) of every interval middle point: $a^*(L+1) = \sum_{j=1}^S [T_j(L)]_{ij} \cdot a_j$, if $a(L) \in I_i$.

265 Therefore, the l -step ahead velocity can be predicted by: $v^*(L+1) = v(L) + \sum_{q=1}^{l-1} a^*(L+q) \cdot \Delta T$. Finally,

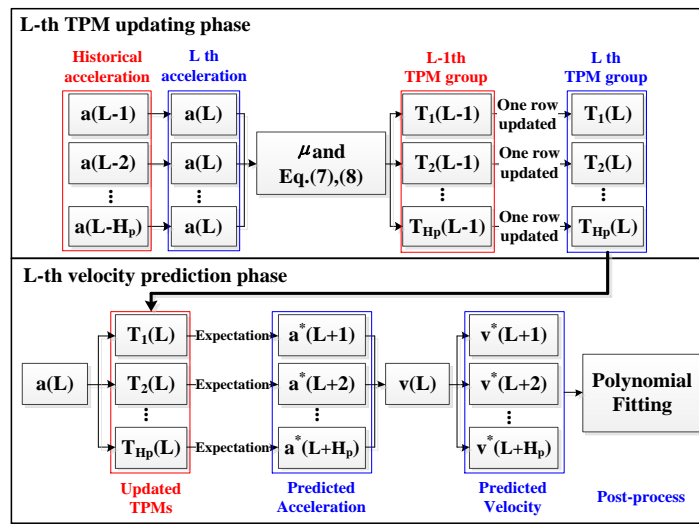
266 to guarantee the smoothness of the forecasted speed profiles, the polynomial fitting algorithm is adopted

267 for post-processing the velocity-forecast profiles. The sampling period $\Delta T = 1s$.

268 To sum up, without using offline driving database, the enhanced Markov predictor is established and

269 updated online based on the real-time measured driving data, where its working principle at L -th time

270 step is depicted in Fig. 3.



271

272

Fig. 3. Working flow within L^{th} updating and prediction phase.

273 **3.2. Battery SoC reference planning approach**

274 The plug-in property permits the vehicular battery to be recharged through the external grid power,

275 which, hence, enables a way towards better fuel economy by consuming the low-cost electricity energy.

276 Specifically, to realize the efficient utilization of battery energy under sophisticated traffic conditions,

277 an explicit SoC reference trajectory is necessary for the MPC controller to track. Through narrowing the

278 discrepancy between the real SoC and the reference one, the battery output behaviors can be properly

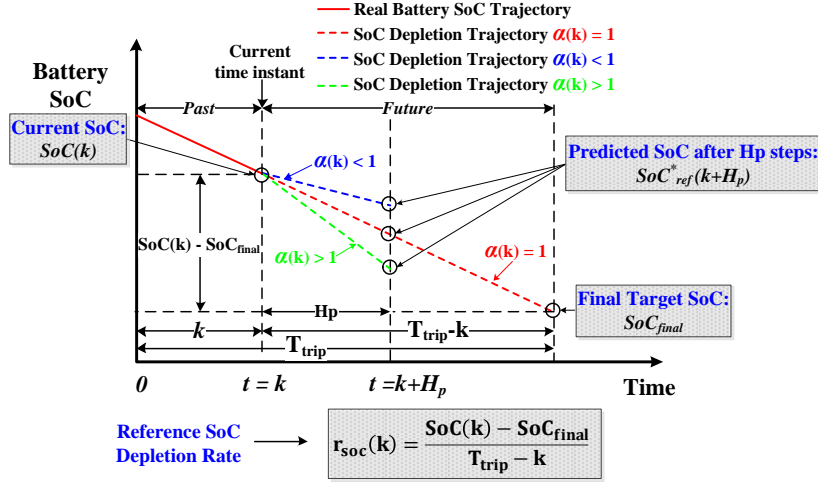
279 regulated for adapting to different power requests.

280 Actually, depleting battery energy at various rates under multiple driving patterns may enhance the EMS

281 control performance. Specifically, high-average power requests occur under highway driving conditions.

282 In this case, the low-cost battery energy should be primarily utilized to save the hydrogen consumption,

283 which leads to a high declining rate of SoC. In contrast, the low-average power requests in urban regions
 284 imply a relatively low SoC declining rate. Therefore, an adaptive SoC reference planning approach is
 285 designed for adjusting the battery SoC declining rates under multiple driving patterns, where Fig. 4
 286 details the regulation mechanism of the proposed method.



287

288

Fig. 4. Schematic diagram of the adaptive SoC reference generator.

289 The maturation of modern telematics techniques makes it possible to acquire the estimated trip duration
 290 information T_{trip} in advance. At $t = k$, let $SoC(k)$ denotes the actual SoC, SoC_{final} the terminal SoC
 291 target and $V_k^* = [v^*(k+1), \dots, v^*(k+H_p)]$ the forecasted speed profile, the predicted reference SoC at $t = k$
 292 $+ H_p$ is expressed by:

$$293 \quad SoC_{ref}^*(k + H_p) = SoC(k) - \underbrace{\left(\frac{k_\alpha}{1 + \frac{v_{std}(k)}{v_{ave}(k)}}} \right)}_{\alpha(k)} \cdot \underbrace{\left(\frac{SoC(k) - SoC_{final}}{T_{trip} - k} \right)}_{r_{soc}(k)} \cdot H_p \quad (9)$$

294 Where r_{soc} represents the k-th reference SoC declining rate concerning the remaining time of trip.
 295 Moreover, $\alpha \in (0, k_\alpha]$ is the adjustment coefficient, where the constant parameter $k_\alpha > 0$ specifies the
 296 upper boundary of α . Besides, r'_{soc} represents the modified SoC declining rate. Specifically, reducing
 297 k_α would slow down the overall SoC declining rate and thus may fail to entirely exploit the battery
 298 energy, whereas an exceeding large k_α would extremely accelerate the battery energy depletion, thus

299 prolonging the vehicle's CS working period. Hence, a trade-off on the EMS performance against the
300 battery energy utilization ratio should be made by using an appropriate k_α .

301 Additionally, $v_{std}(k)$ and $v_{ave}(k)$ represent the standard deviation and mean value of the predicted
302 velocity V_k^* , respectively. Note the forecasted speed trace V_k^* with higher v_{ave} and lower v_{std} implies
303 the highway scenario, leading to a larger α . In contrast, a speed profile with lower v_{ave} and higher
304 v_{std} indicates the urban scenario, meaning a smaller α . Consequently, through the obtained α in
305 different driving scenarios, the actual SoC declining rate r'_{soc} is tuned by the following mechanism.
306 If $\alpha > 1$, r'_{soc} is larger than the reference declining rate (r_{soc}). If $\alpha < 1$, r'_{soc} is smaller than r_{soc} . Besides,
307 $\alpha = 0$ if and only if $v_{ave} = 0$.

308 Furthermore, a linear SoC reference model (10) from literature [14] is introduced for comparison.

$$309 \quad SoC_{ref}^*(k) = SoC_{ini} - \frac{k}{T_{trip}}(SoC_{ini} - SoC_{final}) \quad (10)$$

310 where SoC_{ini} is the initial battery charge state. To ensure the battery operation safety, SoC_{ref}^* is bounded
311 within $[SoC_{min}, SoC_{max}]$, where $SoC_{min} = 0.3$ and $SoC_{max} = 0.9$. It should be mentioned that such range
312 only specifies the boundary of SoC reference. When the actual SoC is beyond $[0.3, 0.9]$, the “SoC
313 emergency” working mode is triggered for urging SoC return to this range.

314 **3.3. Power Allocation Strategy using Model Predictive Control**

315 As the decision-maker with the PEMS framework, MPC acquires the optimal control sequences through
316 minimizing the objective function at each time step. In this subsection, the MPC design process is
317 presented in detail.

318 **3.3.1. Control-Oriented Model**

319 Let the symbol $\mathbf{x} \in R^{2 \times 1}$ denotes state variable, $\mathbf{u} \in R^{1 \times 1}$ the control input, $\mathbf{y} \in R^{1 \times 1}$ the system output,
320 $\mathbf{w} \in R^{1 \times 1}$ the disturbance and $\mathbf{r} \in R^{2 \times 1}$ the reference trajectory, the control-oriented model is formulated
321 as a linear discrete-time system (with 1s sampling period) as denoted by (11), where the MPC control
322 horizon is identical to its prediction horizon (H_p).

$$\mathbf{x}(k+1) = \mathbf{A}(k)\mathbf{x}(k) + \mathbf{B}(k)\mathbf{u}(k) + \mathbf{C}(k)\mathbf{w}(k)$$

$$323 \quad \mathbf{y}(k) = \mathbf{D}\mathbf{x}(k) + \mathbf{E}\mathbf{u}(k) + \mathbf{G}\mathbf{w}(k)$$

$$with \begin{cases} \mathbf{x}(k) = [\text{SoC}(k), P_{fc}(k-1)]^T \\ \mathbf{u}(k) = \Delta P_{fc}(k) = \frac{P_{fc}(k) - P_{fc}(k-1)}{\Delta T} \\ \mathbf{y}(k) = P_b(k) \\ \mathbf{w}(k) = P_d(k) \\ \mathbf{r}(k) = [\text{SoC}_{ref}, P_{ref}]^T \end{cases} \quad (11)$$

324 Combined (11) with the DC power balance relationship (12a) and the first-order differential

325 approximation of SoC dynamics (12b), the system matrices $\mathbf{A}, \mathbf{B}, \mathbf{C}, \mathbf{D}, \mathbf{E}, \mathbf{G}$ are specified as (13).

$$326 \quad \begin{cases} P_d(k) = P_b(k) + \eta_{DC/DC} \cdot P_{fc}(k) & (a) \\ \frac{\text{SoC}(k+1) - \text{SoC}(k)}{\Delta T} = -\frac{\eta_b}{U_{dc}(k) \cdot Q_b} P_b(k) & (b) \end{cases} \quad (12)$$

$$327 \quad \mathbf{A}(k) = \begin{bmatrix} 1 & \frac{\Delta T \cdot \eta_{DC/DC} \cdot \eta_b}{U_{dc}(k) \cdot Q_b} \\ 0 & 1 \end{bmatrix} \quad \mathbf{B}(k) = \begin{bmatrix} \frac{\Delta T \cdot \eta_{DC/DC} \cdot \eta_b}{U_{dc}(k) \cdot Q_b} & 1 \end{bmatrix}^T \quad \mathbf{C}(k) = \begin{bmatrix} -\frac{\Delta T \cdot \eta_{DC/DC} \cdot \eta_b}{U_{dc}(k) \cdot Q_b} & 0 \end{bmatrix}^T \quad (13)$$

$$\mathbf{D} = [0 \quad -\eta_{DC/DC}] \quad \mathbf{E} = [-\eta_{DC/DC} \cdot \Delta T] \quad \mathbf{G} = [1]$$

328 3.3.2. Multi-criteria performance index formulation

329 Three metrics are taken into account of the MPC performance index, namely (i) FCS working efficiency,

330 (ii) FCS durability and (iii) SoC reference tracking ability. Consequently, the k -th control decision

331 $\mathbf{U}^*(k) = [u_1^*(k), \dots, u_{H_p}^*(k)]$ is obtained by minimizing the multi-criteria cost function (14) subject to

332 constraints (15).

$$333 \quad \text{Obj}(k) = \sum_{i=1}^{H_p} \left[\pi_1 \cdot \underbrace{\left(\frac{P_{fc}(k+i-1) - P_{ref}}{P_{fc}^{max}} \right)^2}_{L_1} + \pi_2 \cdot \underbrace{\left(\frac{\Delta P_{fc}(k+i-1)}{\Delta P_{fc}^{max}} \right)^2}_{L_2} \right] + \pi_3 \cdot \underbrace{\left(\frac{\text{SoC}(k+H_p) - \text{SoC}_{ref}}{\text{SoC}_{max} - \text{SoC}_{min}} \right)^2}_{L_3} \quad (14)$$

$$334 \quad \begin{cases} \text{SoC}^L \leq [\mathbf{x}]_1 \leq \text{SoC}^H & (a) \\ P_{fc}^L \leq [\mathbf{x}]_2 \leq P_{fc}^H & (b) \\ \Delta P_{fc}^L \leq \mathbf{u} \leq \Delta P_{fc}^H & (c) \\ P_b^L \leq \mathbf{y} \leq P_b^H & (d) \\ \mathbf{w}(k+i) = P_d^*(k+i), i \geq 1 & (e) \end{cases} \quad (15)$$

335 Where $P_{fc}^{max} = 30kW$, $\Delta P_{fc}^{max} = 1kW/s$, $SoC_{min} = 0.3$ and $SoC_{max} = 0.9$. Moreover, to achieve a
 336 balanced EMS performance among three cost terms (L_1, L_2, L_3), the penalty coefficients (π_1, π_2, π_3) are
 337 tuned by trials and errors, based on the DP-optimized EMS performance. More details regarding the
 338 parameter tuning process can be found in [17]. As a result, π_1, π_2, π_3 are set as 1, 8 and 80000,
 339 respectively. Besides, the major objectives of L_1, L_2, L_3 are attached as below:

- 340 • To guarantee the overall fuel cell operation efficiency, L_1 penalizes the FCS operating points
 341 deviating from the predefined reference one (the most efficient point), namely $P_{ref} = P_{\eta}^{max}$.
- 342 • As indicated in [35], restricting fuel cell power varying rate is beneficial to improving the FCSs'
 343 durability. Consequently, L_2 lays a penalty on large ΔP_{fc} to retard the fuel cell degradation imposed
 344 by dynamic loading conditions.
- 345 • The function of L_3 is to shrink the deviation between the real SoC and the reference one given by
 346 (9), namely $SoC_{ref} = SoC_{ref}^*(k + H_p)$. By tracking the terminal reference value in each prediction
 347 horizon and ignoring the intermediate processes, MPC could better restrain the fuel cell power
 348 transients introduced by improper SoC reference values.

349 Furthermore, constraint (15a) defines a wider SoC variation range for real-time optimization, where
 350 $SoC^L = 0.25$ and $SoC^H = 0.95$. However, if SoC emergency incident ($SoC > 0.9$ or $SoC < 0.3$) appears,
 351 π_1 and π_2 are set to zero to urge SoC back to [0.3, 0.9]. Constraints (15b) - (15d) denote the physical
 352 limitations on fuel cell and battery, where $P_{fc}^L = 0W$, $P_{fc}^H = 30kW$, $\Delta P_{fc}^H = -\Delta P_{fc}^L = 1kW/s$, $P_b^L = -25kW$
 353 and $P_b^H = 50kW$. Besides, (15e) sets the estimated DC power demands as the disturbance, where P_d^* is
 354 calculated according to the forecasted speed V_k^* and Eq. (1)-(2). Finally, the original optimization
 355 problem, namely minimizing (14) while respecting constraints (15), could be converted into a quadratic
 356 programming (QP) problem and resolved by the well-established interior-point algorithm through
 357 calling the MATLAB-embedded *quadprog* function [17].

358 **IV. Simulation and Discussion**

359 A simulation study is conducted in section IV to validate the performance of the presented EMS. All the
 360 simulations are performed in the MATLAB/Simulink environment (version: R2016a), which is installed

361 in a desktop PC with an Intel Core i7-7700 CPU @ 3.30 GHz and a 64G RAM. The discrete sampling
362 time step is set to 1 second.

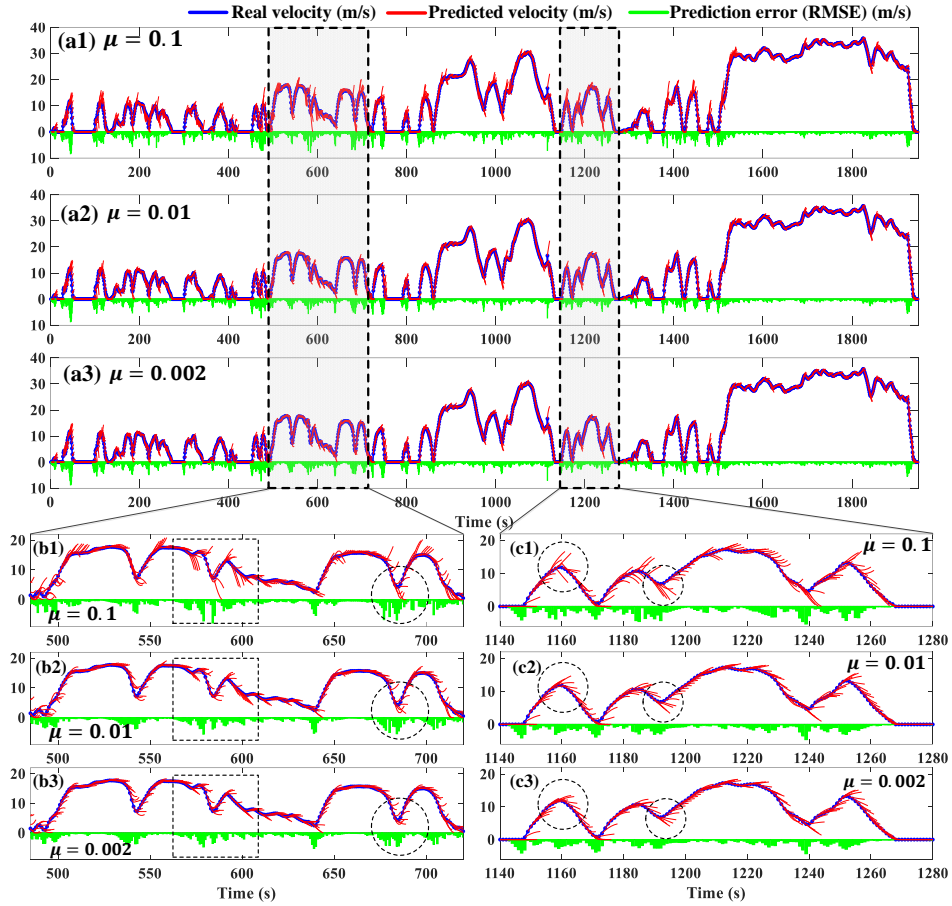
363 **4.1. Speed Forecast Performance Verification**

364 In subsection 4.1, the performance of self-learning Markov speed-forecast method is validated. The
365 Root-Mean-Square-Error (RMSE) is picked as the evaluation metric of forecast accuracy [36].

366 **4.1.1. Influences on forgetting coefficient μ**

367 A small μ would reduce the updating rate of MC predictive model, while a large μ would shorten the
368 effective memory length $D_\mu = 1/\mu$, reducing the completeness and reliability of the MC model. To
369 explore the impacts on prediction performance by different μ , the self-learning MC predictor with
370 multiple forgetting coefficient candidates is evaluated under the INRETS driving cycle [32], where the
371 prediction performance is shown in Fig. 5.

372 Fig. 5(b) and (c) thoroughly demonstrate the forecast results when $H_p = 5s$, where the average RMSE
373 under different μ are respectively 1.1946 m/s ($\mu = 0.1$), 0.9766 m/s ($\mu = 0.01$) and 0.9594 m/s ($\mu =$
374 0.002). Specifically, when $\mu = 0.1$, the forecasted speed profiles tend to diverge significantly from the
375 actual one. When μ reduces from 0.1 to 0.002, the prediction performance improves greatly, especially
376 in the circled regions, since the corresponding enlarged D_μ (from 10 to 500) enables adequate
377 measurements for TPM estimation, thus improving the forecast precision. However, if μ continues to
378 decrease, the forecast precision would decrease to some extent, as shown in TABLE II. This is because
379 the enlarged D_μ (from 500 to 10000) would include superfluous information that cannot represent recent
380 driving conditions, thus reducing the forecast reliability. Meanwhile, when $H_p = 10s$, similar tendency
381 would also be detected. Hence, as a compromise between the prediction performance and the online
382 memory burden, μ is set as 0.002 ($D_\mu = 500$) to handle the changeable driving conditions.



383
 384 Fig. 5. Prediction performance ($H_p = 5s$) with different μ . (a) Velocity prediction results (global perspective). (b) Detail
 385 prediction results from 500s to 720s. (c) Detail prediction results from 1140s to 1280s.

386 TABLE II. Average RMSE (m/s) with respect to different $D_\mu = 1/\mu$ under INRETS cycle

D_μ	5	10	50	100	200	500	1000	2000	5000	10000
$H_p = 5s$	1.1946	1.1336	1.0102	0.9766	0.9624	0.9594	0.9713	0.9782	0.9828	0.9844
$H_p = 10s$	2.5048	2.3823	2.1211	2.0513	2.0275	2.0198	2.0433	2.0550	2.0643	2.0661

387 4.1.2. Prediction Performance Comparison with Benchmark Predictors

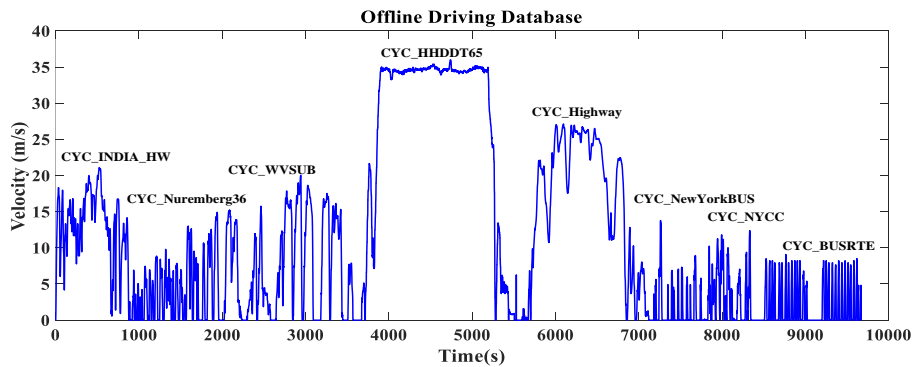
388 To compare the proposed method with benchmark approaches, two commonly used velocity-forecast
 389 methods, namely a multi-step MC (MSMC) and a BPNN predictor, are introduced as evaluation basis.

390 • Benchmark Predictors Description

391 Unlike the self-learning MC, the TPMs of MSMC predictor are estimated by (6) using offline stationary
 392 driving database. Additionally, as suggested in [36], a three-layer BPNN with 10 input neurons and 20
 393 hidden neurons is adopted for speed forecasting.

394 • Database Preparation

395 The performances of benchmark predictors are highly dependent on the offline driving database. To
 396 cover vehicle's daily driving scenarios, several standard cycles with different driving patterns
 397 (urban/suburban/highway) are concatenated to form the offline driving database, as shown in Fig. 6(a).
 398 All standard cycles are extracted from ADVISOR. Note this database is used for the estimation of MC
 399 TPM and the training of BPNN, where 85% of data is for BPNN training while the remaining portion is
 400 for NN validation.



401

402 Fig. 6(a). Offline driving database for NN training and TPM estimation.

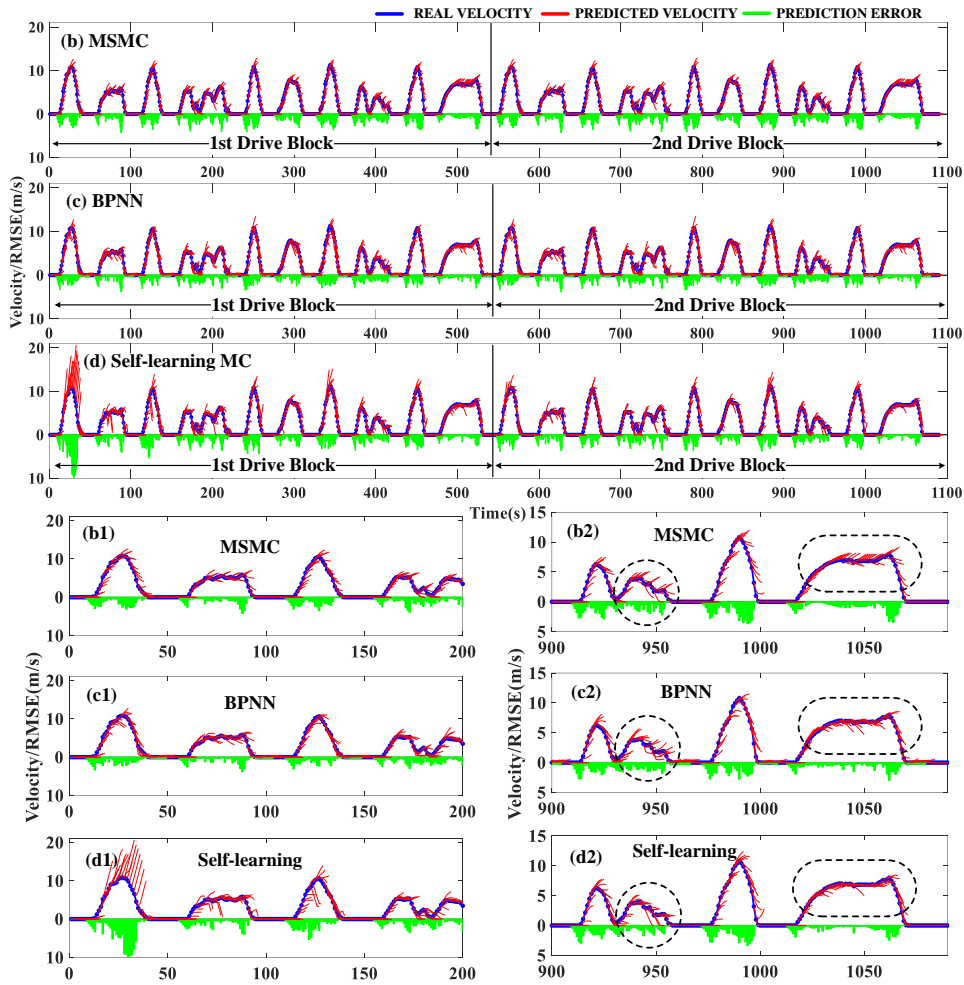
402

403 • **Performance Comparison Under Repetitive Driving Conditions**

404 Firstly, the performance of three predictors is compared under the Manhattan driving cycle, which
 405 represents the typical urban driving scenarios with very low average speed, frequent start-and-stops, and
 406 repetitive driving patterns.

407 Taken $H_p = 5s$ as an example, the prediction performance discrepancy is presented in Fig. 6(b)-(d).
 408 Specifically, both MSMC and BPNN predictor perform stably over the whole cycle. In comparison, due
 409 to the use of initial TPM groups, the online-learning Markov predictor results in the largest error in the
 410 first 200 seconds (Fig. 6(b1), (c1) and (d1)). As the updating of TPM group, its forecast errors gradually
 411 decrease to a lower level. Especially, as shown in the circled regions in Fig. 6(b2), (c2) and (d2), it
 412 performs even slightly better compared to benchmark predictors.

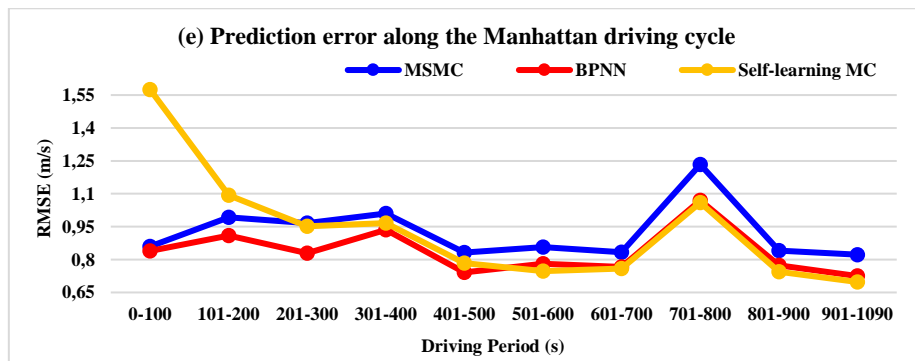
413 Moreover, Fig. 6(e) exhibits the error evolution processes (per 100s) of three predictors. Within the first
 414 200s, the self-learning MC predictor leads to the significantly larger error compared to other predictors.
 415 Afterwards, due to the online TPM updating, its performance discrepancy against other predictors is
 416 shrinking. Specifically, it outperforms the MSMC predictor after 200s. After 500s, it even slightly
 417 outperforms the BPNN predictor until the trip end.



418

419

Fig. 6(b)-(d). Detail speed forecasting performance under Manhattan driving cycle ($H_p = 5s$).



420

421

Fig. 6(e). Average RMSE comparison (per 100s) under Manhattan Driving Cycle.

422

423

424

425

Besides, the average RMSE along the trip is summarized in TABLE III. Unlike benchmark predictors, under two identical drive blocks, the average RMSE for the proposed method is reduced by 20.4% (from 1.0247 m/s to 0.8156 m/s). This indicates the proposed method can acquire predictive knowledge from the incrementally measured driving data and thus its dependency on offline driving database is reduced

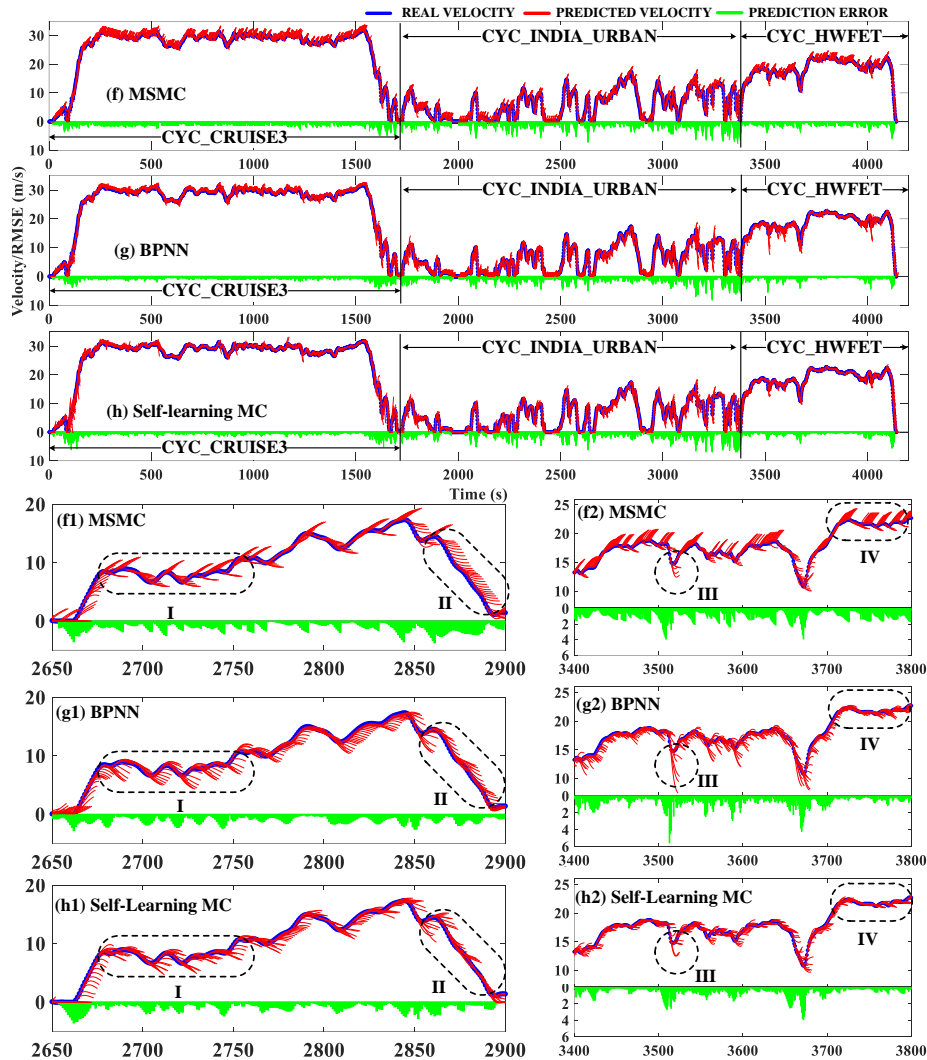
426 compared to benchmark predictors. Moreover, the effectiveness in enhancing the forecast precision by
 427 the online-learning technique is also verified.

428 TABLE III. Average RMSE (m/s) under Manhattan driving cycle.

	1st Drive Block	2nd Drive Block	Total
MSMC	0.9124	0.9208	0.9166
BPNN	0.8279	0.8279	0.8279
Self-learning MC	1.0247	0.8156	0.9206

429 • **Performance Comparison Under Complex Driving Conditions**

430 To further evaluate the prediction performance under complex driving conditions, three standard cycles
 431 [32] are concatenated to form a multi-pattern testing cycle, as shown in Fig. 6(f)-(h). Note H_p is set as
 432 10s to clearly show their performance discrepancies.

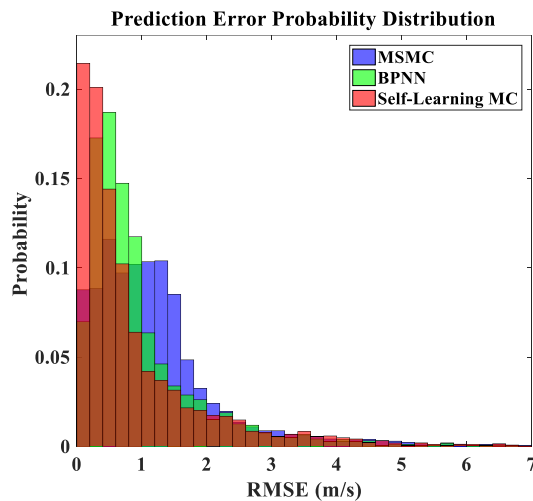


433

434 Fig. 6(f)-(h). Detail speed forecasting performance under multi-pattern driving cycle ($H_p = 10s$).

435 As can be seen, three predictors tend to generate smaller errors over the CRUISE3 and HWFET cycles,
436 whereas larger errors appear over the INDIA_URBAN cycle. This is because the actual speed profile
437 changes more sharply under city driving conditions, making higher forecast accuracy hard to achieve.
438 Moreover, as depicted in the circled region I in Fig. 6(f1)-(h1), the forecasted speed profiles by MSMC
439 predictor tend to remain the same tendency (rising or falling) as the input driving states, while other
440 predictors can more precisely describe the future velocity dynamics. In comparison with BPNN
441 benchmark, the online-learning Markov predictor can more promptly re-converge to the real speed trace
442 after each inflection point, thus increasing the prediction accuracy during this period. Similarly, as
443 shown in the zoomed regions II to IV, the proposed method shows the higher forecast accuracy and
444 robustness compared to benchmark predictors.

445 The reason for such performance discrepancies is given as follows. Benchmark predictors learn future
446 velocity dynamics from the offline stationary database and thus their predictive behavior toward each
447 driving pattern is pre-determined. Nevertheless, owing to the absence of online-update mechanism, it is
448 hard for them to fully adapt to the novel driving characteristics, thus compromising the forecast
449 performance. In contrast, the proposed method can adjust its predictive behaviors by using the real-time
450 updated TPMs, thus leading to the improved performance.



451

452 Fig. 6(i). Average RMSE probability distribution under multi-pattern testing cycle ($H_p = 10s$).

453 In addition, as displayed in Fig. 6(i), the proposed method tends to generate smaller errors among three
454 approaches. Moreover, as summarized in TABLE IV, the proposed method can bring down the average
455 RMSE by 25.73% (MSMC) and 7.90% (BPNN) under the multi-pattern testing cycle. Therefore, it can

456 be confirmed that the proposed method can effectively characterize the future speed dynamics under
 457 changeable driving conditions with the reasonable forecast precision.

458 TABLE IV. Average RMSE (m/s) under combined driving cycle.

	CYCLE_Cruise3	CYCLE_INDIA_URBAN	CYCLE_HWFET	Total
MSMC	1.0365	1.4422	1.0540	1.2032
BPNN	0.7577	1.3204	0.6839	0.9703
Self-learning MC	0.6434	1.2662	0.6387	0.8936

459 4.2. Performance Verification of Energy Management Strategy

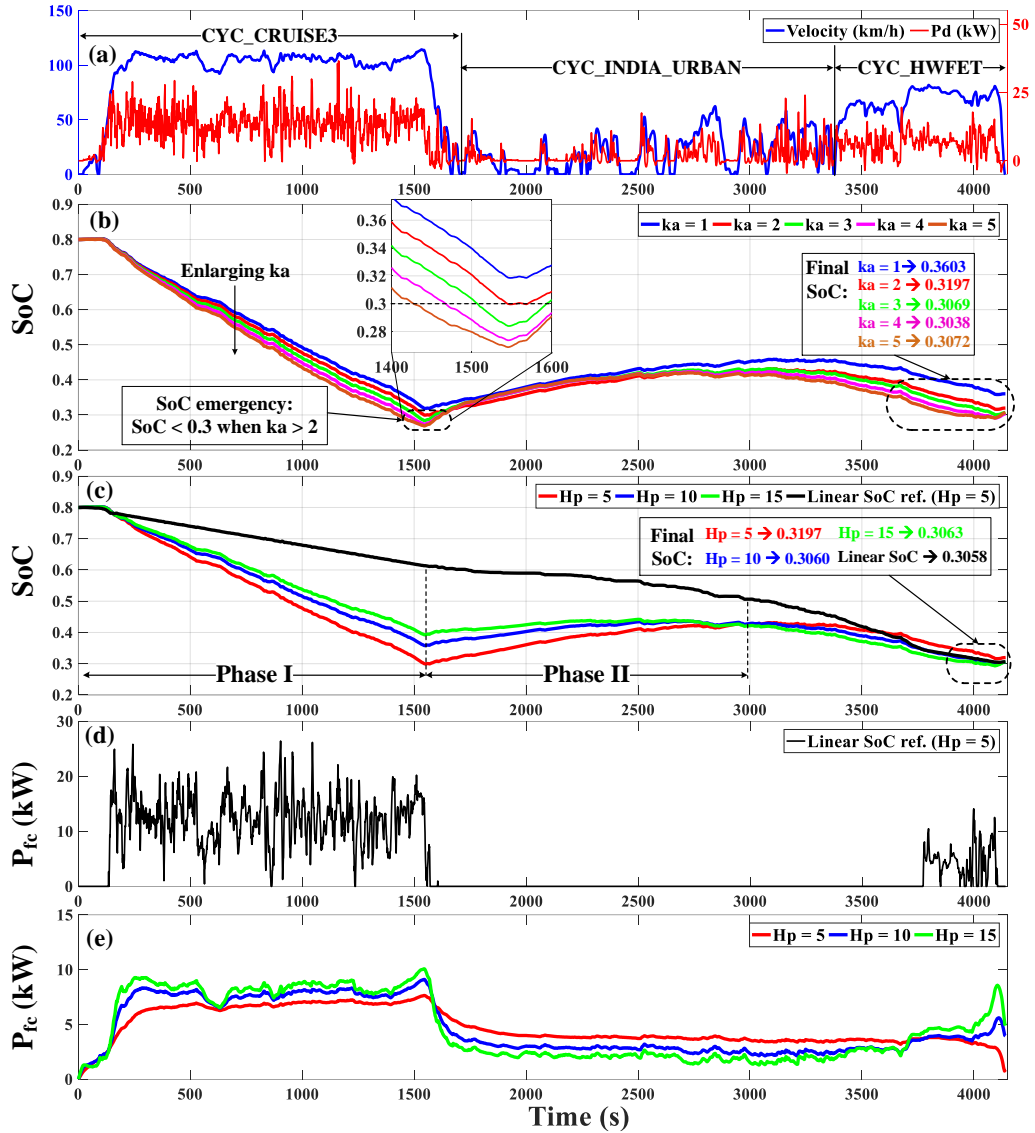
460 The proposed predictive energy management strategy will be comprehensively evaluated in this
 461 subsection. In all case studies, the initial and terminal SoC values are set as 0.8 and 0.3, respectively.

462 4.2.1. Impacts on EMS performance by k_α , H_p and different SoC reference generators

463 Several parameters of the proposed PEMS would heavily affect its performance, which should be
 464 carefully tuned before online implementations. This subsection presents a detailed analysis regarding
 465 the determination criteria of EMS parameters and the battery energy allocation performance comparison
 466 with linear SoC reference (10). Please note that the same multi-pattern driving cycle in Fig. 6(f) is used
 467 as the testing cycle, whose speed and power demand profiles are depicted in Fig. 7(a).

- 468 • **Determination of SoC reference adjusting factor boundary k_α**

469 As mentioned before, k_α controls the upper boundary of the adjusting factor α . To find a proper k_α for
 470 online application, the MPC-based EMS with multiple k_α candidates (1 to 5) is tested under the multi-
 471 pattern driving cycle, where H_p is set as 5 seconds. Fig. 7(b) displays the obtained SoC traces.
 472 Apparently, if $k_\alpha = 1$, larger final SoC value is detected compared to other k_α settings, meaning the
 473 overall SoC declining rate is not enough to ensure the full utilization of battery energy. In contrast,
 474 although using larger k_α can ensure a deeper battery discharge, if $k_\alpha > 2$, the overlarge SoC declining
 475 rates would contribute to the SoC emergency events ($SoC < 0.3$, as shown in the zoomed area). Hence,
 476 set k_α as two is a trade-off decision between the battery working safety and the exploitation rate of
 477 battery energy.



478 Fig. 7. EMS performance comparison under different parameter settings. (a) Velocity and power request profile of the multi-
 479 pattern driving cycle. (b) SoC profiles under multiple k_α ($H_p = 5s$). (c) SoC regulation performance comparison by different
 480 reference generators and different H_p ($k_\alpha = 2$). (d) Fuel cell power profile using linear SoC reference ($H_p = 5s$). (e) Fuel cell
 481 power profiles using the proposed SoC reference and different H_p .
 482

483 • **EMS performance discrepancy using different SoC reference generators**

484 Given $k_\alpha = 2$, the performances of MPC-based EMS with different SoC references are compared in Fig.
 485 7(c) to Fig. 7(e). For the linear SoC reference based EMS, Fig. 7(c) and (d) only depict its performance
 486 when $H_p = 5s$, while the performance under other H_p settings is given in TABLE V.

487 Fig. 7(c) depicts the SoC regulation performance by two types of reference generators. The linear
 488 reference model (10) (black curve) tends to evenly distribute battery energy over the entire trip. Due to
 489 the extremely low external power demand in phase II, despite the fuel cell has been turned off in this

490 phase (Fig. 7(d)), the SoC declining rate is still slightly lower than that in phase I. In contrast, the
491 adaptive SoC reference generator ($H_p = 5s$, red curve) can effectively adjust battery energy usage
492 under different driving patterns. Specifically, the battery energy is largely used due to the high average
493 power demand in highway scenario (phase I), whereas the battery tends to be recharged or less used in
494 urban scenario (phase II).

495 Guided by the linear SoC reference (10), the EMS adjusts the fuel cell output power in an aggressive
496 way, as displayed in Fig. 7(d). Large power transients and frequent start-and-stop cycles can be observed
497 over the testing cycle, especially from 200s to 1500s and from 3700s to 4150s. Such working conditions
498 would accelerate the degradation of fuel cell system, leading to the compromised fuel cell durability. In
499 contrast, as shown in Fig. 7(e), guided by the proposed SoC reference model (9), fuel cell works stably
500 around the reference point, with few power transients. Besides, no FC on-off cycles can be observed
501 within the entire testing cycle.

502 Moreover, TABLE V summarizes the EMS performance discrepancies under different SoC reference
503 models, where m_{H_2} denotes the actual H2 mass consumption, $m_{H_2, equ}$ the equivalent H2 consumption
504 that converts the terminal SoC (SoC_{end}) deviation from 0.3 into corresponding H2 consumption [31],

505 $|\overline{\Delta P_{FC}}|$ the average fuel cell power changing rate and T_{step} the online calculation time per step. It can be
506 clearly seen that, after using the proposed SoC reference model (9), $m_{H_2, equ}$ and $|\overline{\Delta P_{FC}}|$ are greatly
507 reduced compared to those of linear SoC reference based EMS. Besides, both SoC reference based
508 EMSs perform similarly in terms of final SoC and online computation efficiency.

509 To sum up, the proposed SoC reference model (9) is capable of depleting battery energy in a flexible
510 manner regarding different power requirements, thus enhancing the rationality of battery energy
511 allocation in contrast to linear reference model (10). Furthermore, benefiting from such proper battery
512 energy distribution, the EMS can greatly suppress the fuel cell power spikes and effectively improve the
513 fuel cell working efficiency.

514 • **Determination of prediction horizon H_p**

515 H_p defines the length of speed prediction and the size of real-time optimization problem, which would
516 have large impacts on both online computation efficiency and EMS performance. With different H_p
517 settings, the fuel cell power and SoC profiles of the adaptive SoC reference based EMS are illustrated
518 in Fig. 7(c) and (e), respectively, where the related quantitative results are listed in TABLE V. It is clear
519 that increasing H_p would enlarge $m_{H_2, equ}$ but guarantee a deeper battery discharge. Moreover, $|\overline{\Delta P_{FC}}|$
520 and T_{step} increase with the growth of H_p . Therefore, set H_p as five is a trade-off decision among the
521 following metrics, namely the H2 consumption conservation, the fuel cell power transients and the
522 online calculation burden.

523 TABLE V. EMS Performance discrepancies under different H_p and different types of SOC reference.

SoC reference	H_p	m_{H_2} (g)	$m_{H_2, equ}$ (g)	SoC_{end}	$ \overline{\Delta P_{FC}} $ (W/s)	T_{step} (ms)
Linear Eq. (10)	5	256.0	253.9	0.3058	438.2	16.89
Linear Eq. (10)	10	254.4	252.4	0.3057	343.1	23.79
Linear Eq. (10)	15	253.8	251.8	0.3057	298.5	32.89
Adaptive Eq. (9)	5	236.7	229.8	0.3197	7.3	17.48
Adaptive Eq. (9)	10	234.0	231.8	0.3060	14.3	25.68
Adaptive Eq. (9)	15	235.8	233.6	0.3063	21.8	36.73

524 4.2.2. Comparative Study against Benchmark Control Strategy

525 To thoroughly evaluate the proposed PEMS, two commonly used control strategies are introduced as
526 comparison basis, where the DP-based strategy is deemed as the upper benchmark and the CD-CS
527 strategy is deemed as the lower benchmark.

528 • Benchmark EMS Description

529 As the upper benchmark, DP-based strategy aims at obtaining the global optima by minimizing the
530 predefined cost function. In this study, the DP problem is denoted as below:

$$\begin{aligned}
& \min_{\Delta P_{fc} \in \mu_{fc}} \sum_{k=0}^{N-1} \Delta m_{H_2} (\Delta P_{fc}(k)) \cdot \Delta T \quad (a) \\
& \text{s.t.} \begin{cases} 0.3 \leq SoC(k) \leq 0.9 & (b) \\ 0 \leq P_{fc}(k) \leq 30\text{kW} & (c) \\ -1\text{kW/s} \leq \Delta P_{fc}(k) \leq 1\text{kW/s} & (d) \\ -25\text{kW} \leq P_b(k) \leq 50\text{kW} & (e) \\ SoC_0 = 0.8, P_{fc_0} = 0\text{W} & (f) \\ SoC_N = 0.3 & (g) \end{cases} \quad (16)
\end{aligned}$$

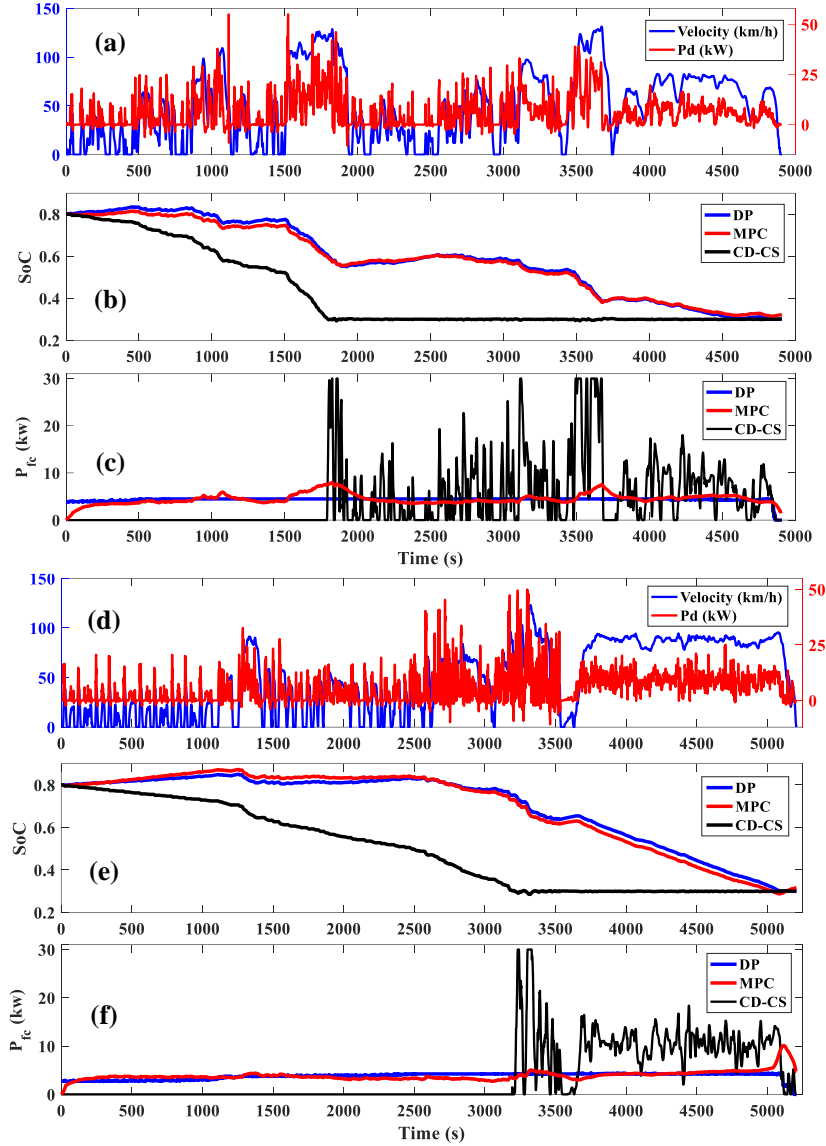
532 Note the fuel cell power-changing rate ΔP_{fc} is selected as the control variable and μ_{fc} is the discrete
533 feasible region for ΔP_{fc} , where the resolution of control (input) variable is set as $1 \text{ W} / \text{s}$. Besides,
534 $SoC, P_{fc}, \Delta P_{fc}$ and P_b are bounded in their allowable ranges, as indicated by (16b)-(16e). The initial
535 states for SoC and fuel cell power are defined by (16f). Constraint (16g) forces the final SoC reaching
536 the preset level 0.3.

537 In contrast, the CD-CS strategy controls the FC output power based on the SoC value. Specifically,
538 when SoC is higher than the threshold 0.3, the FCS switches off. When SoC is lower than this threshold,
539 the FCS switches on and the reference working point is set as $P_{fc_{max}} = 30 \text{ kW}$. To guarantee the fairness
540 for EMS comparison, the permissible FC power-changing rate for CD-CS strategy is bounded within
541 $[-1, 1] \text{ kW/s}$, which is identical to DP-based and MPC-based EMS.

542 • Evaluation against benchmark EMSs

543 Three EMSs are performed under two multi-pattern testing cycles (namely CYCLE1 and CYCLE2).
544 Note H_p is set to 5s and k_α is set to 2. The performance discrepancies among three EMSs are shown in
545 Fig. 8(a)-(f). As can be seen, under both testing cycles, the SoC profiles of the MPC-based EMS are
546 close to the DP benchmarks, while the CD-CS strategy depletes the battery energy more quickly than
547 other strategies. Specifically, due to the availability of entire trip information, DP strategy can urge the
548 FCS working steadily along the trip with few power transients. In contrast, MPC-based EMS can greatly
549 restrict the FC power transients. The CD-CS strategy switches the FCS off when the SoC is higher than
550 0.3. Afterwards, when the battery SoC drops below 0.3, the FCS frequently turns on and off to maintain
551 the SoC level. As a result, much more FC power transients can be observed within the entire CS phases.
552 TABLE VI summaries the numerical results of three strategies. In contrast to CD-CS benchmark, the
553 MPC-based EMS can respectively reduce $m_{H_2, equ}$ by 15.30% and 12.05% under both testing cycles.
554 Moreover, compared to DP benchmark, its performance gaps on $m_{H_2, equ}$ are respectively 3.74% and
555 4.88%. In addition, the MPC-based EMS can suppress the FC power transients under both testing cycles
556 by 96.80% and 94.90% compared to CD-CS strategy, thus reducing the possibility of fuel cell
557 performance degradation imposed by dynamic load shifts. Finally, it can be observed that as a global

558 optima-searching approach, DP benchmark consumes the largest amount of computation time, while the
 559 online computation burden for MPC-based EMS is adequately smaller in contrast to the sampling period
 560 (1s) and thus is affordable for online implementations.



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563 Fig. 8 (a)-(f). Performance discrepancy of three control strategies under multi-pattern driving cycles. (a)-(c) Evaluation results

564

on CYCLE1. (d)-(f) Evaluation results on CYCLE2.

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TABLE VI. EMS results compared to benchmark strategies.

EMS		m_{H_2} (g)	$m_{H_2, \text{equ}}$ (g)	SoC_{end}	$ \Delta P_{FC} $ (W/s)	T_{total} (s)	T_{step} (ms)
CYCLE1	DP	245.9	245.9	0.3000	5.6	412.36	N/A
	MPC	262.8	255.1	0.3218	11.8	81.13	16.39
	CD-CS	301.6	301.2	0.3011	375.1	11.48	2.32
CYCLE2	DP	223.5	223.5	0.3000	7.3	489.56	N/A
	MPC	240.3	234.4	0.3168	9.4	87.72	17.20
	CD-CS	266.8	266.5	0.3008	185.2	15.56	3.05

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- Influences on EMS performance imposed by T_{trip} estimation errors

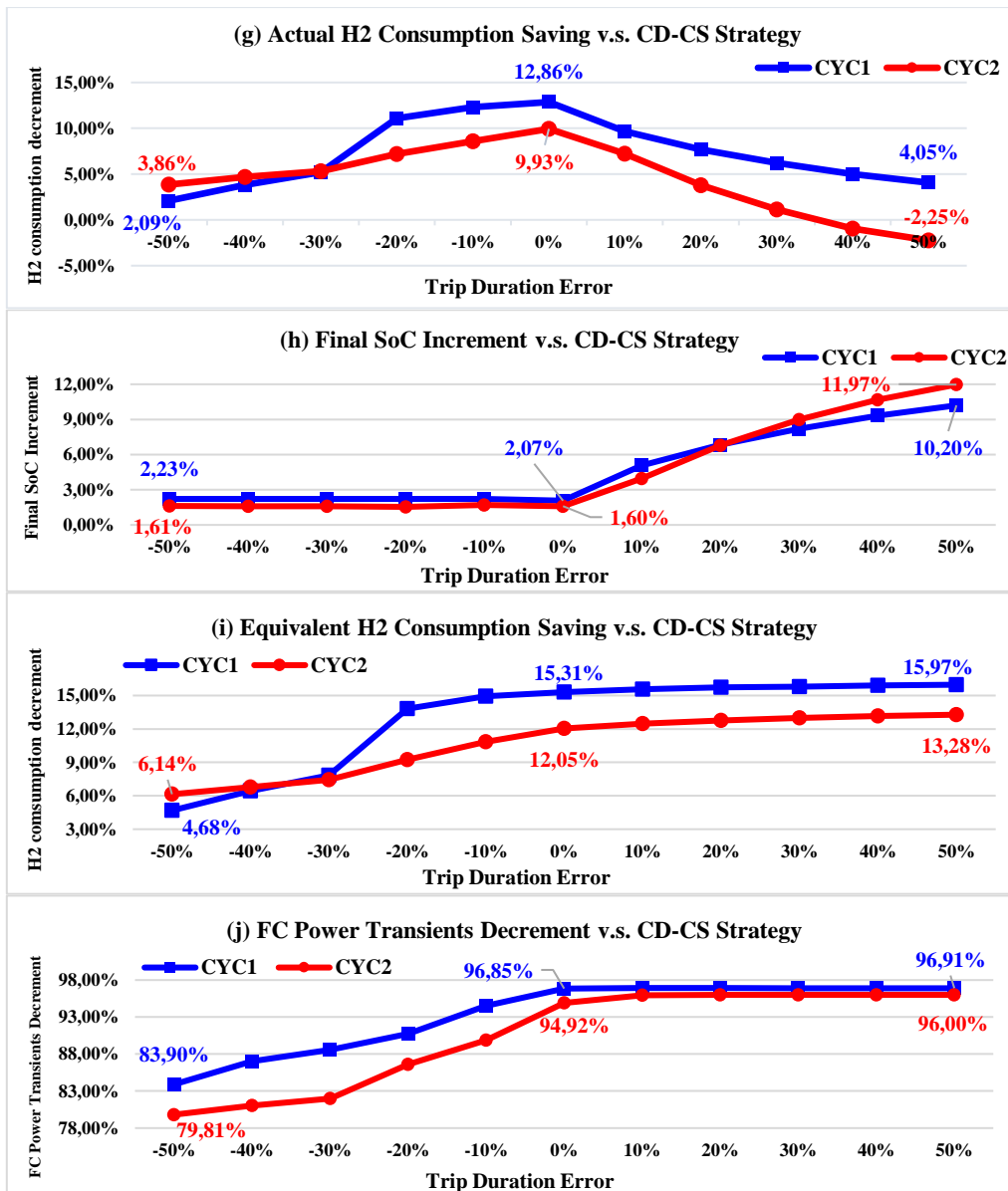
567 As indicated in (9), the planning of battery energy depletion is realized by assuming the information of
568 estimated trip time can be obtained in advance. Nevertheless, many uncertain events, like the traffic
569 congestions or the driving routes adjustment, will eventually lead to the discrepancy between the
570 estimated T_{trip} and the actual one. To study the possible influences on EMS performance, different levels
571 of trip duration errors (ranging from -50% to 50% of the real trip time) are applied to the proposed SoC
572 reference generator (9). Positive errors indicate the estimated trip duration is larger in contrast to the
573 real trip time, whereas negative ones mean the opposite. Under $\pm 50\%$ estimation errors, the MPC-based
574 EMS is performed under CYCLE1 and CYCLE2, where the performance gaps against the CD-CS
575 benchmark are given in Fig. 8(g)-(j).

576 ➤ **Fuel Economy Comparison**

577 As shown in Fig. 8(g), when positive errors (0 to 50%) appear, the performance gap on the actual H2
578 consumption against the CD-CS benchmark is shrinking on both testing cycles. This is because the
579 enlarged T_{trip} would slow down the SoC declining rate, resulting in the larger amount of remaining
580 battery energy (see Fig. 8(h)). However, since the FCS's working efficiency can be maintained relatively
581 stable, the performance on the equivalent H2 consumption remains almost the same as the "zero-error"
582 conditions (Fig. 8(i)). In contrast, when negative errors occur (0% to -50%), the adaptive SoC reference
583 generator would lead to a faster battery energy usage, thus extending the CS driving phases.
584 Consequently, the FCS tends to work at higher power level for both supplying the external power
585 demands and sustaining SoC level, thus compromising fuel efficiency performance.

586 ➤ **FC Power Transients Comparison**

587 Additionally, as depicted in Fig. 8(j), the FC power transients would be enlarged if negative errors
588 appear, whereas it would remain nearly unchanged when positive errors occur. This is because the
589 prolonged CS phases imposed by the minus errors enforce fuel cell operating in a more active manner,
590 thus increasing the power spikes. In contrast, the period of CS working stage would be reduced (or even
591 eliminated) under positive errors and thus the FC power transients would remain almost the same level
592 as "zero-error" conditions.



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Fig. 8(g)-(j). MPC-based EMS performance deviations against CD-CS strategy under different trip duration errors.

Overall, despite $\pm 50\%$ trip duration errors, the MPC-based EMS can effectively (1) improve the fuel efficiency by at least 4.68% (CYCLE1) and 6.14% (CYCLE2), and (2) reduce the FC power spikes by at least 83.90% (CYCLE1) and 79.81% (CYCLE2), compared to CD-CS strategy. To sum up, in face of the trip the duration errors imposed by unpredictable traffic conditions, the proposed EMS could still outperform the CD-CS benchmark, thus denoting its potential for actual applications.

• **Influences on EMS performance imposed by vehicle powertrain sizing configuration**

This work adopts an available powertrain sizing configuration from [16] for EMS development, where the FCS is functioned as a range extender. Under such powertrain configuration, battery can offer the

606 majority of vehicular power demand if its SoC is high (e.g. $SoC_{ini} = 0.8$ in all case studies). In this case,
607 the FCS does not necessarily work towards its nominal power level. Moreover, benefiting from the
608 previewed trip knowledge, DP and MPC-based strategies can better anticipate and control the SoC drop
609 compared to the CD-CS strategy, thus making as much FCS working points as possible towards the
610 most efficient point (~ 5 kW) for saving H₂ and enhancing FCS working efficiency. Although the FCS
611 seems to be oversized when battery SoC is high, it is still meaningful of using a 30 kW FCS, since it
612 can provide sufficient traction power to ensure the vehicle's operation safety when SoC emergency
613 event occurs. Furthermore, if we slightly downsize the battery capacity in the current powertrain, larger
614 portion of vehicular power demand would be supplied by FCS. As a result, the corresponding increased
615 average FCS power level would lead to a higher FCS efficiency, and escaping from extremely low
616 loading conditions would contribute to the FCS lifetime extension.

617 **V. Conclusion**

618 This paper proposes a multi-criteria power allocation strategy for a fuel cell/battery-based plug-in hybrid
619 electric vehicle. Firstly, a novel speed-forecast approach using online-learning Markov Chain is
620 designed. Afterwards, a state-of-charge reference planning approach is designed for guiding battery
621 energy allocation. Combining the speed-forecast results and the reference SoC value, MPC acquires the
622 optimal control action through minimizing the multi-purpose objective function in a finite time horizon.
623 The important findings in this research are detailed as below:

- 624 1) Compared to benchmark predictors, the benefits of the online-learning Markov velocity-forecast
625 approach lie in: (a) the reduced dependency on the offline driving database since its TPMs are identified
626 online using the recently measured data; (b) the higher prediction robustness towards the new driving
627 conditions since its predictive behaviors can be adjusted by the real-time updated TPMs. Moreover,
628 validation results show the proposed method is more capable of describing the future speed dynamics
629 under complicated driving conditions.
- 630 2) Assisted by the estimated trip duration information and the speed-forecast results, the rapid SoC
631 reference planning approach is able to adjust the battery energy-declining rate with respect to various

632 driving patterns, thus enhancing the rationality in battery energy allocation in contrast to linear SoC
633 reference model.

634 3) In contrast to CD-CS benchmark, the proposed EMS can conserve the equivalent hydrogen
635 consumption by over 12.05% and suppress the average FC power transients by over 94.90%, indicating
636 the enhanced FCS efficiency and durability. Furthermore, in spite of trip time prediction errors, the
637 presented control strategy is still able to bring performance improvement over CD-CS benchmark,
638 which should be deemed as the potential benefits for its real-world implementations.

639 Future works will focus on developing a data-driven SoC reference estimation approach, which would
640 be embedded into the EMS of a FCPHEV dedicated to postal-delivery.

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