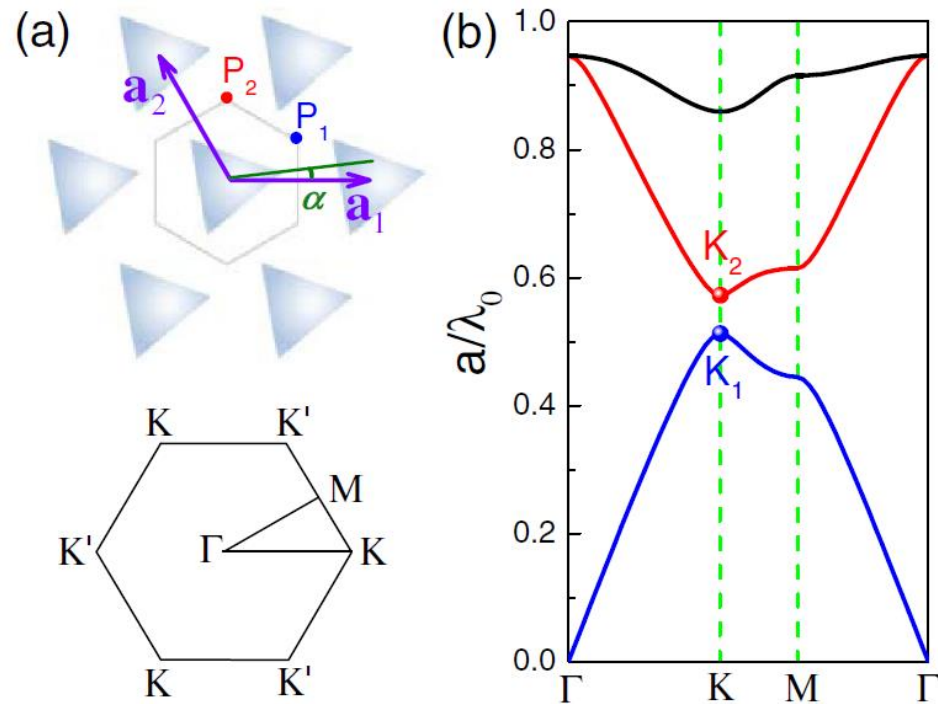


Acoustic topological circuitry in square and rectangular phononic crystals

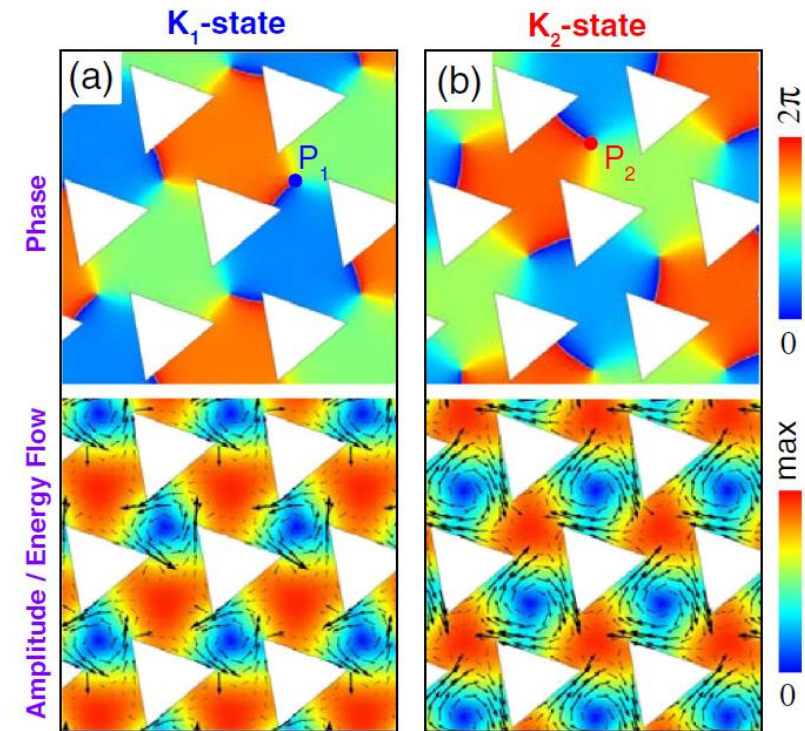
NICOLAS LAFORGE, RICHARD WILTSHAW, RICHARD V. CRASTER, VINCENT LAUDE, JULIO ANDRÉS IGLESIAS MARTINEZ, GUILLAUME DUPONT, SÉBASTIEN GUENNEAU, MUAMER KADIC AND MEHUL P. MAKWANA

Acoustic analog of quantum valley Hall effect



Lu *et al.*, Phys. Rev. Lett. 116, 093901 (2016).

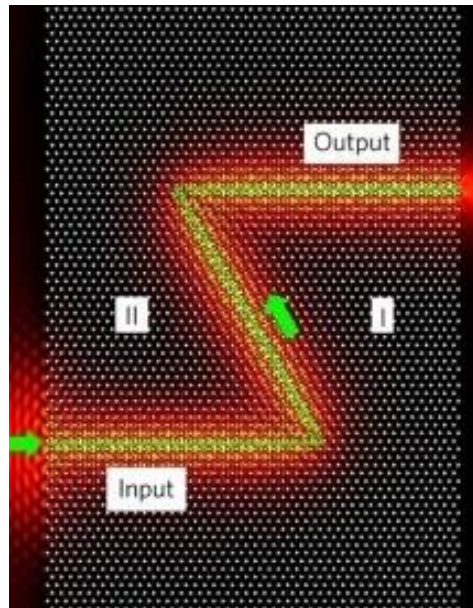
Lu *et al.*, Nat. Phys. 13, 369 (2017).



- (Bloch) vortex waves at the K point hold the topological *valley* invariant
- Edge modes guided at a domain wall are formed by combining crystals with angles $\pm\alpha$

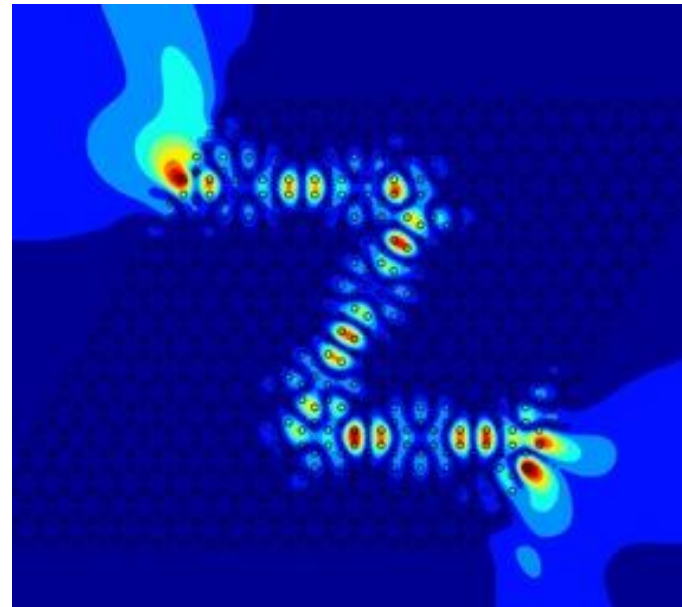
Three K Points: no backscattering in 3 directions

Acoustics



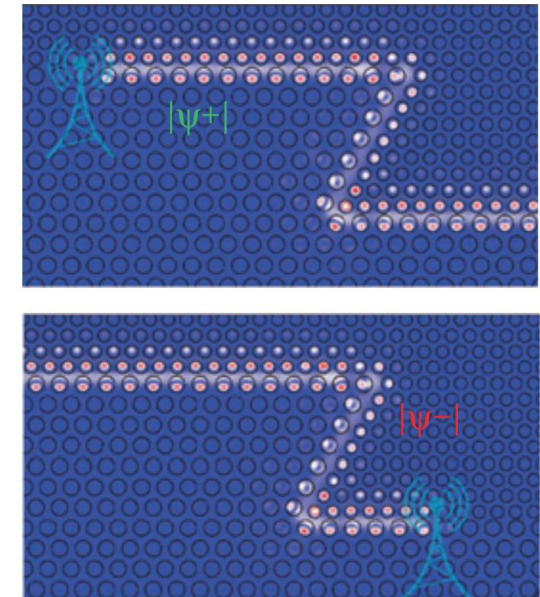
Lu *et al.*, *Nat. Phys.* 13
(2017) 369

Elastic waves



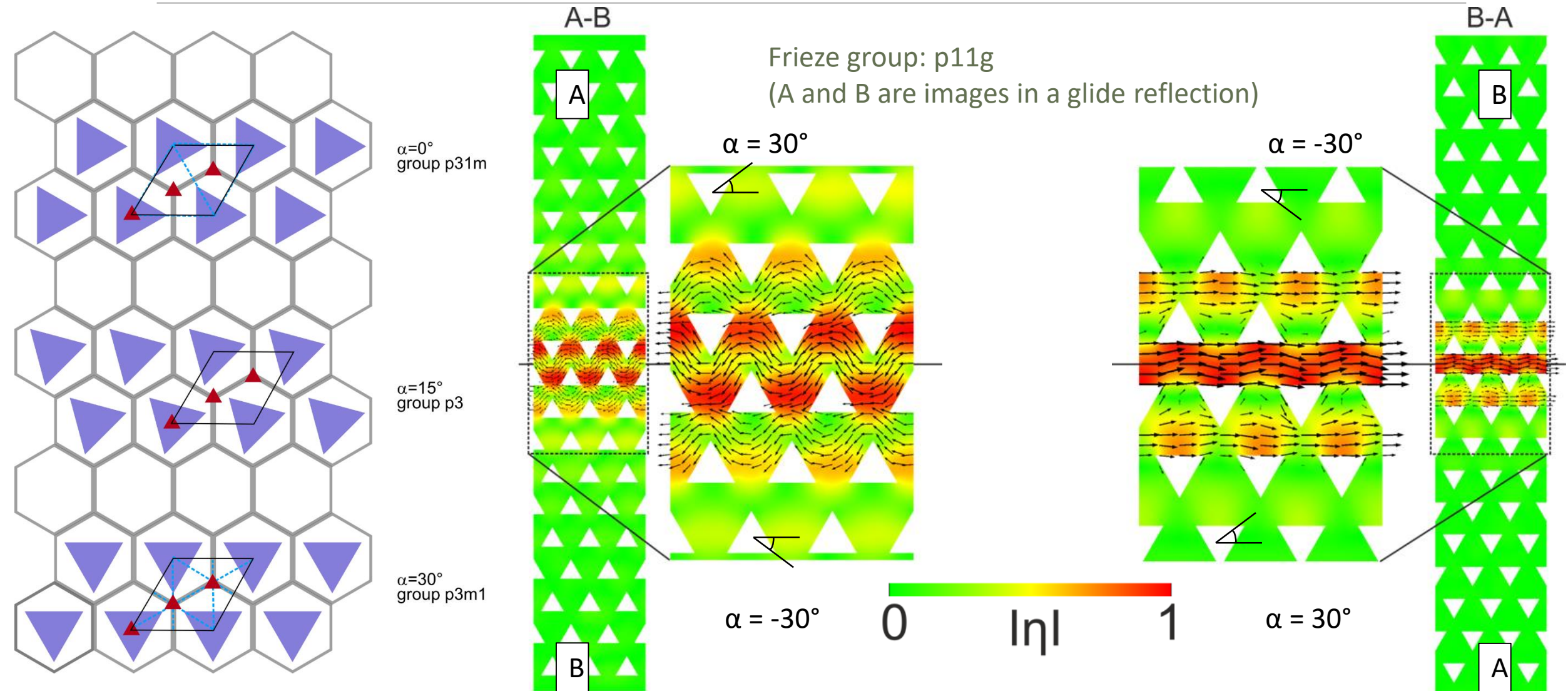
Pal *et al.*, *New J. Phys.* 19,2
(2017) 025001

Optics

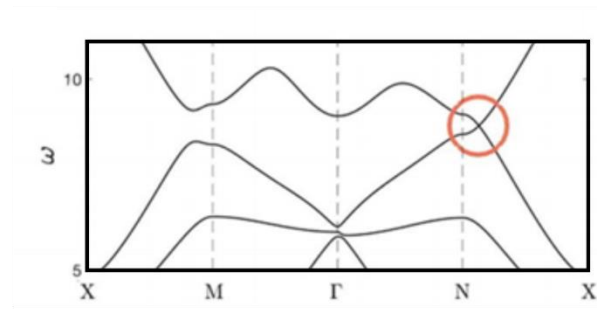
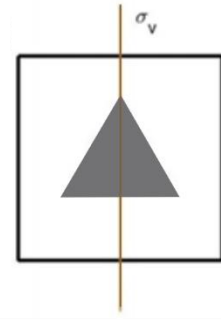


Khanikaev *et al.*, *Nat. Mater.* 12
(2012) 223

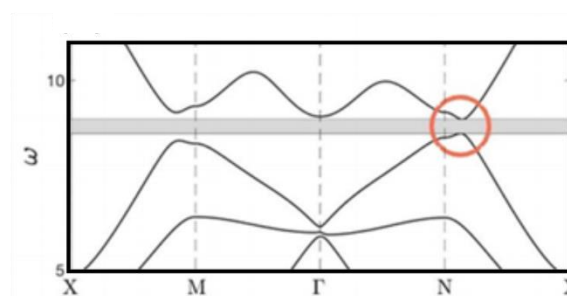
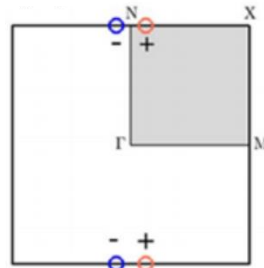
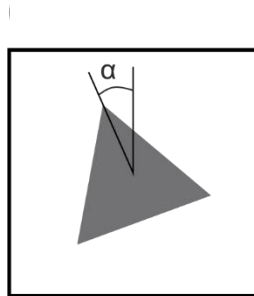
Space groups of the 2D crystal and the 1D waveguide



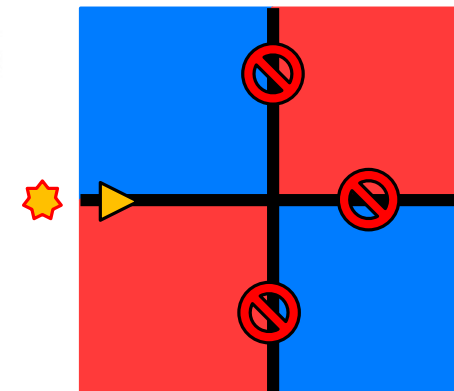
Dirac points in the square lattice? 3-way splitter?



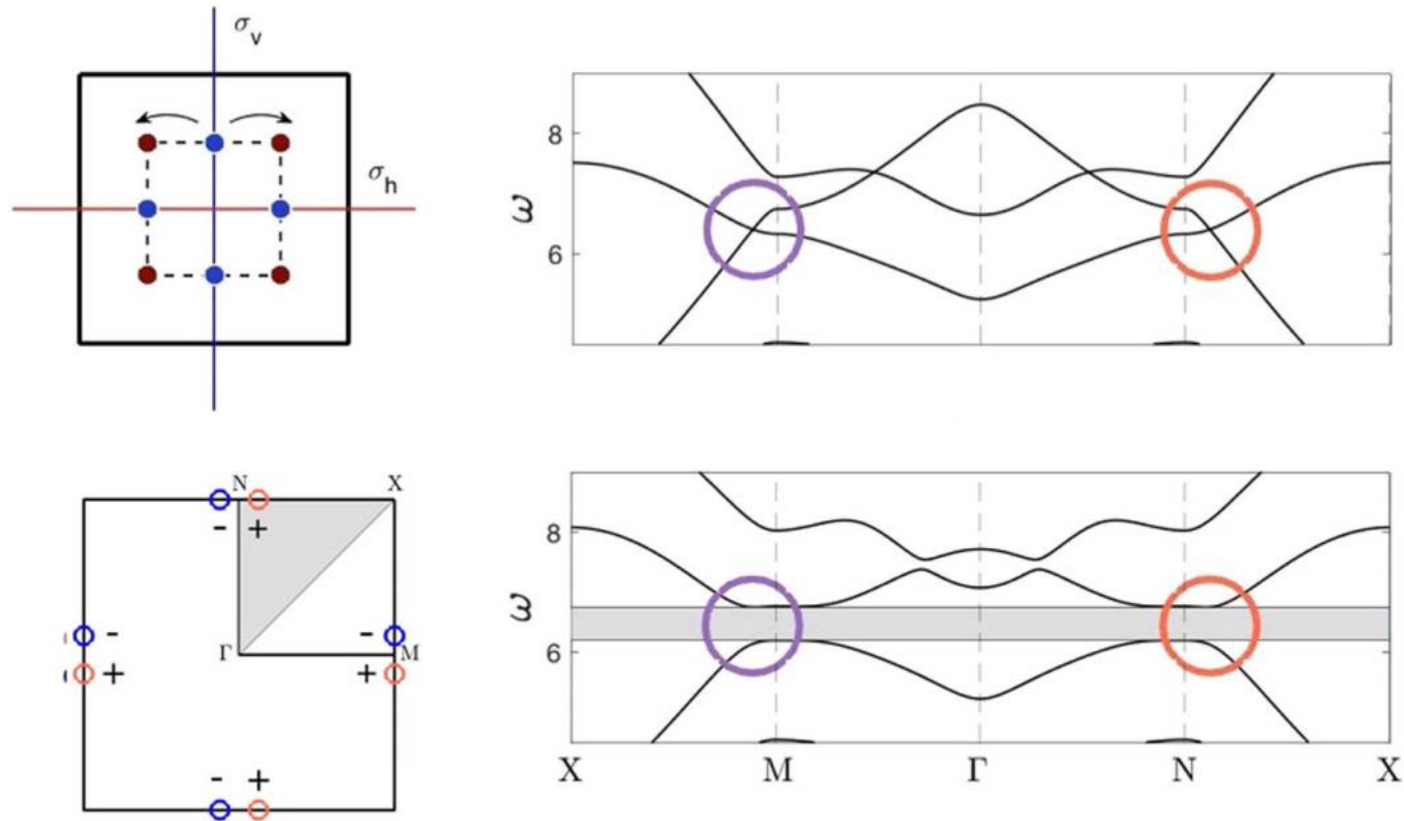
Makwana, M.P., Chaplain, G. Tunable three-way topological energy-splitter. *Sci Rep* **9**, 18939 (2019)



The sign of the Chern number associated with Dirac cones dictates if waves go along a domain wall or not



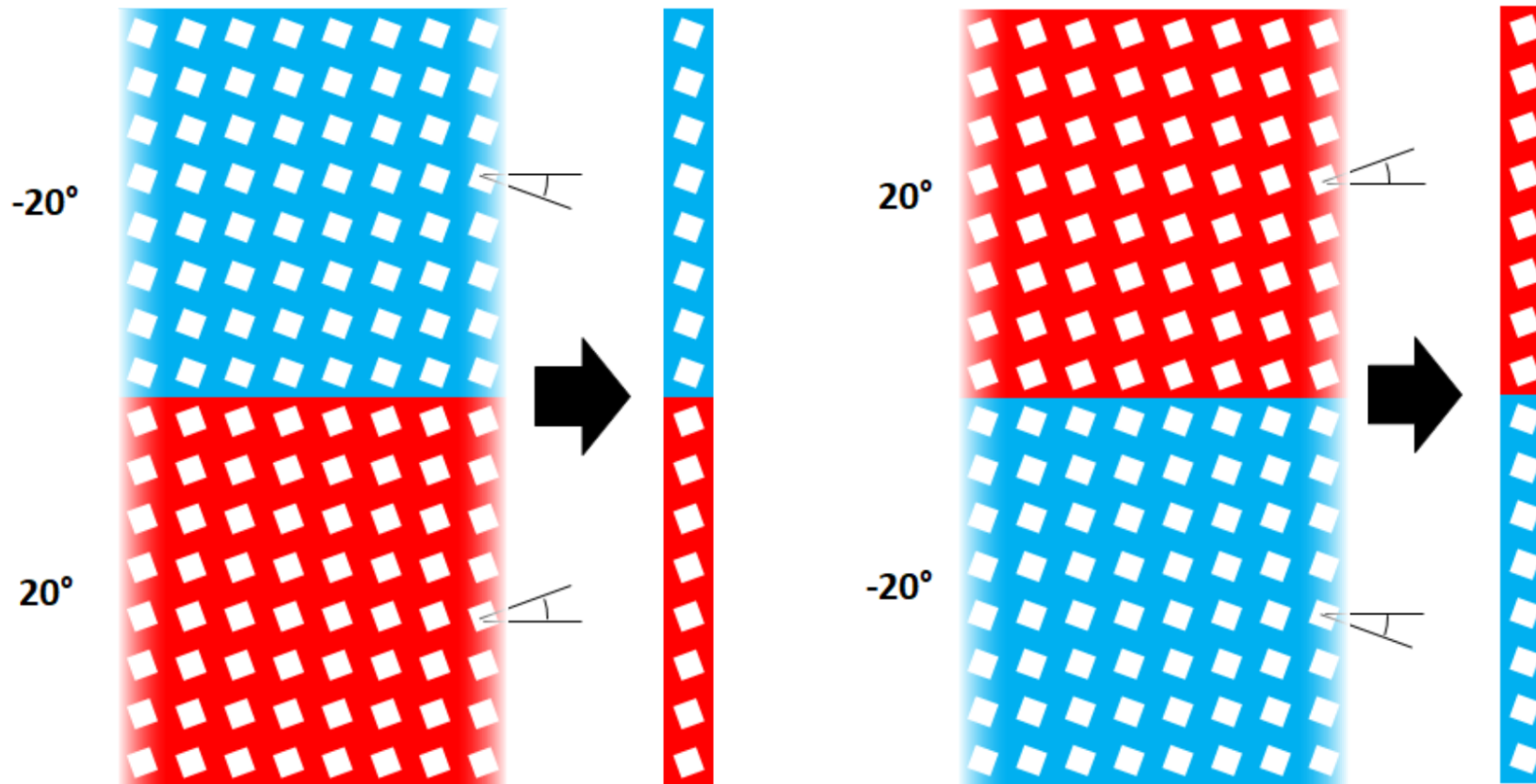
Square inclusion in square-lattice



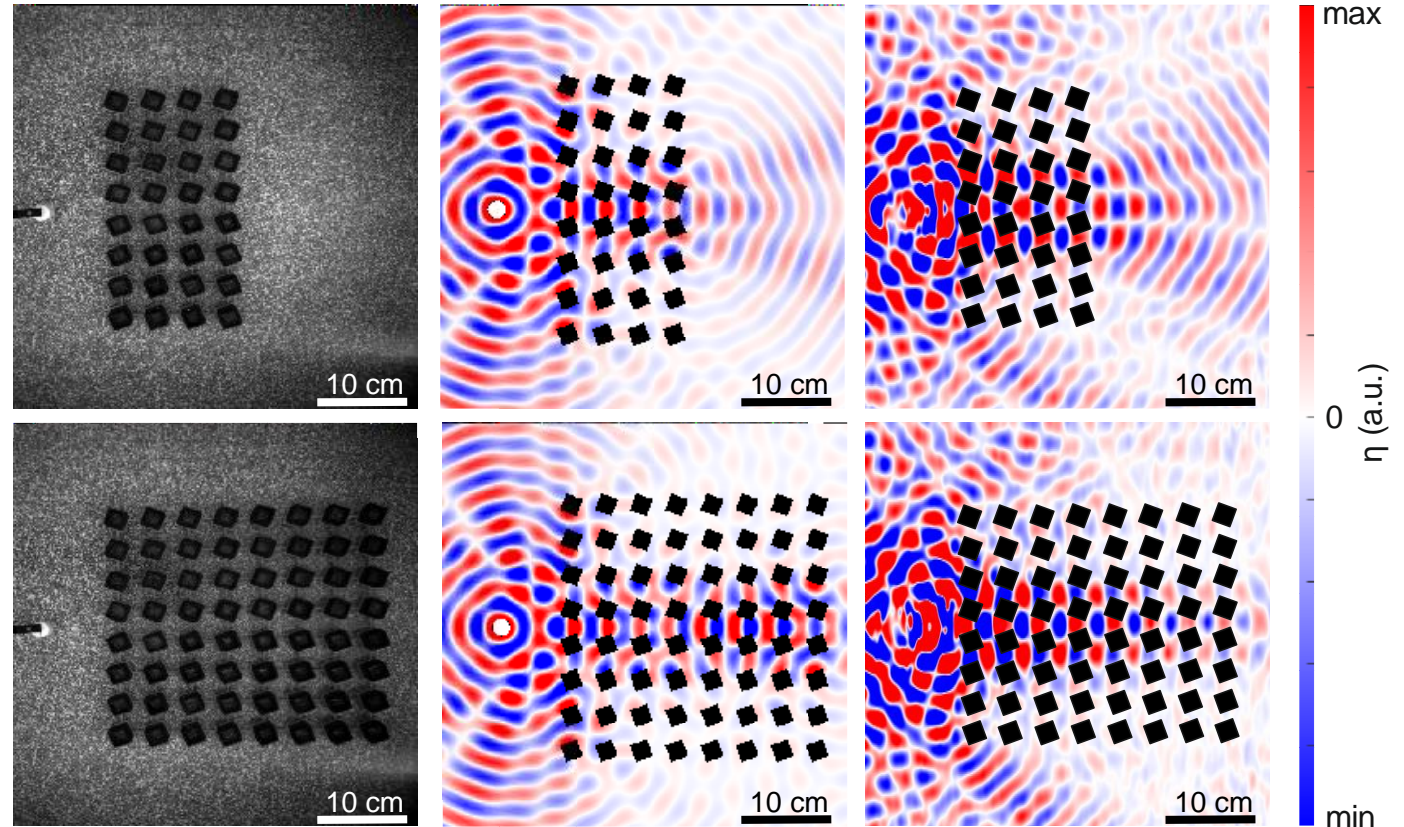
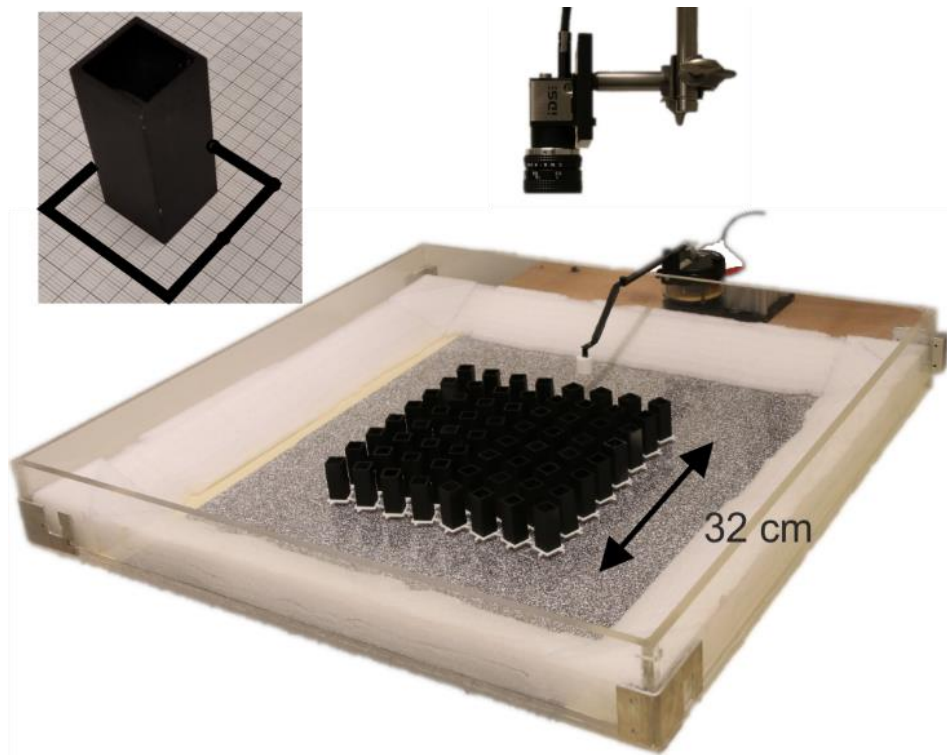
A pair of Dirac points is needed along each direction

Makwana, M.P., Chaplain, G. Tunable three-way topological energy-splitter. *Sci Rep* **9**, 18939 (2019)

Domain walls with square-lattice crystal



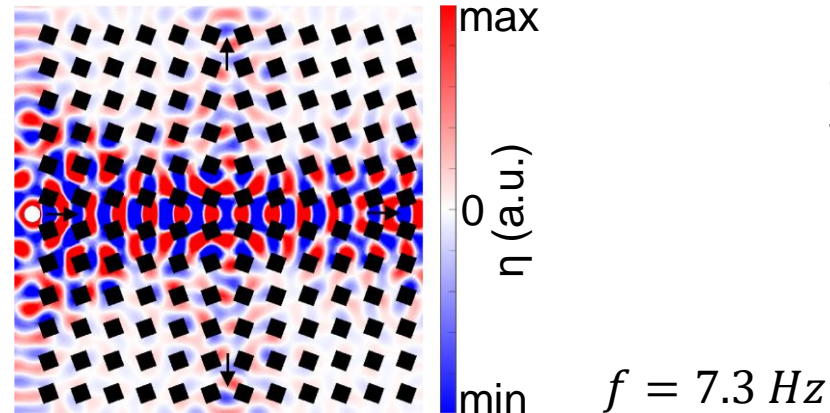
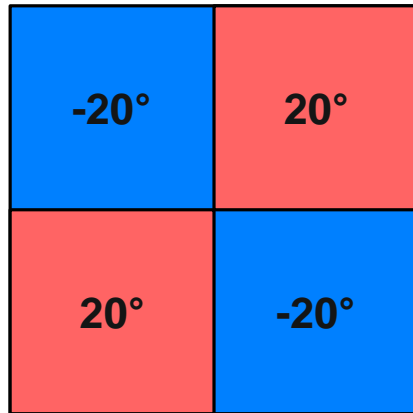
Square-lattice topological crystal: water waves



Makwana, Mehul P., et al. "Experimental observations of topologically guided water waves within non-hexagonal structures." *Applied Physics Letters* 116.13 (2020): 131603.

$$f = 7.3 \text{ Hz}$$

3-way splitter with water waves?

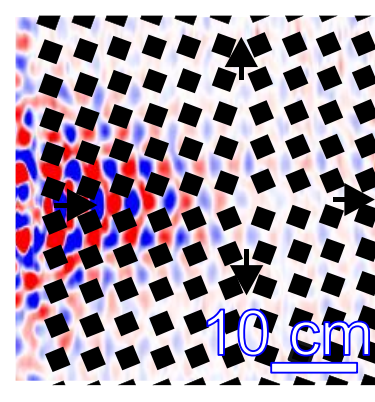
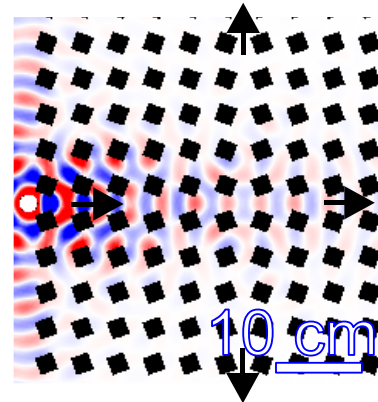
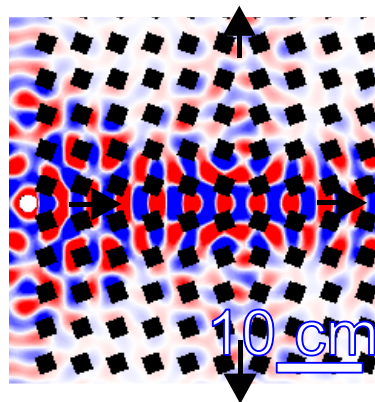


Makwana, Mehul P., et al. "Experimental observations of topologically guided water waves within non-hexagonal structures." *Applied Physics Letters* 116.13 (2020): 131603.

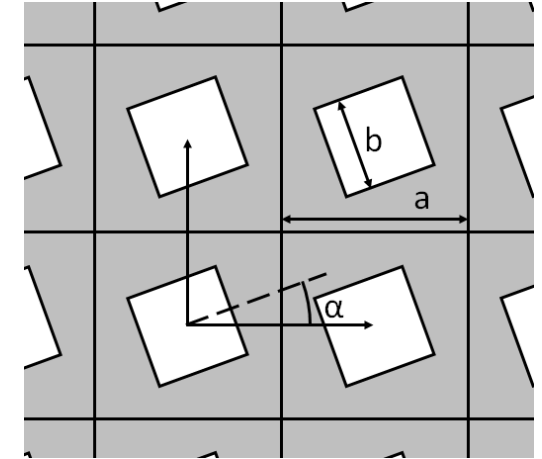
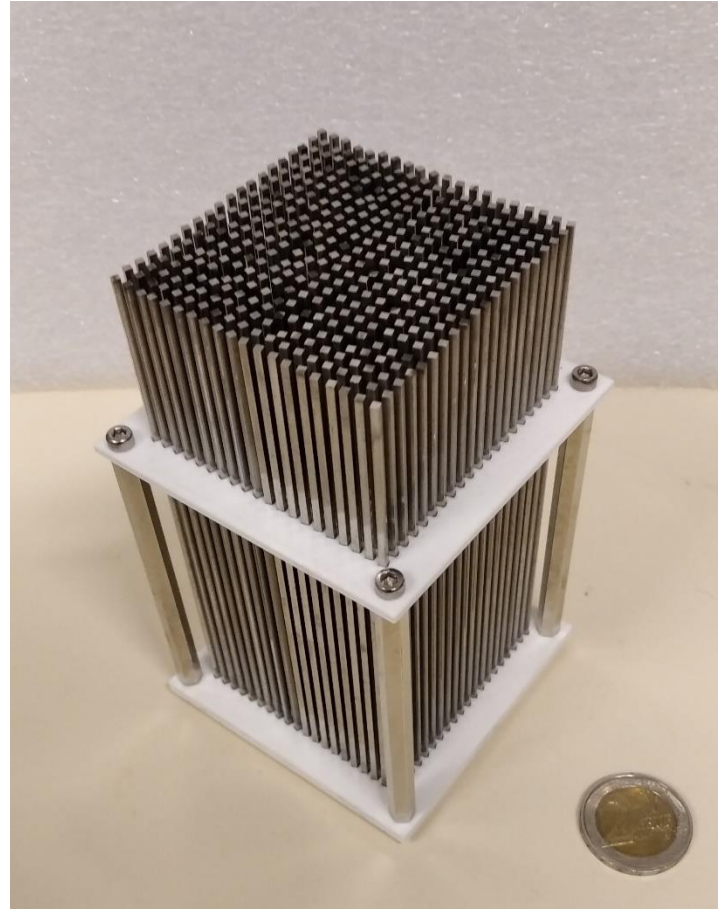
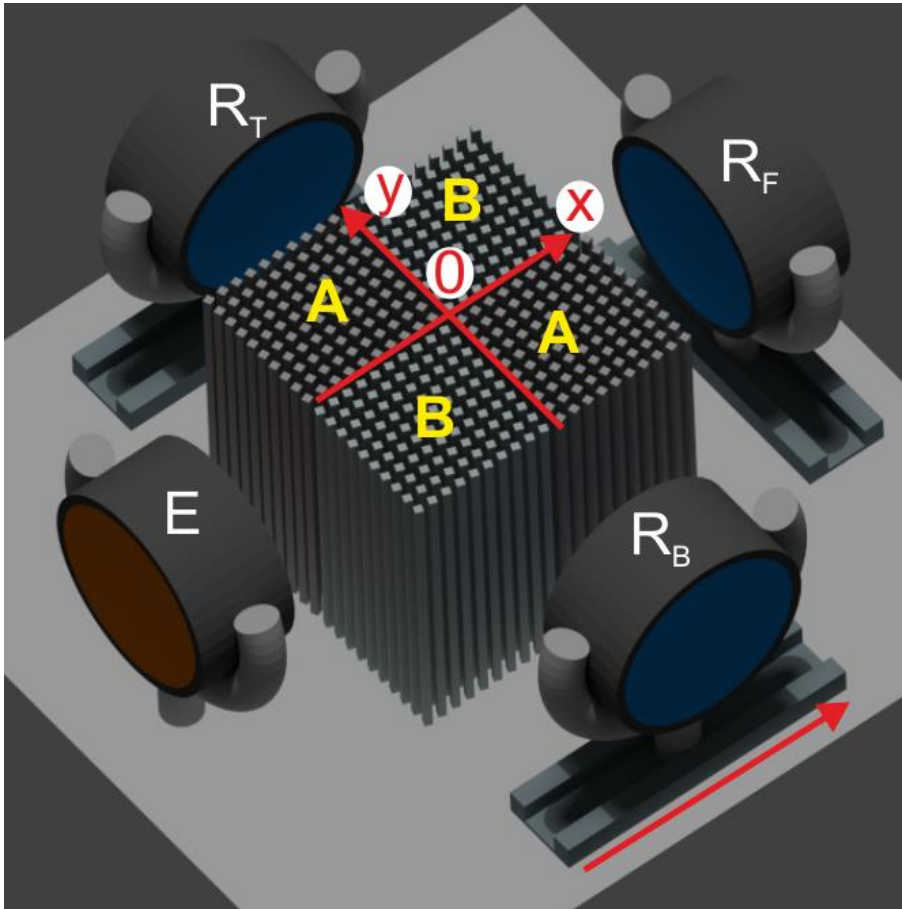
Simulation without dissipation

Simulation with dissipation

Experiment



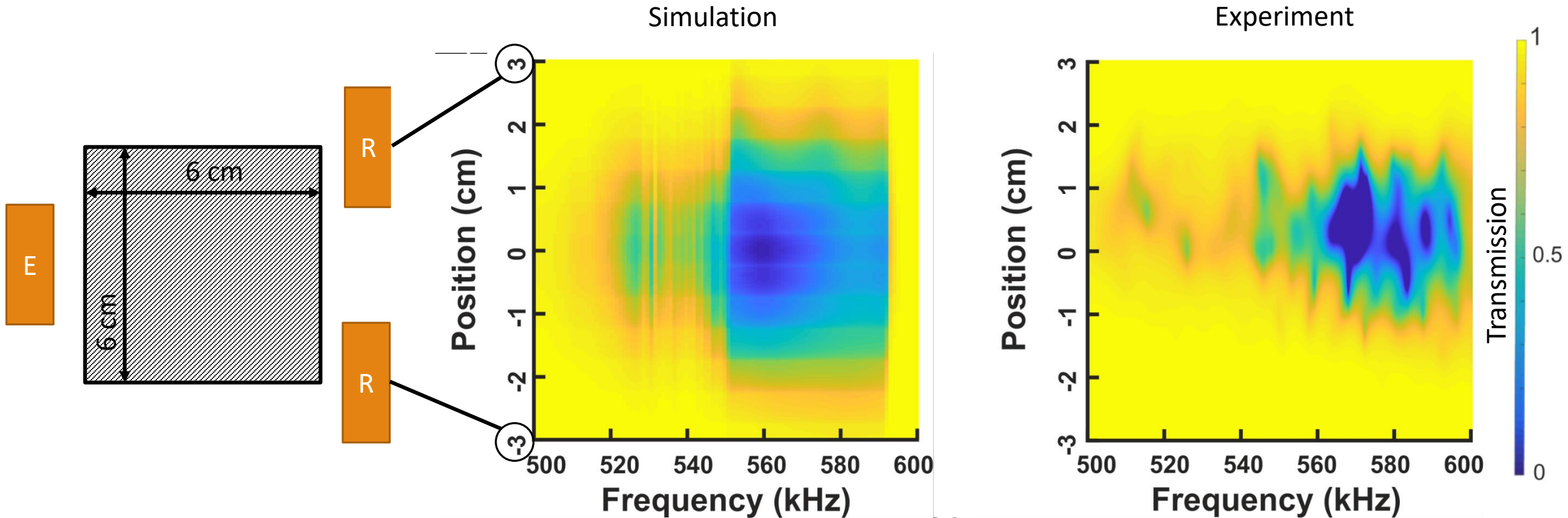
Square lattice topological crystal: acoustic waves



$$a = 3 \text{ mm}, b = 1.5 \text{ mm}$$
$$f \sim 500 \text{ kHz}$$

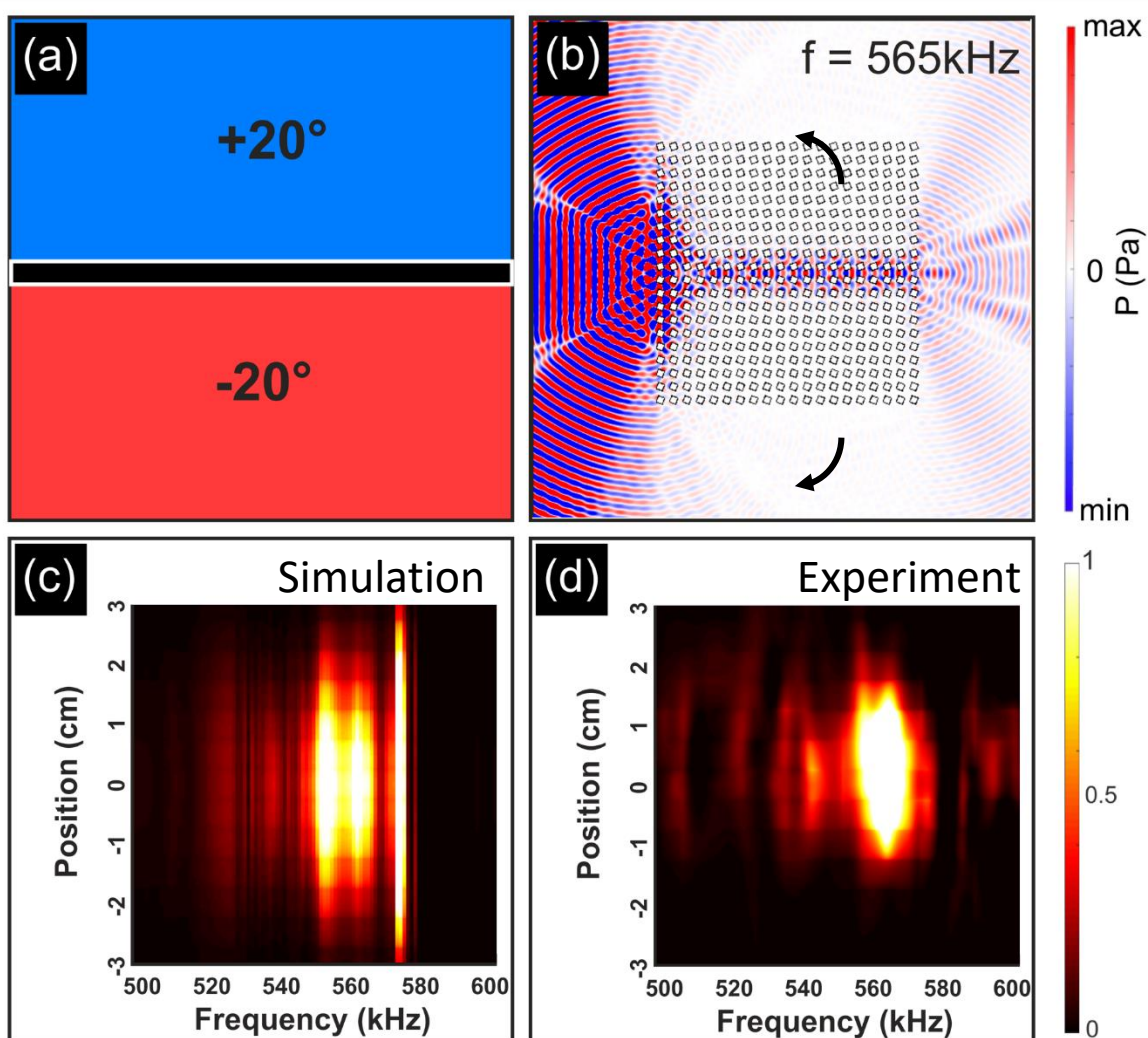
Laforge, Nicolas, et al. "Acoustic topological circuitry in square and rectangular phononic crystals." arXiv preprint arXiv:2012.08014 (2020).

Measuring the phononic band gap



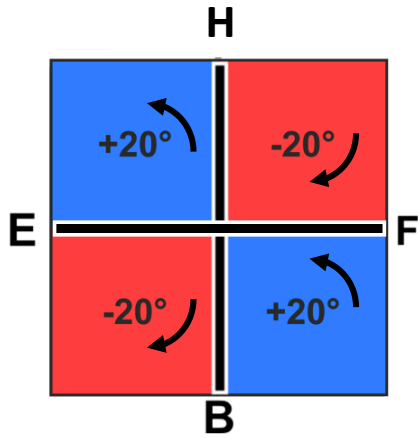
Laforge, Nicolas, et al. "Acoustic topological circuitry in square and rectangular phononic crystals." arXiv preprint arXiv:2012.08014 (2020).

Measuring the domain wall waveguide

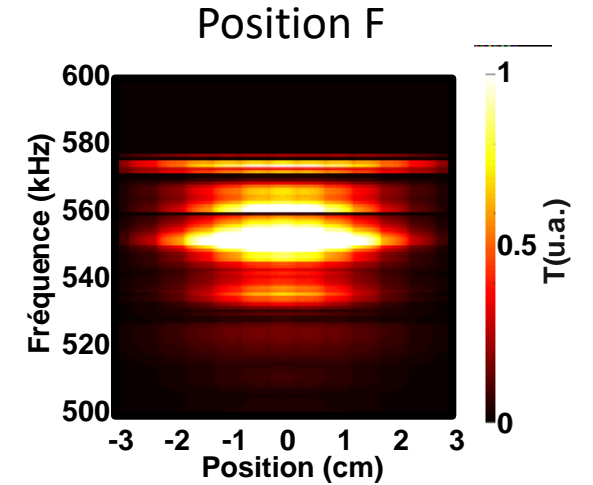
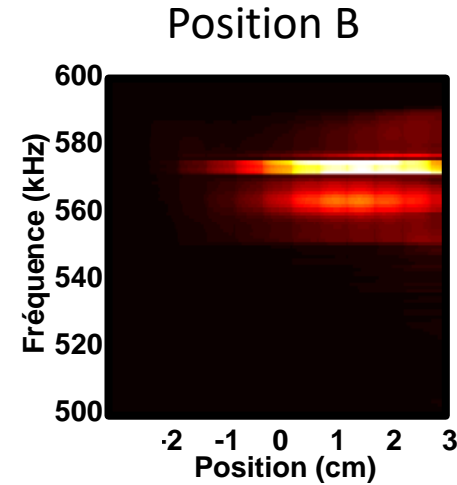
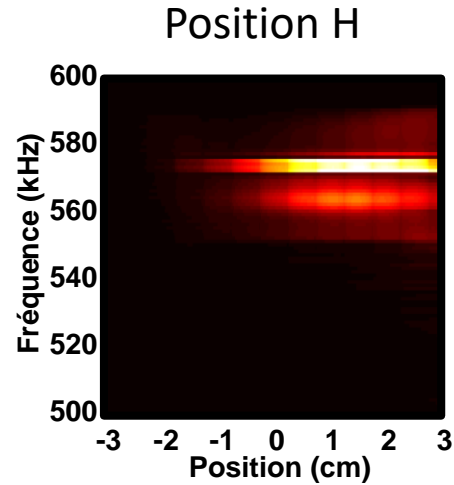


Laforge, Nicolas, et al. "Acoustic topological circuitry in square and rectangular phononic crystals." arXiv preprint arXiv:2012.08014 (2020).

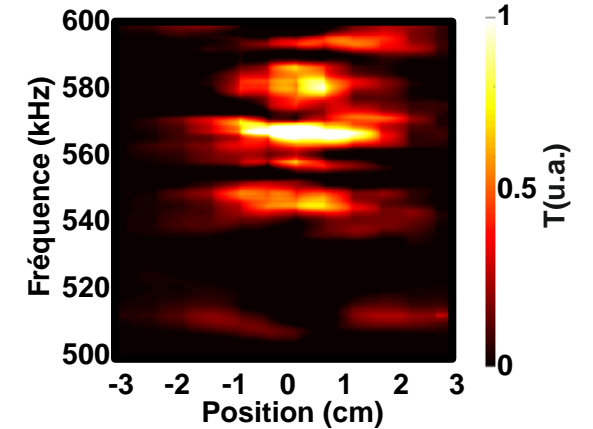
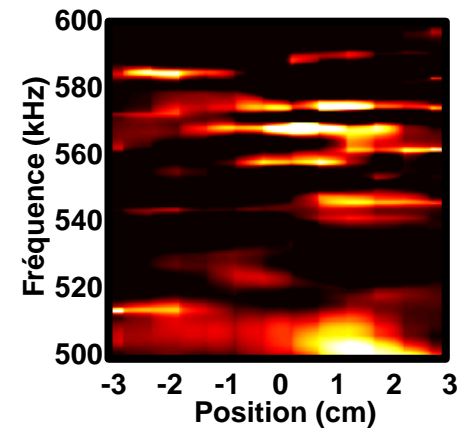
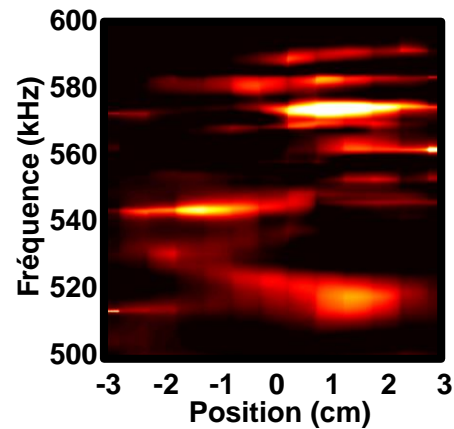
3-way splitter, square-lattice



Simulations

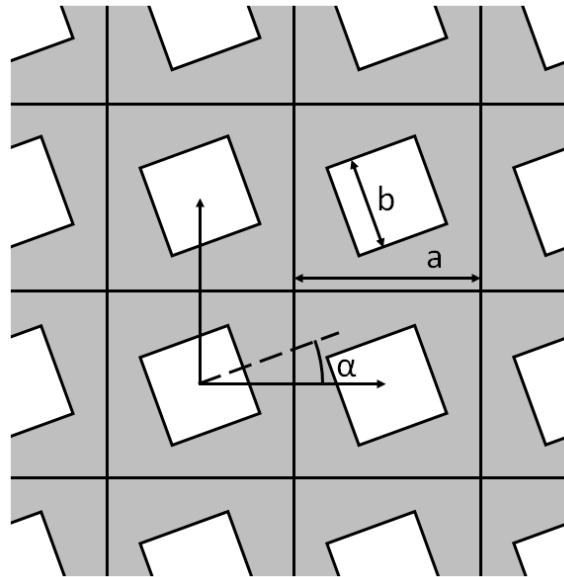
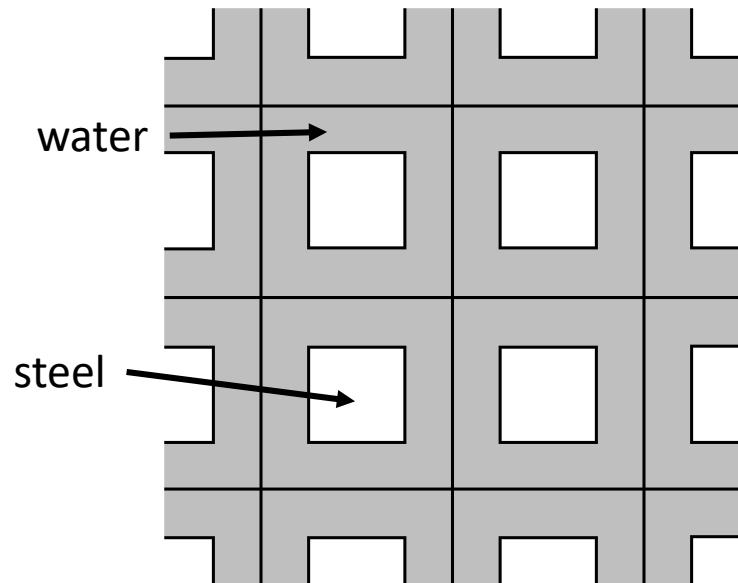


Experiment



Laforge, Nicolas, et al. "Acoustic topological circuitry in square and rectangular phononic crystals." arXiv preprint arXiv:2012.08014 (2020).

Coupling of acoustic and elastic waves



$$\nabla \cdot (\rho_1^{-1} \nabla p) = \frac{1}{\kappa} \frac{\partial^2 p}{\partial t^2}$$

$$\nabla \cdot [\mathbb{C} : \nabla \mathbf{u}] = \rho_2 \frac{\partial^2 \mathbf{u}}{\partial t^2}$$

Acoustoelastic coupling:

$$\mathbf{T} = \mathbb{C} : \nabla \mathbf{u}$$

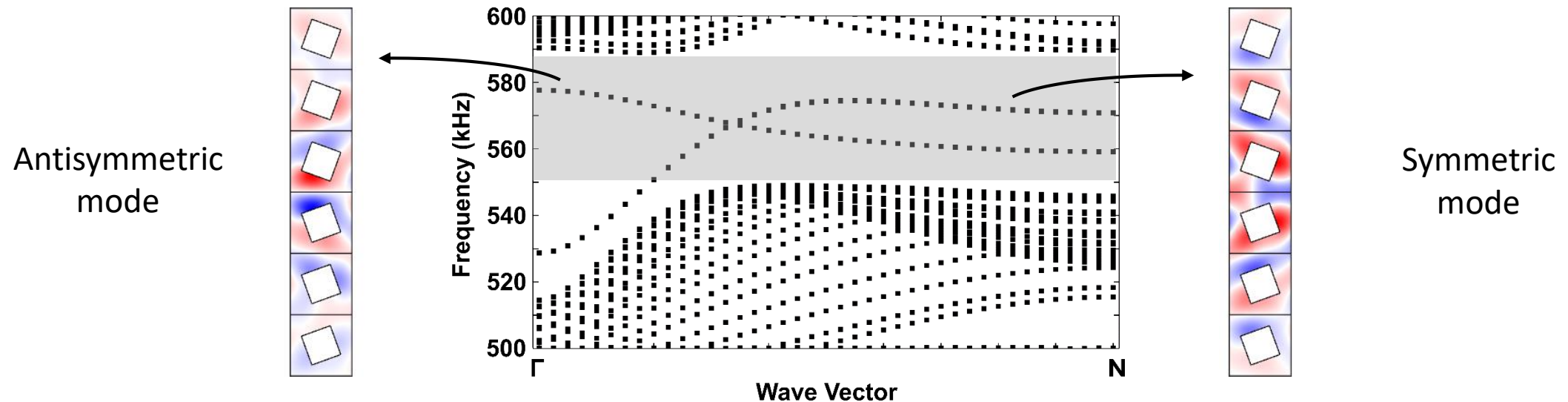
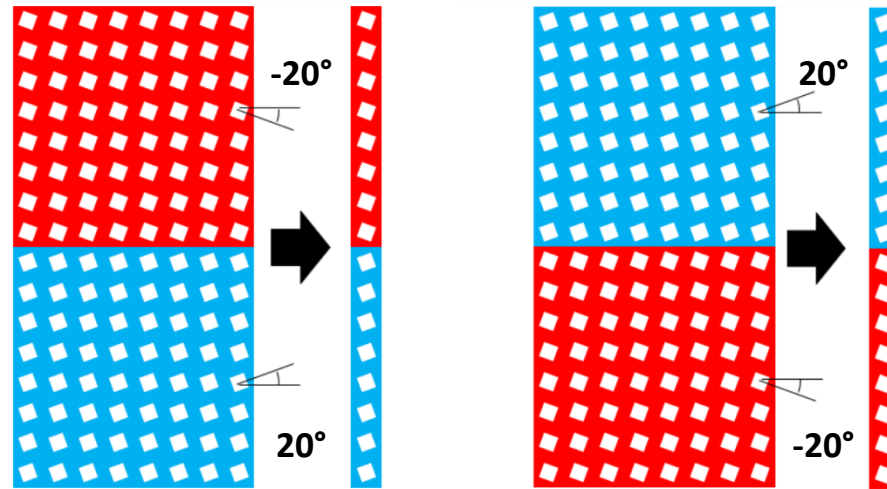
$$T_{ij} n_j = -p n_i$$

$$\mathbf{n} \cdot (\rho_1^{-1} \nabla p) = -\mathbf{n} \cdot \frac{\partial^2 \mathbf{u}}{\partial t^2}$$

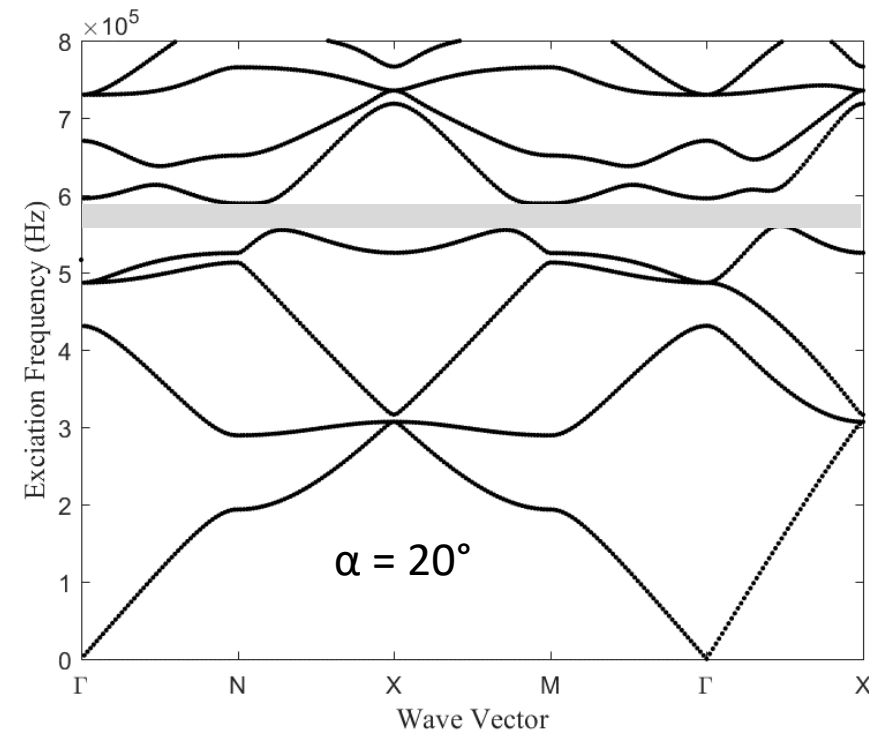
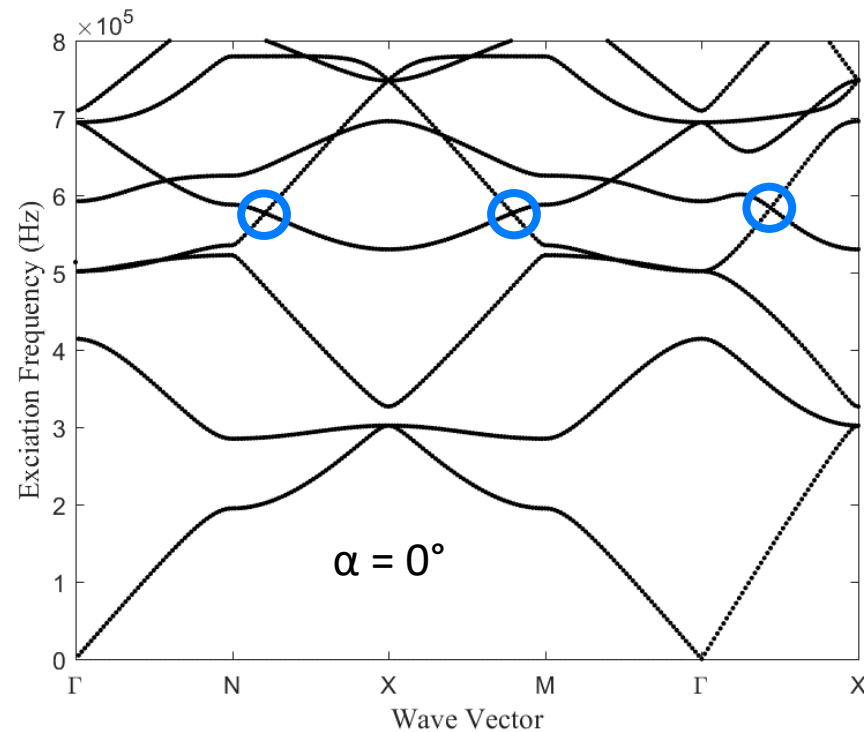
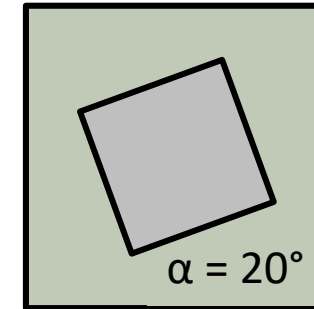
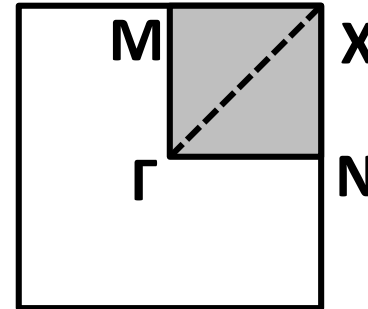
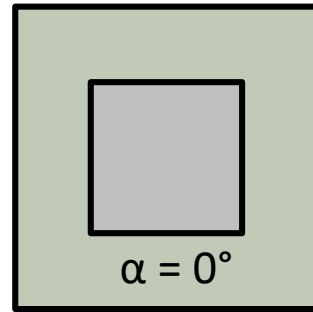
$$a = 3 \text{ mm}, b = 1.5 \text{ mm}$$

Dispersion of guided waves

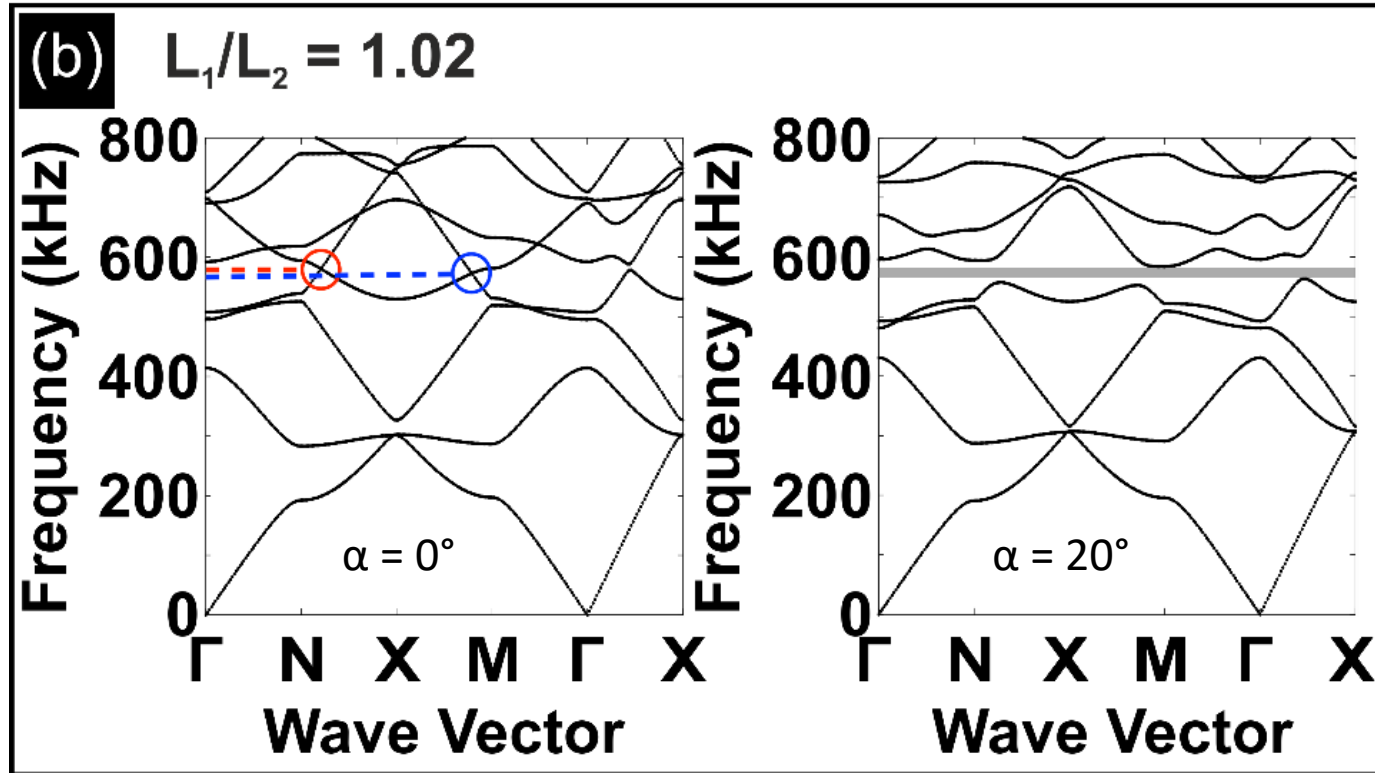
Laforge, Nicolas, et al. "Acoustic topological circuitry in square and rectangular phononic crystals." arXiv preprint arXiv:2012.08014 (2020).



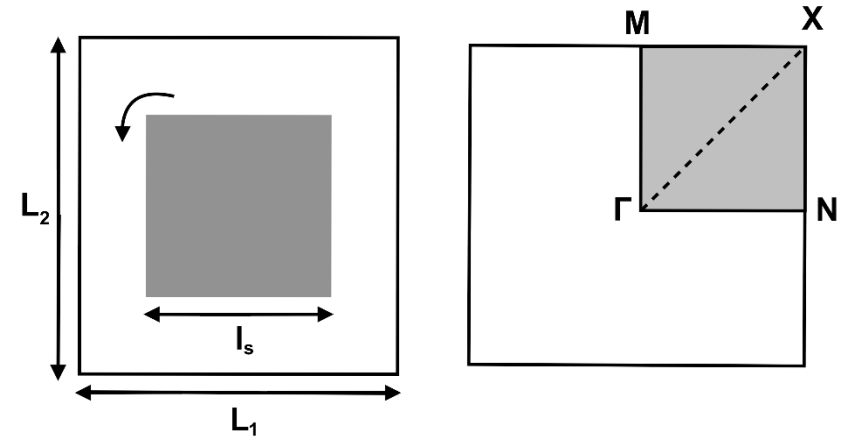
Trouble is... there's a third Dirac point!



Breaking diagonal symmetry removes the third Dirac point

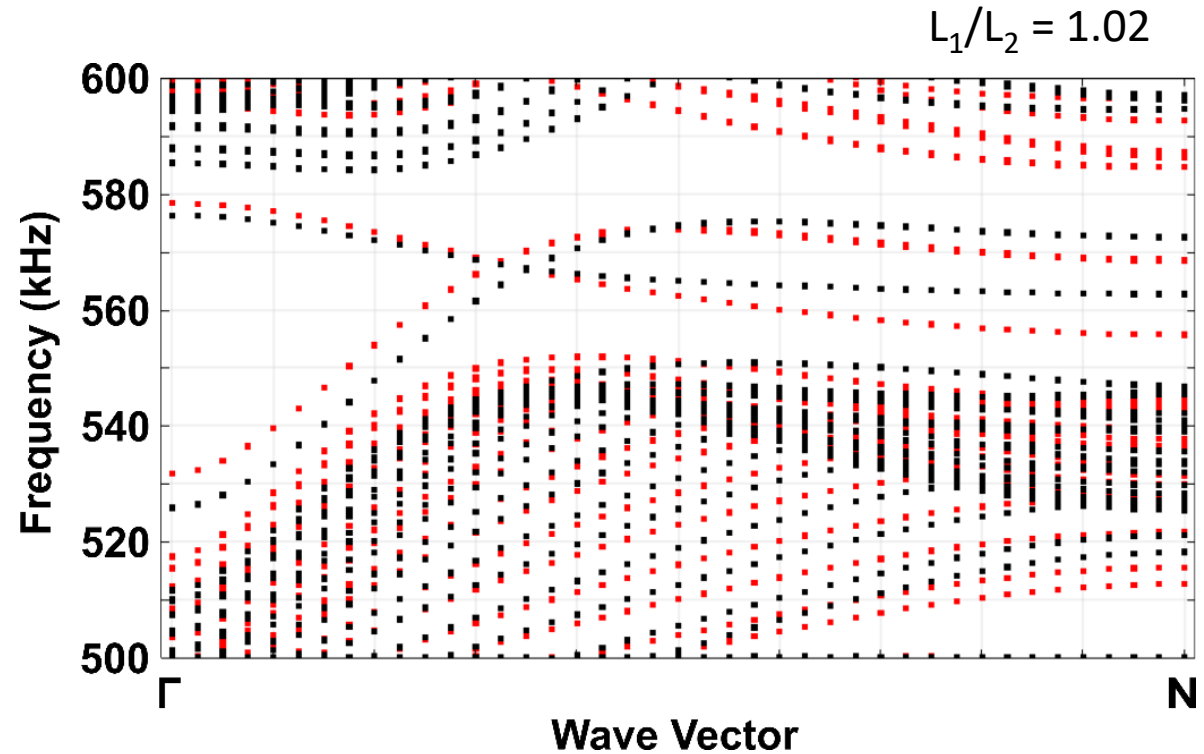
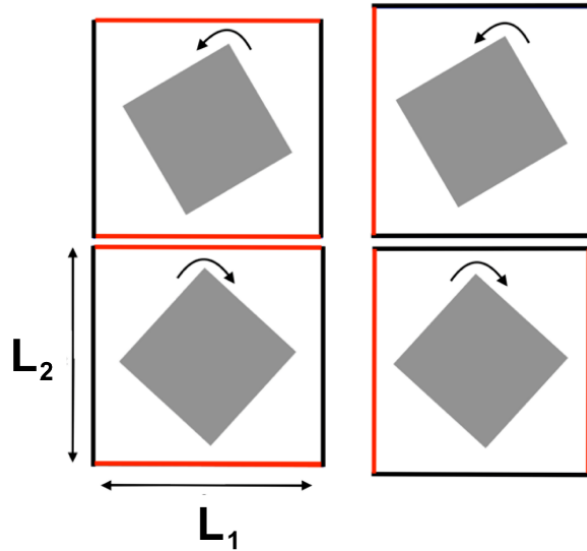


It also results in a slight frequency shift of the main Dirac points
And a slight reduction in band gap width



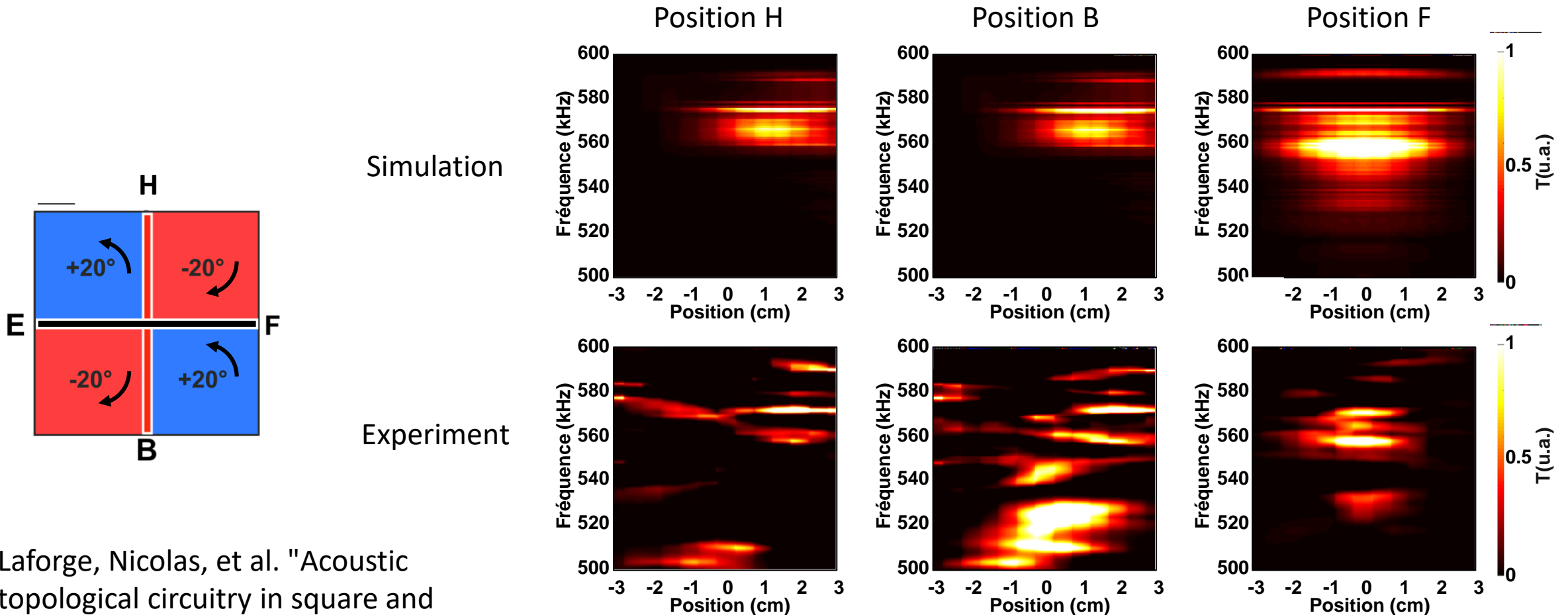
Laforge, Nicolas, et al. "Acoustic topological circuitry in square and rectangular phononic crystals." arXiv preprint arXiv:2012.08014 (2020).

Dispersion of the guided waves shifts



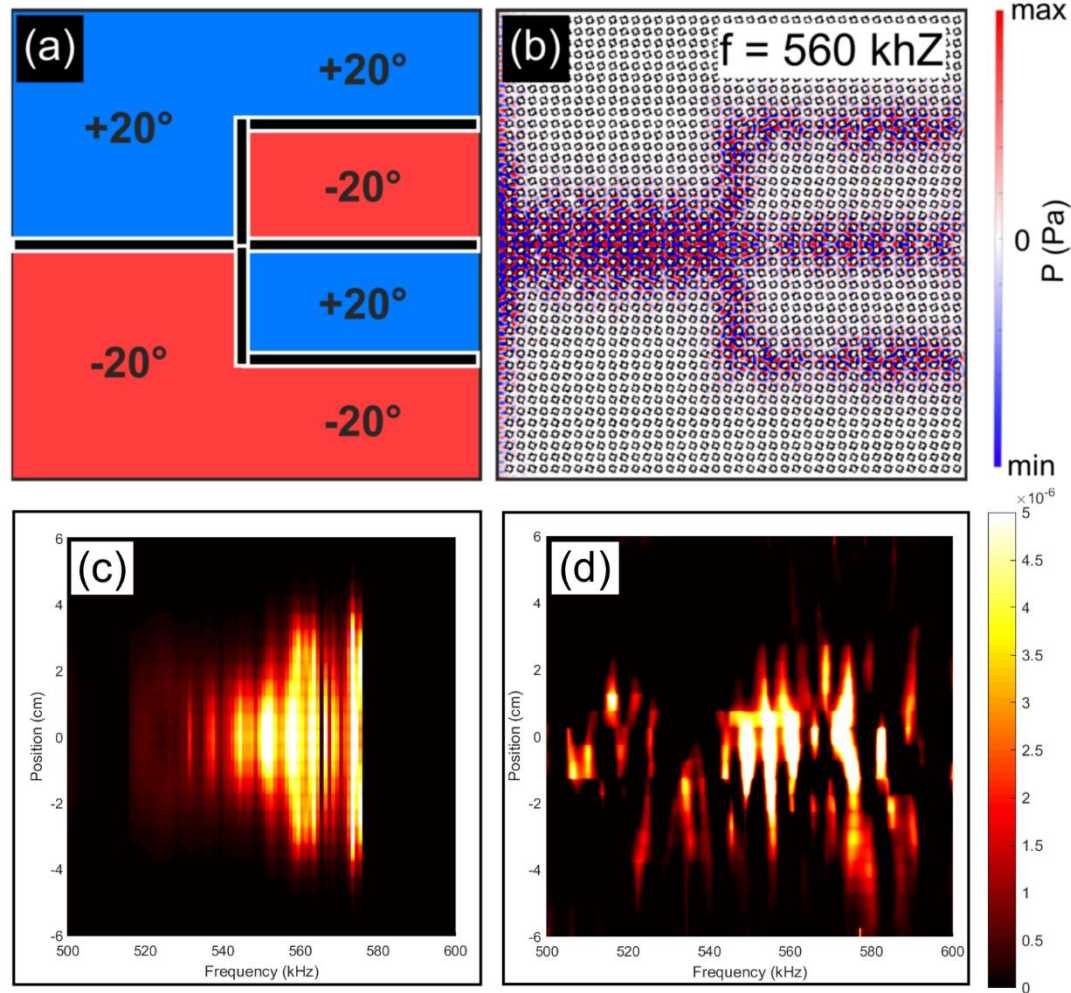
Laforge, Nicolas, et al. "Acoustic topological circuitry in square and rectangular phononic crystals." arXiv preprint arXiv:2012.08014 (2020).

3-way splitter with the rectangular-lattice



Laforge, Nicolas, et al. "Acoustic topological circuitry in square and rectangular phononic crystals." arXiv preprint arXiv:2012.08014 (2020).

And finally, a 'trident' circuit!



Simulation

Experiment

Laforge, Nicolas, et al. "Acoustic topological circuitry in square and rectangular phononic crystals." arXiv preprint arXiv:2012.08014 (2020).

Summary and conclusion

- Dirac points exist not only in the hexagonal (graphene) lattice, but with other symmetries, including the square and the rectangular lattices
- We have implemented topological phononic crystal circuits both with water waves and ultrasonic acoustic waves
- The rotated square inclusion in square-lattice crystal has ‘spurious’ Dirac points that can be removed considering the rectangular lattice
- Square and rectangular lattices are compatible with 3-way splitters and more general phononic circuits

