Planning in-hand dexterous micro-manipulation using 3-D rotations decomposition

Pardeep KUMAR, Redwan DAHMOUCHE, Michaël GAUTHIER

Abstract—This paper aims to contribute to the improvement of dexterity in contact micro-manipulation by performing in-hand dexterous micro-manipulation planning. Previous experimental works on planar micro-manipulation showed that such an approach allows for large rotations of arbitrary shaped objects. Moving from planar to 3-D manipulation significantly increases the complexity of the manipulation planning, especially when considering the rolling of the fingers on the object during the manipulation. We propose in this paper a dexterous manipulation planning algorithm that leverages the complexity of 3-D manipulation planning by decomposing the desired 3-D rotations into three successive rotations within two different planes. Optimal paths of the manipulating fingers are thus obtained in the planar spaces and then combined to form the trajectories in the 3-D space. Besides the relevance of the approach, the simulation results show that exploiting adhesion forces improves the robustness of the manipulation and extends the manipulation capabilities, but at the expense of the computation time.

Index Terms—Micro-manipulation, Manipulation Planning, Dexterity, Grasping, In-hand manipulation.

I. INTRODUCTION

Dexterous manipulation at the macro-scale has been an active research topic in the last three decades [1]–[3]. Different operations like rolling [4], sliding [5], and finger gaiting [6] have been studied to perform in-hand manipulation tasks [7]. The demonstrated capabilities range from simple pick-and-place to more complex tasks, such as in-hand rotation of a cube [8], picking up a coin from the floor [9], opening a bottle cap [10], and many others.

At the micro-scale, manipulation methods are classified into two groups: (i) non-contact manipulation, in which the object trajectory is controlled with a physical field (e.g., electric, magnetic, etc.) and; (ii) contact-based manipulation, where the manipulator is in physical contact with manipulated object, just like the way humans manipulate common objects. This paper focuses on this second category, which is currently limited to basic tasks [11]–[15].

In contact based micro-manipulations, two main types of robot architectures are proposed. The first one consists of a basic tweezer mounted on a precision manipulation robot. Yet, we face hurdles in achieving the desired rotations using this architecture, while achieving translations is usually more trivial. Indeed, the uncertainties and variations of the robot kinematic parameters and the existence of mechanical defects (backlash, out of roundness, etc.) affect the position of the rotation center of the tweezers and introduce undesired motion of the manipulated object [16]. In addition, the entire robot has to rotate in order to manipulate the micro-object, which requires a large space. Unfortunately, such spaces are not available in many applications such as in Scanning Electron Microscope’s chambers or in several medical applications. Such constraints limit the feasibility of this approach.

The second approach in contact micro-manipulation is to use two or more decoupled probes or fingers that have several Degrees of Freedom (DoF). In this approach, the trajectory planning of the fingers is more complex but the manipulation of the objects requires less space since it is done in the manipulating “micro-hand” [17], [18]. However, most of the works that use this approach are limited to simple object shapes like spheres [19]–[21]. Other works consider more complex shapes but the dexterity of the proposed approaches is limited. For instance, two fingers are used in [22] to rotate a Lego-like object but the rotation angles are small since no re-grasp operation is performed. In [23], the manipulated object lays on a substrate (2-D motion) and is pushed by four probes to get to the desired object’s pose. The manipulation is thus limited to a horizontal plane.

Contact micro-manipulation is also made difficult because of surface forces (capillary, van der Waals and electrostatic). Those forces are often dominant over gravitational and inertial forces which make the manipulated objects stick to substrate and the tweezers [24]. For a long time, adhesion forces were seen as disturbing effects that we have to mitigate [25]. However, it was recently shown that such forces can be exploited to improve dexterous micro-manipulation capabilities. Indeed, the adhesion forces allow the fingers to pull the object which enhances the stability of the grasps [26]. In [27], Séon et al. demonstrated that in-hand planar micro-manipulation of arbitrary shaped planar objects can be achieved in presence of adhesion forces. Dexterous manipulations with rotations above 220° for a wide variety of planar objects at the micro-scale were experimentally achieved.

The aim of this work is to enhance the capabilities of manipulating micro-objects with complex shapes in the 3-D space. The main challenge in performing 3-D dexterous manipulation in general, and micro-manipulation in particular, is the complexity of the manipulation planning algorithm.

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that might increase exponentially with the dimension of the configuration space of the object and that of the hand.

In this article, we develop a dexterous 3-D manipulation algorithm with a moderate complexity. The main idea is to perform 3-D dexterous manipulation by using 2-D planners. The proposed approach consists in: i) decomposing 3-D rotations into three individual 2-D rotations; ii) planning the manipulation within the sub-spaces and; iii) combining them to form 3-D manipulation trajectories. The increase in complexity from 2-D manipulation to 3-D is thus moderate (three 2-D paths). The adhesion forces are exploited to stabilize the grasps and the \( A^* \) search algorithm is used to generate optimal paths in the considered sub-spaces.

II. MODELING AND BACKGROUND

A. Grasping Forces

To grasp an object with \( F \) fingers, the fingers must make contact and apply some grasping force on the object’s surface. As proposed in [28], we assume in micro-scale that the contact forces can be modeled using a combination of the Coulomb’s Law in which the friction magnitude is independent of the velocity and contact area, and the pull-off force \( F_{po} \) representing the force required to detach the finger from the object as:

\[
\sqrt{f_x^2 + f_y^2} \leq \mu(f_n + f_{po}), \quad (1)
\]

where \( f_x \) and \( f_y \) are the tangential components of the force on \( X - \)axis and \( Y - \)axis respectively, \( f_n \) is the normal component of force, and \( \mu \) is the friction coefficient.

Due to the presence of the pull-off force \( f_{po} \), it is possible to apply a negative force (pulling the object) in micro-scale since the applied force lies in the modified friction cone, whereas in macro-scale only the positive grasping forces (pushing the object) are possible.

B. Grasping Equilibrium

The manipulated object must be in equilibrium during the whole manipulation process. The equilibrium condition for rigid body is that the sum of all the wrenches should be equal to zero. Whereas, a wrench vector is composed of forces and torques at a contact point as provided by:

\[
w = \begin{bmatrix} f \\ \tau \end{bmatrix} \quad (2)
\]

where \( w \) is a wrench, \( f \) and \( \tau \) represent the force and torque respectively.

Grasp Equilibrium has been discussed in detail in [26], [27], [29]. A grasp using \( F \) fingers is stable if:

\[
\sum_{i=1}^{F} w_i + w_{ext} = 0, \quad (3)
\]

where \( w_i \) is the grasping wrench applied by \( i^{th} \) finger, and \( w_{ext} \) is the external wrench applied to the object.

C. Impact of Pull-off forces on Finger Gaiting

Pull-off force has an important role in re-grasping and finger gaiting (i.e. fingers replacement). When a finger (e.g. the \( F^{th} \) finger) is being detached, it will pull the object with a force corresponding to the pull-off force \( (f_{po}) \). This pull-off force may disturb the grasping equilibrium. Thus, it is necessary for the remaining \( F - 1 \) fingers to compensate for this \( f_{po} \) to maintain the object’s stability. Thus, removing a finger is possible only if the following equation is satisfied:

\[
\sum_{i=1}^{F-1} w_i + w_{ext} + w_{po} = 0, \quad (4)
\]

where \( w_{po} \) is the pull-off wrench caused by releasing the \( F^{th} \) finger.

III. PROBLEM FORMALIZATION

In order to perform fingers path planning, we assume that the object’s shape is known through its Computer-Aided Design model (CAD model). Considering the small size of the manipulated object, we also assume that the fingers movement range is significantly larger than the object’s dimensions. We also consider only two and three fingers grasps. The admissible contact points on the object that can be used to grasp it are obtained by sampling the object’s surface. We then compute the set of all stable grasps, called Maps (M), as well as all the admissible finger gaiting configurations (3 to 2 fingers grasps that can resist a finger detachment). Therefore, there are three different sets of maps: i) initial grasp for which the object can be detached from the substrate (\( M_{IG} \)); ii) object translation and rotation while the fingers roll on the object without sliding (\( M_{RG} \)); iii) reconfiguration where the number of fingers used for a grasp changes (\( M_{RC} \)).

To generate finger trajectories, the maps are converted to Graph (\( G \)), where each stable grasp is connected to its subsequent stable grasp(s). Each element of graph is considered as a Node (\( n \)) which are connected by Edges (\( e \)). Finding an optimal finger trajectory to rotate an object consists in finding a path in the Graph (\( G \)). This step can be performed using a graph search algorithm. Since, a node is an outcome of links of stable grasp configuration of manipulated object, which is based on contact points, fingers, and object orientation; thus, it is possible to represented a node by four parameters i.e. \( n = [i j k l] \) where \( i \), \( j \), and \( k \) define the indexes of contact points on object of the first, second and third fingers respectively, and \( l \) defines the index of angular position of the object.

For finger path planning, we are using \( A^* \) algorithm whose time complexity is \( O(b^d) \) where \( d \) is the depth (number of nodes to reach the goal) and \( b \) is the branching factor (average number of branches per node). There are two cases for branching factor, one is when two fingers are in use, and the second is when three fingers are used. For first case when two fingers are already in contact with object, the branching factor is sum of operations: clockwise rotation, counter clockwise rotation and addition of third finger over
the remaining \( c - 2 \) contact points. Whereas for the second case when three fingers are in use, the branching factor is sum of operations: clockwise rotation, counter clockwise rotation, and detaching one of the finger.

A. Reducing the complexity using Euler’s angle

Beside the complexity of search algorithm, the major issue to deal with is the number of grasping possibilities (\( gp \)), which is the result of the number of contact points (\( c \)) of an object, the numbers of fingers (\( F \)) being used to grasp the object, and the possible angular positions/orientations (\( l_a \)) of object (i.e. one turn of rotation (360°) divided by constant rotational step \( \Delta \theta \)).

In planar manipulation, where we consider to manipulate an object in a single plane, the number of grasping possibilities is computed as:

\[
gp^{2D} = c^F \cdot l_b ,
\]

(5)

Whereas, to manipulate an object in spatial case (\( S \)), we imagine \( P \) numbers of planes over which the contact points are generated. In this case, the number of grasping possibilities is computed as:

\[
gp^{2D} = (P \cdot c)^F \cdot l_b = P^F \cdot gp^{2D}
\]

(6)

This increase in the number of grasping possibilities, exponentially increases the complexity of search algorithm.

One of the challenges in 3-D manipulation is to reduce the number of grasping possibilities and search algorithm complexity. According to Euler’s Angles, it is possible to decompose any 3-D rotation into three individual 2-D rotations along any two orthogonal axes [30]. Thus keeping that in mind, we propose to only retain two orthogonal planes \( P_1 \) at \( XY - axis \) and \( P_2 \) at \( XZ - axis \) intersecting the object over lines \( L_1 \) and \( L_2 \) as illustrated in Fig. 1. Since, the three individual 2-D rotations will be carried out in two different planes, we consider the two intersecting points \( I \) and \( J \) of lines \( L_1 \) and \( L_2 \) as a common link for these three individual rotations. The three individual rotations will be carried out as: \( R(z, \theta_1) \) over \( P_1 \), \( R(y, \theta_2) \) over \( P_2 \), and \( R(z, \theta_3) \) over \( P_1 \) respectively as represented in Fig. 2, which will reduce this number of grasping possibilities to sum of grasping possibilities of each rotation carried out over these two planes as:

\[
gp^{3D} = 2 \cdot gp^{2D_{1}} + gp^{2D_{2}}.
\]

(7)

The reduction of complexity introduced by two planes also reduces the genericity of our approach. Indeed the considered objects should have a geometry in which both planes \( P_1 \) and \( P_2 \) can be defined.

B. Sampling strategy

As we consider that the object’s CAD model is known, we sample the manipulation lines \( L_1 \) and \( L_2 \) to generate contact points (\( c \)) for grasping. We consider the curvilinear abscissa as the coordinates for each contact point on the object. Whereas, for sampling on the object we considering that the rolling between two successive sample points corresponds to a constant rotation \( \Delta \theta \) of the object.

IV. IN-HAND MANIPULATION STRATEGY

Given the number of fingers, and object geometry, the finger trajectory generation is accomplished using two steps. The first is to compute the stable grasps and generate the Graph (\( G \)), while the second step is to define a path by traversing the graph(s) to achieve the desired configuration.

Since, the object modeling is restricted only to two planes \( P_1 \) and \( P_2 \), and intersecting contact points \( I \) and \( J \) being the only common link induces some constraints for successive rotations. These constraints are:

- The first rotation should end at the intersecting points \( I \) and \( J \).
- The second rotation should start from these intersecting points \( I \) and \( J \), and end at the same intersecting points.
- The third rotation should start from these intersecting points \( I \) and \( J \).

In previous work, Seon et al. [26], [27], [29] achieved only desired pose of object for planar manipulation, while to manipulate the object in 3-D we need to comply with these constraints. Thus, we propose an original method to provide finger trajectories using \( A^* \) algorithm.
The $A^*$ algorithm uses a heuristic for traversing the graph(s), while ensuring that it computes a path with minimum cost through the nodes $n$. The algorithm optimizes the function $f(n)$, which consists of the cost function $g(n)$ and heuristic function $h(n)$ as:

$$f(n) = g(n) + h(n).$$

(8)

A. Cost Function $g(n)$

Cost function is used to characterize the distance between two nodes. There are three cases for cost function $g(n)$: i) initial node cost $g(n_i)$ i.e. when fingers grasp the object for first time, ii) when current node $n$ is reached using finger rolling on object $g(n)^{\text{rolling}}$, iii) when current node $n$ is reached using finger gaiting $g(n)^{\text{gaiting}}$.

Initial node cost $g(n_i)$, is the distance between fingers’ initial position, and first contact points on object for grasp. When the node $n$ is reached using finger rolling (i.e. without reconfiguration), the cost can be defined as the sum of rolling distance $d_{Fi}$ which is the curvilinear abscissa between two contact points covered by each finger $F_i$, and previous cost $g(n_{\text{previous}})$ as:

$$g(n)^{\text{rolling}} = 3 \sum_{i=1}^{3} d_{Fi}^{\text{roll}} + g(n_{\text{previous}}).$$

(9)

Whereas when the node $n$ is reached using a finger reconfiguration (i.e. finger attachment or detachment), the cost $g(n)^{\text{gaiting}}$ will be:

$$g(n)^{\text{gaiting}} = g_r + g(n_{\text{previous}}),$$

(10)

where $g_r$ is a constant and estimated as the minimal distance applied by the actuator to guarantee that the finger is detached. In our case, we choose the value of $g_r$ as three times the finger radius.

B. Heuristic Function $h(n)$

In search algorithms, heuristic function $h(n)$ estimates the minimum cost (in terms of distance for our case) from current node $n$ to the goal node $n_g$. As it is important to develop a good heuristic function that guarantees the shortest path; for which the heuristic must underestimates the actual cost. Since, a node is dependent on contact points, fingers being used, and angular position of object, thus we take these parameters into account to formalize our heuristic as:

$$h(n) = \sum_{i=1}^{3} d_{Fi}^{\text{roll}} + h_r(p),$$

(11)

where $d_{Fi}^{\text{roll}}$ is the estimated rolling distance covered by finger $F_i$ from current node $n$ to goal node $n_g$, and $h_r$ is the heuristic for reconfiguration, function of parameter $p$:

$$p = \sqrt{(l+l-i_g-l_g)^2 + (j+l-j_g-l_g)^2 + (k+l-k_g-l_g)^2}$$

(12)

where current node is $n = [i j k l]$ and target node is $n_g = [l_g f_k k_g l_g]$.

Parameter $p$ checks whether a path between current node $n$ and goal node $n_g$ without any reconfiguration exists or not. If such path exists then $p$ will always be zero which will result in $h_r(p)$ being zero as well. Otherwise, to reach the goal node $n_g$ we will need at least one reconfiguration, and the value of $h_r(p)$ in such case will be three times the finger radius.

V. RESULTS

The proposed methodology presented in the previous sections, has been simulated and implemented to generate the finger trajectories for three objects with different curvatures in 3-D space i.e. Ellipsoid, Convex shaped object, and Concave shaped object provided in Fig. 3, using three spherical fingers having diameter of 10μm each. For the simulations, we have considered the physical properties of silicon for all fingers and objects, a pull-off force of 1.5 μN [31], and a friction coefficient of 0.3.

As described in section IV, we propose to decompose the movement in 3 successive rotations as: $R(z,\theta_1)$ over $XY$–plane $\mathcal{P}_1$, $R(y,\theta_2)$ over $XZ$–plane $\mathcal{P}_2$, and $R(z,\theta_3)$ over $XY$–plane $\mathcal{P}_3$ respectively.

Fig. 3: Different objects a) Ellipsoid, b) Convex Shaped Object, and c) Concave Shaped Object, each with isometric, and 2-D top and side views; used for in-hand dexterous manipulation in 3-D space.

A. Characteristics of the graph $G$

The Table I represents the total number of nodes for finger path generation against number of contact points over manipulation lines $L_1$ and $L_2$ when adhesion forces are not present. The difference in number of nodes generated is 2 - 4 times higher when adhesion forces are available in comparison to when there is no adhesion force. Indeed, when
there is adhesion, the object is more stable and a higher number of grasping is stable.

TABLE I: Simulated numerical data for both (i) considering adhesion with a pull-off force of 1.5 µN and (ii) without adhesion. Finger diameter is 10µm, friction coefficient (µ) is 0.3, and rotational step (Δθ) is 10°.

<table>
<thead>
<tr>
<th>Object</th>
<th>Number of contact points c (L1, L2)</th>
<th>Number of nodes in the generated graph (in millions)</th>
<th>With Adhesion</th>
<th>Without Adhesion</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ellipsoid</td>
<td>362, 362</td>
<td>337.8, 337.8</td>
<td>110.7, 110.7</td>
<td>46.2, 228.5</td>
</tr>
<tr>
<td>Convex</td>
<td>288, 302</td>
<td>530.1, 595</td>
<td>268.8, 228.5</td>
<td></td>
</tr>
<tr>
<td>Concave</td>
<td>440, 302</td>
<td>1817.4, 595</td>
<td>416.2, 228.5</td>
<td></td>
</tr>
</tbody>
</table>

B. Example of finger trajectory

Fig. 4 - 6 represent an example of the optimal finger path to perform three successive optimal rotations (respectively 40°, 70°, 20°) of Concave Shaped Object. The object is expended on Z-Axis, which is the case for most of the objects at micro-scale built using clean-rooms micro-fabrication methods. We show that the proposed method enables to determine a finger path planning to rotate the micro-object in 3-D space.

C. Performance of the path planning

In order to illustrate the performance of our proposed methods, we determined several optimal finger paths considering the objects presented in Fig. 3. In all the cases, we have considered two possibilities: with adhesion.

Fig. 4: Concave Shaped Object (2-D top view of XY plane): Sequence of first rotation of 40° along XY plane/z-axis; (a) initial grasp of object (b)-(c) rotation of 40° with rotational step of 10°.

Fig. 5: Concave Shaped Object (2-D side view XZ plane): Sequence of second rotation of 70° along XZ plane/y-axis; (a) position of fingers on the intersection points (I, J) (sec. III), (b) rotation of rotation of 10°, (c)-(f) reconfiguration of finger composing of finger detachment and finger addition, (g)-(h) rotation of 20°, (i)-(j) finger detachment to go back to its reference position, (k)-(n) rotation of 40°.

Fig. 6: Concave Shaped Object (2-D top view XY plane): Sequence of third rotation for 20° along XY plane/z-axis; (a) last pose from 2nd rotation, (b)-(c) rotation of 20°.
and without adhesion to evaluate the impact of adhesion on fingers paths. Various large rotations: for ellipsoid object (40°, 30°, 50°), (40°, 140°, 70°), (130°, 150°, 90°), (90°, 120°, 140°), for convex shaped object (40°, 70°, 30°), (40°, 140°, 80°), (90°, 160°, 30°), (80°, 90°, 30°), and for concave shaped object (50°, 140°, 30°), (40°, 70°, 20°), (40°, 90°, 20°), (60°, 150°, 30°) have been carried out. The rotations with (†) represent particular cases where the desired rotation cannot be reached due to the instability of object in the absence of adhesive forces. Indeed, some of the rotations are not accessible without adhesion. It comes from the fact that the graph G is smaller without adhesion.

The technical data of three simulations are described in Table II. With adhesion forces, the reconfigurations are required only for the 2nd rotations, while in the case of without adhesion forces (60°, 150°, 30° for concave shaped object), the other rotations (1st or 3rd) may require reconfiguration(s). The average time to generate: the finger path of 1st rotation for all various object is around 50 seconds (with adhesion) and 1 second (without adhesion), the finger path of 2nd rotation is 3 seconds (with adhesion) and 4 seconds (without adhesion), and the finger path of 3rd rotation for all objects is 1 second in both cases with and without adhesion. The time taken to generate the finger path of 1st rotations(s) is higher due to the initial grasping possibilities from fingers’ reference position (off-contact) to initial nodes on object (on-contact).

### VI. Conclusion

We proposed in this paper a new method to perform finger path planning for 3-D dexterous manipulation of micro-objects. To leverage the complexity of 3-D dexterous micro-manipulation, we proposed to perform three planar rotations about two perpendicular axes. To ensure the continuity of the manipulation process over the three rotations, we proposed an algorithm that is able to rotate the manipulated object over three successive angles while starting and/or ending the rotations with predefined fingers positions on the object. The simulation results showed that most trajectories are generated within few seconds. Exploiting adhesion forces enables more feasible trajectories with a lower number of reconfigurations but at the expense of a higher number of nodes (stable grasps) and a longer calculation time. The focus for our future work will be on the fingers collision avoidance and the experimental validation of the proposed method.

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### REFERENCES


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<table>
<thead>
<tr>
<th>Object</th>
<th>Rotations</th>
<th>Number of nodes in:</th>
<th>Number of required reconfiguration(s)</th>
<th>Time to generate path (sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ellipsoid</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>θ₁ = 40°</td>
<td>147,612</td>
<td>5 6,528 5 0</td>
<td>0</td>
<td>45 &lt; 1</td>
</tr>
<tr>
<td>θ₂ = 140°</td>
<td>2,536</td>
<td>19 1,689 19 4</td>
<td>4</td>
<td>5 4</td>
</tr>
<tr>
<td>θ₃ = 70°</td>
<td>946</td>
<td>6 946 6 0</td>
<td>0</td>
<td>&lt; 1 &lt; 1</td>
</tr>
<tr>
<td>Convex</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>θ₁ = 80°</td>
<td>143,824</td>
<td>9 8,696 8 0</td>
<td>0</td>
<td>48 1</td>
</tr>
<tr>
<td>θ₂ = 90°</td>
<td>650</td>
<td>14 930 16 4</td>
<td>6</td>
<td>2 3</td>
</tr>
<tr>
<td>θ₃ = 30°</td>
<td>682</td>
<td>4 682 4 1</td>
<td>0</td>
<td>&lt; 1 &lt; 1</td>
</tr>
<tr>
<td>Concave</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>θ₁ = 40°</td>
<td>224,458</td>
<td>5 6,958 5 0</td>
<td>0</td>
<td>63 &lt; 1</td>
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<td>θ₂ = 90°</td>
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<td>6</td>
<td>2 3</td>
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