

# Remaining useful life prognostic-based energy management strategy for multi-fuel cell stack systems in automotive applications

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## Abstract

To achieve the 8,000-hour proton exchange membrane fuel cell stack (PEM FCS) life target set by the U.S DoE and promote fuel cell hybrid electric vehicles (FCHEVs) massive introduction in the automotive market, using multi-fuel cell stack (MFCS) systems instead of single-fuel cell stack systems seems to be an interesting solution that deserves to be explored. MFCS systems' concept combines several small FCSs modules instead of using a single high-powered FCS module. The modularity in such systems can be exploited through energy management to improve their durability and extend their good energy-efficiency power range. However, FCSs' multiplicity makes it challenging to implement effective energy management strategies (EMSs). This paper proposes a remaining useful life (RUL) prognostic-based EMS to extend MFCS systems' lifetime while keeping their hydrogen consumption reasonable. For this purpose, a prognostic algorithm is developed to predict PEM FCSs' RUL in real-world automotive application scenarios. Then a rule-based EMS allocates the demand between stacks using prognostic results. The proposed strategy's performance is evaluated on a hybrid MFCS/ battery system using Matlab/ Simulink's environment. Simulation results show that implementing the proposed strategy instead of conventional EMSs can extend MFCS systems' lifetime by at least a factor of 2.35 while keeping their hydrogen consumption reasonable. © 2001 Elsevier Science. All rights reserved.

*Keywords:* Multi-fuel cell stack systems; Remaining useful life; Prognostic; Energy management strategy; Fuel cell hybrid electric vehicle

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## 1. Introduction

Using hydrogen through PEM FCSs as vehicle power sources is a promising solution to decarbonize transportation [1, 2]. However, their low durability is a significant issue that hinders FCHEVs promotion [3, 4]. According to the U.S. Department of Energy (U.S. DoE), PEM FCSs' lifetime, currently about 5,000 hours, must be increased to at least 8,000 hours to promote FCHEVs massive introduction in the automotive market [5, 6]. From this point of view, adopting the MFCS

systems concept appears to be an attractive solution. It should be noted that MFCS systems have already been used in marine transport and aeronautics with the U212A-class Todaro [7] and the four-seat H4Y aircraft [8] for example. In fact, due to their high modularity, MFCS systems could offer more degrees of freedom to EMSs to make energy management decisions that can extend their lifetime, reduce their hydrogen consumption, and improve their reliability [9-11].

MFCS systems concept advantages could even go beyond these three criteria, by addressing the question of cost from economies of scale's angle.

The proof-of-concept of MFCS systems concerning the four criteria (durability, energy efficiency, reliability, and cost) mentioned before involves the implementation of efficient EMSs. Consequently, energy management is the most addressed issue in the literature regarding MFCS systems. MFCS systems' EMSs that are proposed in the literature can be divided into two categories: rule-based EMSs and optimization-based EMSs. An optimization-based EMS and a rule-based EMS are respectively proposed for MFCS systems in [12] and [13] to improve the conventional Daisy-Chain strategy. Both strategies were found capable of reducing MFCS systems' hydrogen consumption respectively by 9.42 % and 7% compared to the basic Daisy-Chain EMS. However, the MFCS systems' lifetime has not been evaluated, so it cannot be concluded whether these strategies improve MFCS systems' durability or not. Several other Rule-based EMSs [14, 15] and optimization-based EMSs [16-20] are designed to reduce MFCS systems' hydrogen consumption while durability consideration is suggested as a potential future work. Even in research papers where FCSs' degradation is considered in MFCS systems energy management such as [21-26], the lifetime improvement is not quantified.

The review of MFCS systems' EMSs highlights the ability of most strategies to optimize MFCS systems' hydrogen consumption. Furthermore, it shows that the literature lacks EMSs that are likely to enhance MFCS systems' lifetime. Therefore, this paper aims to contribute to addressing this issue by proposing a health-conscious EMS for improving MFCS systems' durability.

FCS and MFCS systems' health-conscious EMSs can be divided into two categories: diagnostic-based EMSs and prognostic-based EMSs.

Prognostic-based EMSs are part of the Prognostic and Health Management (PHM) discipline [27], which consists of 7 modules: data acquisition, data processing, condition assessment, diagnostics, prognostics, decision-making, and human-machine interface. A detailed description of each one of these modules can be found in [28]. Prognostic-based EMSs are complementary to diagnostic-based EMSs [29-32], as they have more available information like FCSs' remaining useful life (RUL) for decision-making even if no operating anomalies are detected. This allows them to adjust energy management rules before faults occur, making them more efficient than diagnostic-based EMSs. FCSs' RULs are predicted by prognostic algorithms, which can be implemented using different approaches: the model-based approach [33, 34], the data-driven approach [35-39], the hybrid approach [40, 41], or the experience-based approach [42].

It should be acknowledged that a great deal of progress has already been made in terms of prognostic methods to help energy management decision-making for FCS or MFCS systems. Two RUL prognostic-based EMSs were proposed in [6, 43] for a range-extender FCHEV. In [44], an end-of-life prognostic-based EMS was applied to an MFCS system made up of three PEM FCSs. By solving a multi-objective optimization problem, this strategy extended the MFCS system's lifetime by around 25% compared to the Daisy-Chain strategy, without increasing its hydrogen consumption.

Several other researchers in [45-47], found that RULs prognostic-based EMSs have the potential to significantly enhance FCS or MFCS systems' durability. However, despite the abundance of prognostic methods in the literature, the number of proposed prognostic-based EMSs is very limited. This discrepancy can be attributed to the fact that integrating FCS prognostic methods into energy management requires additional research, as these two fields of expertise are distinct. Prognostic involves signal processing and data analysis skills, while energy management demands expertise in systems engineering. This paper proposes an EMS for MFCS systems based on RUL prognostic, combining the strengths of these two fields of expertise to enhance such systems' durability.

The present paper will be structured as follows: a PEM FCS aging model will be established in section 2 based on various researchers' FCS modeling works. In Section 3, an ANN-based FCS prognostic algorithm will be proposed for real-world use in automotive applications to investigate the prognostic-based energy management concept under a real vehicle use scenario. An MFCS system RUL prognostic-based EMS will be suggested in section 4. The strategy will be applied to a hybrid MFCS system/ battery in section 5 and the simulation results will be presented and compared to two conventional EMSs' results. In section 6, the proposed EMS will be compared with a state of health (SOH) estimation-based EMS, which appears as the reference EMS in this study regarding the applied energy management principle.

## 2. PEM FCS model with aging consideration

In this paper, the PEM FCS model is established based on previous modeling works that have been suggested in the literature for energy management purposes.

### 2.1. PEM FCS static and dynamic models

- PEM FCS static model:

The static model is based on the polarization equation of an N-cell PEM FCS.

$$\begin{aligned}
V(i_{FC}, T_{FCS}, P_{O_2}, P_{H_2}) & \quad (1) \\
&= N[E_{rev}(T_{FC}, P_{O_2}, P_{H_2}) \\
&\quad - \Delta E_{act}(i_{FC}, T_{FC}) \\
&\quad - \Delta E_{conc}(i_{FC}, T_{FC}) \\
&\quad - \Delta E_{ohm}(i_{FC})]
\end{aligned}$$

$$\begin{aligned}
E_{rev}(T_{FC}, P_{O_2}, P_{H_2}) & \quad (2) \\
&= \frac{T_{FC} \cdot \Delta S - \Delta H}{2F} \\
&\quad + \frac{R \cdot T_{FC}}{2F} \ln \left( \frac{P_{H_2} \cdot P_{O_2}^{\frac{1}{2}}}{P_{O_2}^{\frac{3}{2}}} \right)
\end{aligned}$$

$$\Delta E_{act}(i_{FC}, T_{FC}) = A \cdot T_{FC} \ln \left( \frac{i_{FC} + i_n}{i_0} \right) \quad (3)$$

$$\Delta E_{conc}(i_{FC}, T_{FC}) = -B \cdot T_{FC} \ln \left( 1 - \frac{i_{FC}}{i_l} \right) \quad (4)$$

$$\Delta E_{ohm}(i_{FC}) = R_{FC} \cdot i_{FC} \quad (5)$$

Where  $i_{FC}$  is the FCS current density;  $V$  represents the stationary part of the FCS output voltage;  $E_{rev}$  is the reversible Nernst potential;  $\Delta E_{act}$ ,  $\Delta E_{conc}$ , and  $\Delta E_{ohm}$  symbolize activation losses, concentration losses and ohmic losses respectively.  $T_{FC}$  is the operating temperature of the FCS;  $P_{O_2}$  and  $P_{H_2}$  are oxygen partial pressure and hydrogen partial pressure respectively.  $\Delta S$  denotes the entropy variation while  $\Delta H$  stands for the energy released by the reaction taking place in the FCS.  $R$  and  $F$  are respectively the gas constant and the Faraday constant.

- PEM FCS dynamic model:

In PEM FCS, during power variations, the temperature transient is the slowest physical phenomenon to occur before stabilization in the steady state. As a result, this study will only focus on thermal dynamics modeling.

The slow dynamics effects of thermal phenomena on the FCS voltage can be seen as an additional voltage  $N \cdot V_{dyn}(t)$  which is characterized by a transient and steady state [48]. The FCS output voltage  $V_{FCS}(t)$  can then be written as follows:

$$V_{FCS}(t) = V + N \cdot V_{dyn}(t) \quad (6)$$

Where:

$$\frac{i_{FC}(t)}{\tau_{dyn}} = \frac{dV_{dyn}(t)}{dt} + \frac{V_{dyn}(t)}{\tau_{dyn}} \quad (7)$$

To approximate a real PEM FCS system dynamic, the time constant  $\tau_{dyn}$  will be set so that the steady state of the output voltage should be established after 300 seconds. Thus, to preserve FCSs' SOH in transport applications, it is important to filter the mission profile's

dynamics. In this case, using a power source such as a battery to hybridize the FCS or the MFCS system is necessary.

- Battery and DC-DC converter models for PEM FCS systems

An empirical battery model (Fig.1) that includes an open-circuit voltage source  $V_0$  connected in series with a resistance  $R_{sbat}$ , and a parallel circuit consisting of a resistance  $R_{cbat}$ , and a capacitance  $C_{cbat}$  is adopted in this paper. The values of these parameters can be estimated experimentally on the real battery that will be chosen after system sizing.

From the equivalent electrical circuit illustrated in Fig.1, the current of the battery,  $i_{bat}$ , can be expressed by the equation (8).

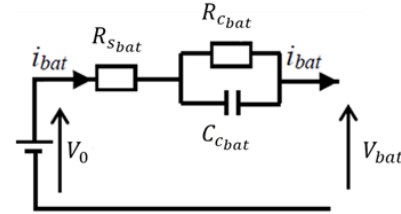


Fig. 1. Battery model

$$\begin{aligned}
i_{bat} &= \frac{V_0 - R_{sbat} i_{bat} - V_{bat}}{R_{cbat}} \quad (8) \\
&\quad + C_{cbat} \frac{d}{dt} (V_0 - R_{sbat} i_{bat} \\
&\quad - V_{bat})
\end{aligned}$$

Equation (9) can be used to calculate the instantaneous state of charge  $SOC_{bat}(t)$  of the battery given its initial state of charge  $SOC_{bat_{init}}$ , capacity  $Q_{bat}$ , and current  $i_{bat}$ . The initial state of charge  $SOC_{bat_{init}}$  will be set arbitrarily before starting each simulation in this study.

$$SOC_{bat}(t) = SOC_{bat_{init}} - \frac{100}{3600 Q_{bat}} \int i_{bat} dt \quad (9)$$

As the study focuses on FCS aging, battery aging is neglected due to the longer lifetime of batteries compared to FCS (over 45,000 hours vs. approx. 5,000 hours). Therefore, battery degradation will not be modelled. However, a boost DC-DC converter model is necessary to increase FCSs' output voltage before connecting them to the DC bus and to regulate their current.

If  $L_{boost}$  and  $V_{boost}$  represent the smoothing inductor and the converter output voltage, respectively, the current  $i_{L_{boost}}$  flowing through the inductor can be obtained by the equation (10), neglecting the effect of the inductor's internal resistance.

$$i_{L_{boost}} = \frac{1}{L_{boost}} \int (V_{bat} - V_{boost}) dt \quad (10)$$

Where the converter's output voltage  $V_{boost}$  and output current  $I_{boost}$  depend on its modulation ratio  $\alpha_{boost}$  and efficiency  $\eta_{boost}$  (equation (11)).

$$\begin{cases} V_{boost} = \alpha_{boost} V_{bat} \\ I_{boost} = \alpha_{boost} I_{PAC} \eta_{boost} \end{cases} \quad (11)$$

## 2.2. PEM FCS cycling aging model

PEM FCS degradation can be caused by several factors such as the frequency or the number of start-stop cycles  $N_{switch}(t)$ , operating power point  $P_{FCS}(t)$ , and mission profile dynamics  $\frac{dP(t)}{dt}$  [49]. Developing and assessing a degradation model  $\Delta_{FCS}(t)$  that considers these main FCS's aging factors could be a good approach to simulate FCS aging due to cycling. Where appropriate, the obtained degradation term can be applied to the FCS's maximum performance to reproduce its power loss as it degrades. Fig.2 illustrates this process.

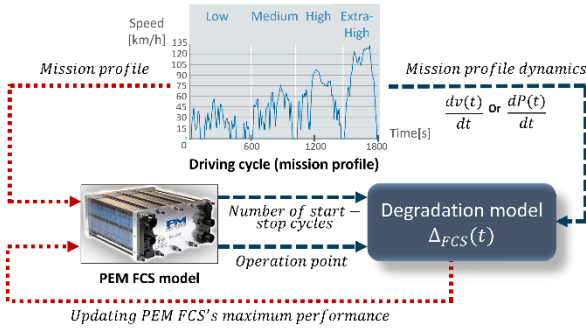


Fig. 2. Cycling aging integration approach into PEM FCS model.

In this study, the FCS degradation model is inspired by the one suggested in [50], which considers the impact of both the number of start-stop cycles and the operating point. The profile dynamics degradation impact on the FCS's SOH is not modelled in this study as the MFCS system will be hybridized by a battery to filter the profile dynamics.

The degradation term will be applied to the electrochemical active surface area  $ECSA_{FCS}(t)$  to update the FCS's maximum performance. In fact, the decrease in ECSA often represents the direct cause of FCS power loss as it ages. As shown by equation (12), the ultimate ECSA  $ECSA_{FCS\_deg}(t)$  can be expressed as a function of the degradation term  $\Delta_{FCS}(t)$  and the  $ECSA_{FCS}(t)$ , which only changes due to normal degradation of the catalyst layer.

$$ECSA_{FCS\_deg}(t) = [1 - \Delta_{FCS}(t)] \cdot ECSA_{FCS}(t) \quad (12)$$

$$\Delta_{FCS}(t) = \int_0^t \delta(t) dt + N_{switch}(t) \cdot \Delta_{switch} \quad (13)$$

$$\delta(t) = \frac{\delta_0}{3600} \left[ 1 + \frac{\alpha}{P_{FCSnom}^2} (P_{FCS}(t) - P_{FCSnom})^2 \right] \quad (14)$$

Where:

$$P_{FCSnom} = \begin{cases} 25\%P_{FCSmax} & \text{si } P_{FCS}(t) < 25\%P_{FCSmax} \\ P_{FCS}(t) & \text{si } 25\%P_{FCSmax} \leq P_{FCS}(t) \leq 95\%P_{FCSmax} \\ 95\%P_{FCSmax} & \text{si } P_{FCS}(t) > 95\%P_{FCSmax} \end{cases} \quad (15)$$

$\delta(t)$  denotes the degradation rate related to the FCS operating point. In this study,  $[25\%P_{FCSmax}; 95\%P_{FCSmax}]$  will be considered as FCSs' safe power range [51, 52], i.e. the power range corresponding to the lowest degradation rate ( $\delta(t) = \frac{\delta_0}{3600}$ ), as it delimits approximately the ohmic losses region. In fact, using FCS in the ohmic losses region can prevent it from the activation and concentration phenomena that accelerate aging. If the FCS operates at low current densities, which means the operating point is close to OCV, it may experience activation losses. The degradation rate  $\delta(t)$  is determined by the relative difference between the FCS output power and the nearest safe power which is  $25\%P_{FCSmax}$ . Similarly, if the FCS delivers power very close to its maximum power  $P_{FCSmax}$ , it is subject to concentration losses. The degradation  $\delta(t)$  rate is determined by the relative difference between the FCS output power and the nearest safe power which is  $95\%P_{FCSmax}$  in this case.

$\Delta_{switch}$  is the degradation caused by a single start-stop cycle, while  $N_{switch}(t)$  denotes the total number of start-stop cycles that the FCS has undergone since its first use.  $\delta_0$ ,  $\alpha$ , and  $\Delta_{switch}$  are empirical parameters. Polarization tests will be conducted during simulations every 200 hours to assess FCSs' SOH considering their slow aging process. The maximum power  $P_{FCSmax}$  will be considered as FCSs' health indicator in this paper, since the output voltage may not be reliable in dynamic current profile applications. Furthermore,  $P_{FCSmax}$  estimation will help determining FCSs' safe power range, which is defined regarding their maximum power (equation (15)).

By estimating the maximum power regularly, its future temporal evolution can be predicted over a specified prediction horizon for FCSs' RUL estimation.

## 3. ANN-based prognostic algorithm for FCSs real-world use in automotive applications

As shown in Fig.3, the data-driven approach makes a good trade-off between the precision, complexity, and applicability. Therefore, it will be adopted for FCSs' SOH prediction and RUL estimation in this study.

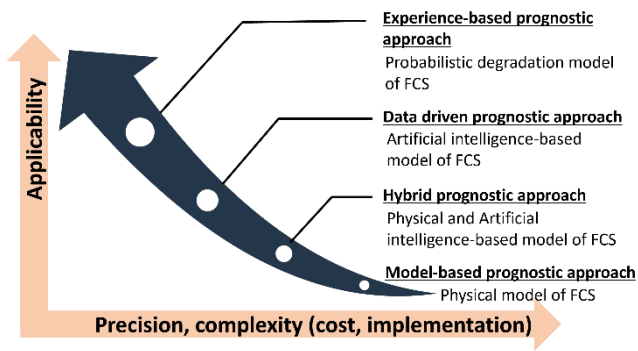


Fig. 3. Prognostic approaches classification according to precision, complexity, and applicability criteria.

### 3.1. Backpropagation neural network-based prognostic algorithm for FCSs real world use in automotive applications

As shown in Fig.4, the basic architecture of a backpropagation neural network (BPNN), typically comprises an input layer, one or more hidden layers, and an output layer.

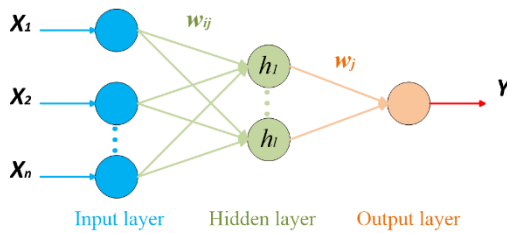


Fig. 4. Basic architecture of the BPNN

BPNN has been used in previous studies, such as in [35, 53], to develop prognostic algorithms for FCS RUL estimation. However, like most data-driven RUL prognostic methods, these algorithms are implemented and tested with the assumption that, the future operating conditions  $\{X_2, X_3, \dots, X_n\}$  of FCSs such as current, relative humidity, gas pressure, temperature, etc., relative to the prediction horizon (the time vector  $X_1$ ) would be known in the prediction phase. This assumption may not be acceptable in automotive applications, especially as RUL prognostic requires a prediction over a very long horizon ( $\sim$  several hundred or even several thousand hours).

To address this issue, a BPNN-based RUL prognostic algorithm for FCSs in real-world scenarios is developed in this study so that only the time vector should be required as input to predict over a given horizon in the prediction phase.

The learning phase involves two steps that enable the network to characterize the FCS degradation trend: a forward propagation phase and the error backpropagation phase. A detailed description of each phase can be found in [35, 53] with the related equations.

## 4. MFCS system RUL prognostic-based energy management strategy

A rule-based approach is adopted for FCSs' RULs prognostics integration in MFCS systems energy management in this paper. The proposed EMS will be referred to as the RUL prognostic-based adaptive Daisy-Chain strategy.

### 4.1. Daisy-Chain principle

The Daisy-Chain principle is a basic strategy of operating an MFCS system. It involves activating the FCS one by one until all the required power is supplied, or until all the FCS are used.

This principle takes advantage of MFCS systems' modularity, as it always activates the minimum number of FCS needed to meet a power demand. However, the non-delimitation of FCSs' operating power ranges accelerates their degradation. Additionally, since FCSs are always used in the same order, some FCSs may age faster than others due to overuse.

In this paper, the RUL prognostic-based adaptive Daisy-Chain strategy will ensure that all FCSs in the MFCS system reach their end-of-life (EoL) at approximately the same time to prevent the MFCS system from too early degraded mode operation. Operating in degraded mode signifies that the MFCS system is reaching its EoL, as it will eventually be unable to meet the load requirements.

### 4.2. RUL prognostic-based adaptive Daisy-Chain energy management strategy

For the FCSs to reach their EoL at almost the same time, their degradation levels must be balanced throughout their operating time. To do so, first, FCSs scheduling is updated in descending order of RULs each time the RULs predictions are made, as shown in Fig.5. RUL predictions will be performed every 1000 hours in this paper to allow the prognostic model to learn FCSs' degradation trend properly, considering that FCSs' aging is a relatively slow process.

The obtained scheduling is updated a second time based on FCSs' previous operating modes to assign to the most degraded FCS the rank that would make it possible to slow down its aging. It should be noted that the first FCS in the queue may not always age faster than the other FCSs, under the Daisy-Chain principle, as the power requested from the MFCS system would be greater than 0 W most of the time due to the mission profile dynamics filtering. Actually, FCSs' start-stop cycles could be reduced by assigning each FCS the top position in the scheduling from time to time. Therefore, after the first scheduling in descending order of RULs, the following adjustments should be made to obtain the final scheduling of FCSs.

- The FCS that has the biggest RUL, which is the first FCS in the queue, must be moved to the rank previously occupied by the FCS that has the lowest RUL.

In the next section, the performance of the proposed EMS will be evaluated on a hybrid MFCS/ battery system using the WLTP class 3 driving cycle and compared to two conventional EMSs'.

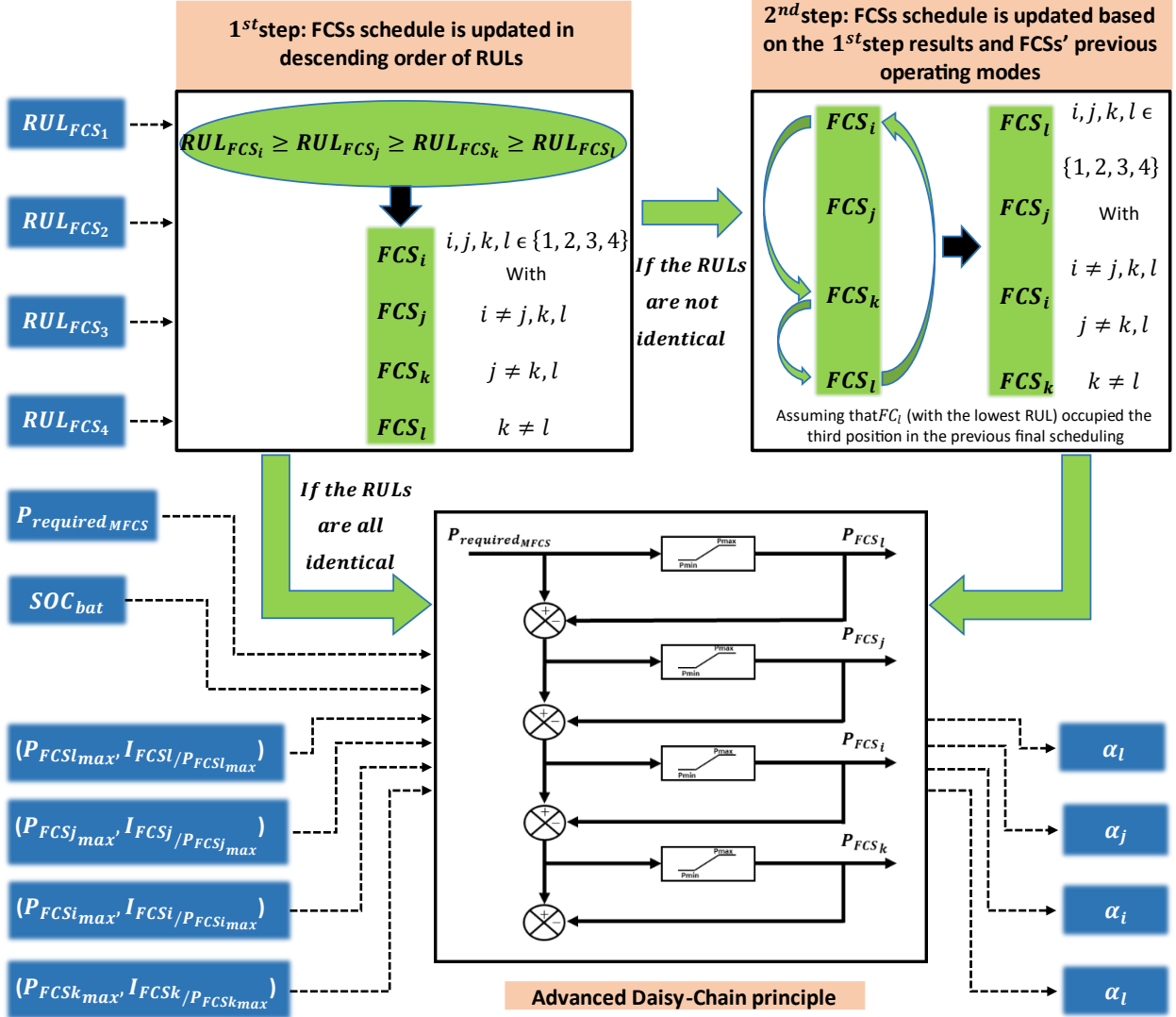


Fig. 5. Operating principle of the RUL prognostic-based adaptive Daisy-Chain EMS considering four FCSs and assuming that the FCS with the lowest RUL occupied the third place in the previous final scheduling.

- The FCS that has the lowest RUL must then move to the front of the queue to slow down its aging process.
- If the FCS with the lowest RUL was the first FCS in the previous final scheduling, all FCSs must be used in the same order as before. In fact, since the first rank corresponds to the slowest degradation rate, if the FCS with the lowest RUL occupied the first rank previously, that means that it is still more degraded than all other FCSs.

Fig.5 illustrates the RUL prognostic-based adaptive Daisy-Chain EMS considering four FCSs and assuming that the FCS with the lowest RUL occupied the third position in the previous final scheduling. This figure depicts the MFCS system EMS block that appears in Fig.6.

## 5. Simulation results

### 5.1. Hybrid MFCS/ battery system design choices

Several design choices and assumptions have been made regarding the hybrid MFCS/ battery system to simplify the study [54] [55].

- Parallel fluidic and electrical architectures are adopted to make the MFCS system as modular as possible, to offer the maximum degrees of freedom to the EMS for decision-making.

- The battery is connected directly to the DC bus, without using a converter. This topology reduces the volume, weight, and cost of the system. It also simplifies energy management between the battery and the MFCS system.
- The battery SOC variation range is restricted to 20% to limit DC bus voltage fluctuations, as this voltage would be imposed by the battery under the adopted topology.
- The DC bus voltage is assumed to be 72 V to match the DC bus voltage on the test bench.
- The MFCS system consists of 500 W-FCS systems, to ensure that power levels during simulations match those on the test bench. Therefore, the power profile obtained by applying the Newton's second law of motion to a regular-sized car is rescaled while keeping the dynamics.
- The hybrid MFCS/ battery system sizing is done regarding the power profile under the WLTP class 3 standard, as this cycle reproduces real driving conditions. Thereby, it is assumed that the hydrogen tank always contains enough hydrogen, and that the

to be recharged with an additional current of 4 A from the MFCS system. The charging current is based on the recommended charging current range which is 10% to 20% of the battery's nominal capacity. The modes that define the charged and discharged states of the battery are summarized by the hysteresis cycle depicted in Fig.7.

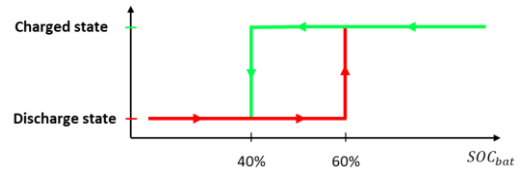


Fig. 7. Battery's charged and discharged states defined by a hysteresis cycle

## 5.2. Hybrid MFCS/ battery system simulation results under the proposed EMS

The distribution of  $P_{required_{MFCS}}$  between the four FCS systems by the RUL prognostic-based adaptive Daisy-Chain EMS proposed in this paper is shown in

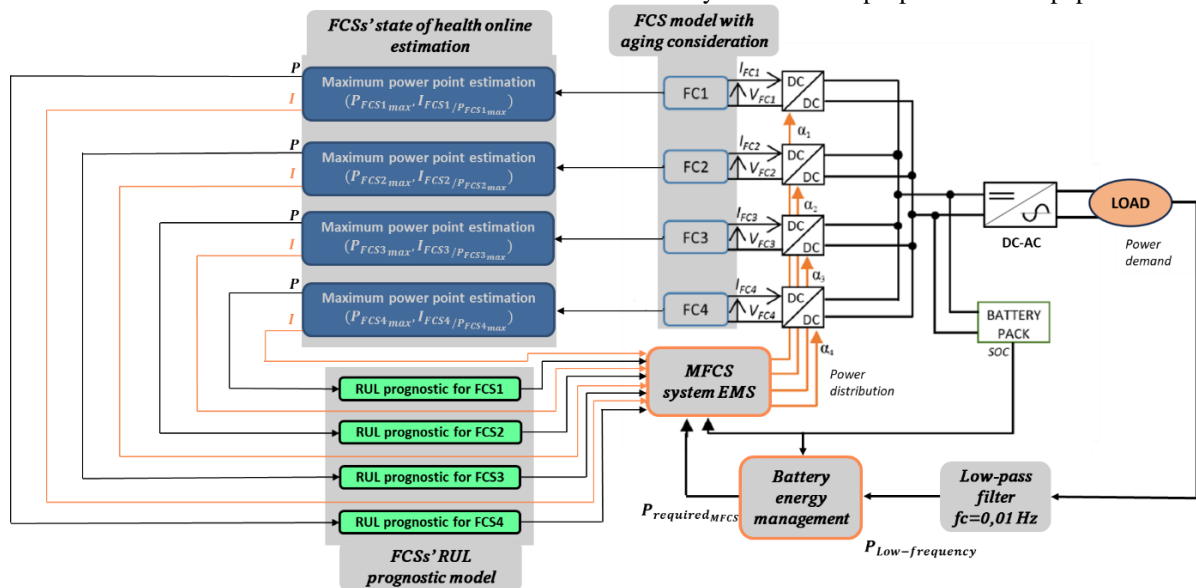


Fig. 6. Synoptic diagram of MFCS systems' RUL prognostic-based energy management concept

vehicle's range is not limited.

- The hybrid MFCS/ battery system sizing is done based on mission profile frequency decomposition technique. A low-pass filter with a cut-off frequency of 10 mHz is used for this purpose. As a result, it was found that at least four 500 W-FCS and a 20 Ah-battery would be necessary to respond to the WLTP rescaled profile.

The synoptic diagram of MFCS systems' RUL prognostic-based energy management concept is presented in Fig.6. The battery energy management module makes sure that the battery's SOC remains between 40% and 60% to limit fluctuations in the DC bus voltage. When the battery gets discharged, it needs

Fig.8. It should be noted that, from 0 h to 1,000 h, the FCSs were used in the same way under the equidistributional EMS, while the first training data of the prognostic algorithm were collected to perform the RUL prediction for the first time at  $t = 1,000 h$ . From 1,000 h to 2,000 h, the FCSs were operated in the initial order, i.e., FCS N°1, FCS N°2, FCS N°3, FCS N°4, as they had the same RUL at  $t = 1,000 h$ , which is 37,000 hours (Fig.9). As shown in Fig.10, using the FCSs in this order resulted in more degradation on FCS N°4 compared to FCS N°2, whose degradation was also important than that of FCS N°3. The FCS N°1, which was the first FCS in the queue from 1,000 h to 2,000 h, had the biggest RUL at  $t = 2,000 h$  (Fig.9), since it was

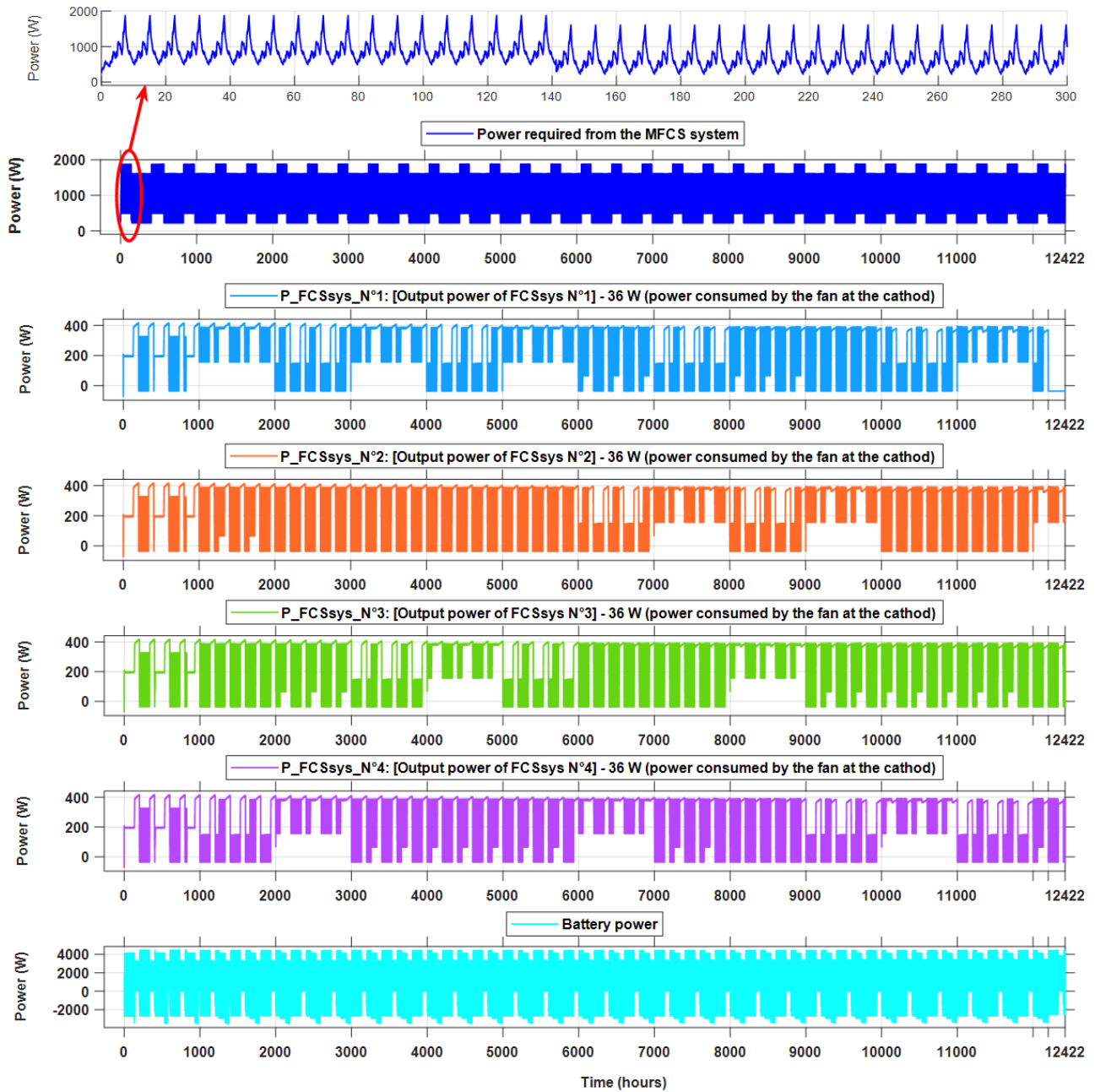


Fig. 8. Distribution of the power required from the MFCS system between the four FCS systems; battery power [RUL prognostic-based adaptive Daisy-Chain EMS]

never shut down in that time range, making it the FCS that experienced the least start-stop cycles. Consequently, at  $t = 2,000$  h, FCSs scheduling in descending order of RULs was FCS N°1, FCS N°3, FCS N°2, and FCS N°4. The second scheduling had to be performed, as the RULs were not equal. The FCS N°4 with the lowest RUL had to be moved to the first position, while the FCS N°1 with the highest RUL had to be moved to the position that was previously occupied by the FCS N°1 from 1,000 h to 2,000 h, meaning the fourth position. Thus, the expected operation order of FCSs from 2,000 h to 3,000 h was FCS N°4, FCS N°3, FCS N°2, and FCS N°1. As can be seen from Fig.8, the

FCSs were actually used in this order from 2,000 h to 3,000 h.

From 3,000 h to 4,000 h, the final operating order of FCSs was FCS N°1, FCS N°4, FCS N°2, FCS N°3, as the first scheduling in descending order of RULs at  $t = 3,000$  h was FCS N°3, FCS N°4, FCS N°2, FCS N°1. The first position occupied by the FCS N°4 from 2,000 h to 3,000 h enabled it to slow down its aging process, indeed (Fig.10). This degradation trend improvement was learned by the RUL prognostic model as well, because at  $t = 3,000$  h, the FCS N°4 was no longer the last FCS in the queue but the second one (Fig.9). However, due to the small amount of training data available at that time, the significant slope variation



observed from  $t = 2,000 h$  in the degradation trend could not be captured accurately by the prognostic model. As a result, FCS N°3's RUL was higher than that of FCS N°4 at  $t = 3,000 h$ . Actually, the FCS N°4 should have the best RUL at that moment. This error was rectified by the prognostic algorithm at the next prediction session (at  $t = 4,000 h$ ), as new maximum power samples were added to the time series between  $t = 3,000 h$  and  $t = 4,000 h$ . It is worth noting the consistency between FCSs' scheduling in descending

then regarding their previous operating mode. After each final scheduling update, the power  $P_{required_{MFCS}}$  required from the MFCS system was distributed between FCSs according to the advanced Daisy-Chain principle applied in this paper, until the MFCS system reached its EoL at  $t = 12,422 h$ , as shown in Fig.8. It should be noted that, the MFCS system is considered at its EoL as soon as the battery is discharged while the MFCS system is operating in degraded mode. Indeed, when operating in degraded mode, the MFCS system is

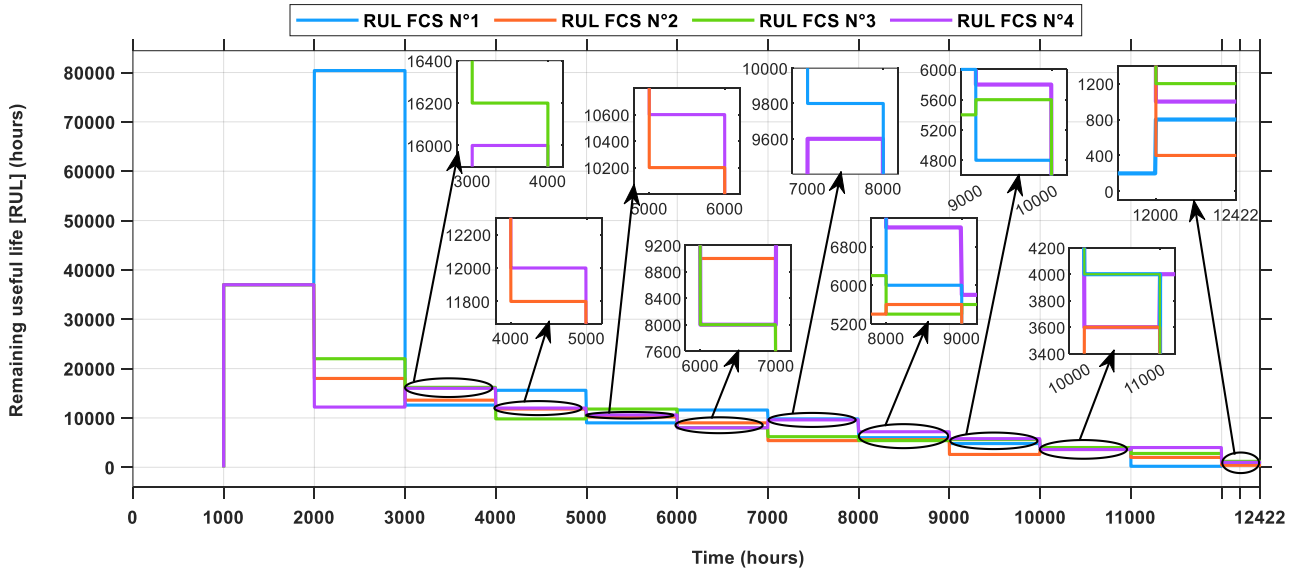


Fig. 9. FCSs' RUL prognostic every five hours [RUL prognostic-based adaptive Daisy-Chain EMS]

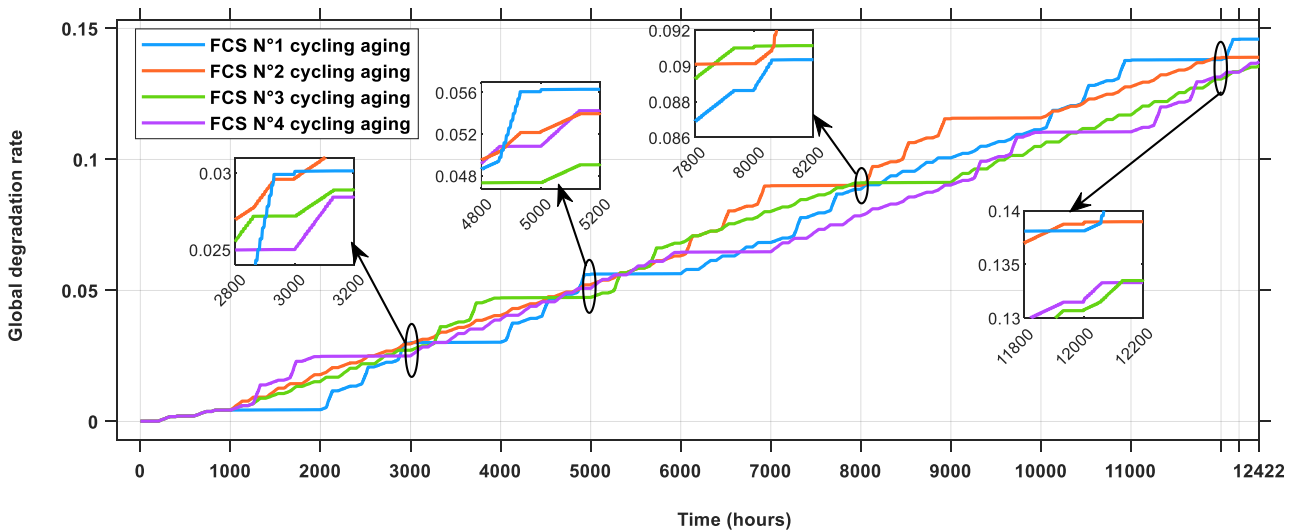


Fig. 10. FCSs' cycling aging evolution [RUL prognostic-based adaptive Daisy-Chain EMS]

order of RULs at  $t = 4,000 h$ , which is FCS N°1, FCS N°4, FCS N°2, FCS N°3 (Fig.9) and their scheduling in ascending order of cycling degradation at  $t = 4,000 h$  (Fig.10). The final operating order of FCSs from 4,000 h to 5,000 h was exactly the expected final scheduling (FCS N°3, FCS N°4, FCS N°2, and FCS N°1).

FCSs' operating order was continuously updated every five hours, first in descending order of RULs and

undersized and cannot meet the requirements for a proper battery use, healthily speaking. In Fig.8, the degraded mode operation of the MFCS system started at  $t = 12,200 h$  when the FCS N°1 reached its EoL (loss of 10% of the maximum power) and the battery got discharged at  $t = 12,422 h$ . Additionally, 982.4 kg of  $H_2$  were consumed over the lifetime of the MFCS system to meet the load demand.

The hybrid MFCS/ battery system's energy management is also carried out by the equidistributional and the Daisy-Chain EMSs to highlight the performance of the proposed EMS. For the comparative study to be fair, these conventional EMSs are revised to operate FCSs only in their safe power range, as the proposed EMS did.

### 5.3. Hybrid MFCS/ battery system simulation results under conventional EMSs

When applying the equidistributional EMS and the Daisy-Chain EMS to the MFCS system over the entire simulation time, the system reaches its EoL after only 5,000 hours, and 5,214 hours, respectively. In addition to the non-adaptive nature of these conventional EMSs, three reasons can explain the lifetime improvement observed with the proposed EMS.

- Firstly, the proposed EMS is based on the Daisy-Chain principle. By allocating  $P_{required_{MFCS}}$  to the first FCS in the queue, one of the FCSs in the MFCS system usually experienced very few start-stop cycles.
- Secondly, the proposed EMS updates FCSs operating order to balance their degradation levels. This offers to each FCS the advantage of being the first FCS in the queue, which results in a reduced frequency of start-stop cycles.
- Finally, when the remaining power demand has to be supplied by a FCS, but it is out of the FCS safe power range, the proposed EMS optimizes the start-stop cycles of this FCS by checking its current state (on or off) before deciding whether to operate it or shut it down.

In conclusion, operating the MFCS system under the equidistributional and the Daisy-Chain strategies instead of the proposed EMS, results respectively in a loss of 59.75% and 58.03% on the MFCS system's lifetime. However, the equidistributional strategy would make the hybrid MFCS/ battery system consume less hydrogen than the proposed strategy for the same operating time. For 5,000 operating hours, the hybrid system consumed approximately 389.2 kg of hydrogen under the proposed EMS versus 356.2 kg under the equidistributional strategy, representing a reduction in hydrogen consumption of around 8.48%. Indeed, the equitable distribution of power demand between FCSs resulted in FCSs operating mostly in the low current density zone, which is very close to the best energy efficiency zone for FCSs. On the other hand, under the proposed EMS and the Daisy-Chain EMS, FCSs were mostly operated in the high current density range to meet the power demand using the minimum number of FCSs.

The Tables 1-2 summarize respectively the comparative analysis of the MFCS system's lifetime and hydrogen consumption under the proposed EMS vs. the conventional EMSs.

Before concluding this work, the proposed EMS should be compared with the reference EMS, which is the SOH estimation-based adaptive Daisy-Chain EMS, to check whether the potential errors in the RUL prediction affects the ultimate lifetime of the MFCS system or not.

## 6. reference EMS simulation results

The SOH estimation-based adaptive Daisy-Chain EMS is a variant of the proposed EMS, as FCSs' operating order would be updated based on their SOH estimations instead of their RULs. This strategy can be seen as the reference EMS regarding the energy management principle applied in this paper, since SOH estimations would be definitely more accurate than RUL predictions. The prognostic algorithm may not be able to capture significant changes in FCSs' degradation trends accurately. Although the resulting RUL predictions errors can be corrected as the amount of training data increases, it could be hard to know if the post-prognostic decisions adjustments were enough to extend the MFCS system's lifetime as much as it would be when using more accurate information like FCSs' SOH estimations. To investigate this, the hybrid MFCS/ battery system simulation results under the reference EMS are presented in this section.

Table 1

MFCS system's lifetime under the RUL prognostic-based adaptive Daisy-Chain EMS vs. conventional EMSs

EMS	Proposed EMS	Equidistributional EMS	Daisy-Chain EMS
MFCS system's lifetime	12,422 hrs	5,000 hrs	5,214 hrs
Gain	-	2.48	2.38

Table 2

MFCS system's  $H_2$  consumption under the RUL prognostic-based adaptive Daisy-Chain EMS vs. conventional EMSs

EMS	Proposed EMS	Equidistributional EMS	Daisy-Chain EMS
MFCS system's $H_2$ consumption	t = 5,000 h	389.2 kg	356.2 kg
	t = 5,214 h	405 kg	404.4 kg
	t = 12,422 h	982.4 kg	
$H_2$ consumption reducing compared to the proposed EMS	-	8.48 %	0.15 %

In the reference EMS, FCSs' maximum powers are resampled each five hours so their operating order will

be updated at the same frequency as in the RUL prognostic-based adaptive Daisy-Chain EMS (proposed EMS). Under the reference EMS, the MFCS system reached its EoL in 12,460 hours, which is just 38 hours longer than the lifetime obtained under the proposed EMS. Therefore, it is quite acceptable to conclude that the proposed strategy extends the MFCS system's lifetime as much as the reference EMS, although RUL prognostics are not as accurate as maximum power estimations.

Furthermore, the hydrogen consumption of the hybrid system under the reference strategy from  $t = 0$  h to  $t = 12,422$  h would be around 984.6 kg (i.e., 2.2 kg more than the amount of hydrogen consumed under the proposed EMS).

It can be concluded from these results that the comparative study of the RUL prognostic-based energy management concept for MFCS systems and the SOH estimation-based energy management approach deserves further investigation. Using FCSs' RUL prognostics in MFCS systems energy management could simplify adaptive EMSs design compared to the SOH estimation-based energy management approach. In fact, the SOH of a FCS can only decrease over time, whereas its RUL can actually increase between two consecutive prognostic sessions. This makes the RUL a suitable parameter to analyze when making adaptive energy management decisions.

## 7. Conclusion

A health-conscious EMS is proposed for MFCS systems in this paper to improve their lifetime. This study is part of the PHM framework, which has seen significant progress over the last decade in FCSs RUL prognostic algorithm development for appropriate energy management decision-making regarding FCSs' durability. Therefore, an ANN-based prognostic algorithm was proposed for FCSs real-world use in automotive applications and combined with an advanced Daisy-Chain energy management principle to investigate the prognostic-based energy management concept under a real vehicle use scenario.

The proposed strategy was referred to as RUL prognostic-based adaptive Daisy-Chain EMS. By integrating RUL prognostics into the Daisy-Chain energy management principle, it was possible to balance FCSs' degradation levels, thus preventing the MFCS system from too early degraded mode operation. Indeed, operating in degraded mode signifies that the MFCS system is reaching its EoL, as it will eventually be unable to meet the load requirements.

The RUL prognostic-based adaptive Daisy-Chain EMS has been validated through simulations in Matlab/Simulink environment. The simulations were performed on an MFCS system consisting of four 500 W-Horizon FCSs using the WLTP class 3 driving cycle.

A comparative analysis of the MFCS system performance was conducted under the proposed EMS and two conventional EMSs (The equidistributional and the Daisy-Chain EMSs). The results showed that the proposed EMS can extend the MFCS system's lifetime by over 2.48 and 2.38 times compared to the equidistributional and the Daisy-Chain EMSs, respectively.

In terms of hydrogen consumption, the MFCS system consumed almost the same amount of hydrogen under both the proposed EMS and the Daisy-Chain strategy. However, approximately 8.48% of hydrogen was saved under the equidistributional EMS, as FCSs were often operated in their best energy-efficient regions (low current density range) due to the equitable distribution of power demand between them. It should be reminded that under the proposed EMS and the Daisy-Chain EMS, FCSs were mostly operated in their high current density range to meet the power demand using the minimum number of FCSs.

A last comparison study was conducted in this paper between the proposed EMS and the reference EMS which is based on FCSs' SOH estimations. The proposed strategy has been found as reliable as the reference strategy although RUL prognostics may not be as accurate as SOH estimations.

This work can be considered as a proof of concept. The next future research objective in this area is to focus on integrating FCSs' RUL prognostics into MFCS systems energy management through an optimization approach.

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