

NVH optimization of electric motors: optimization under constraints and uncertainty

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Abstract

The optimization methodology described in this paper aims at minimizing the noise and vibrations of electric motors. It relies on a numerical workflow involving electromagnetic, dynamic and acoustic models. Afterwards, a deterministic optimization method is described and applied to automotive traction motors. A robust enhancement of the optimization is then presented. It aims at considering the effect of manufacturing tolerances, materials properties dispersion and control uncertainties on the vibratory and acoustic levels to minimize, so that the electric motors are really silent when manufactured and operated. An application case of this robust optimization based on an automotive motor is then detailed.

1 Introduction

To estimate the noise radiated by an electric motor numerically, methods performing a weak coupling between electromagnetic, dynamic and acoustic models are frequently applied to diverse motor technologies [1]-[5]. These methods offer good accuracy when compared with measurements [6], and they enable for the estimation of the level of noise radiated by any design. Some minimization algorithms can be used in order to modify the electric motors design so as to minimize the radiated noise estimated using the multiphysical workflow, while ensuring, by means of optimization constraints, that overall electromechanical performance criteria, such as mean torque, torque ripple or efficiency, are not deteriorated. Using this method, significant noise level reductions can be achieved, owing to the high sensitivity of the electromagnetic excitations harmonic and spatial content to slight design modifications. Such optimization algorithms are used to reduce the noise of electric motors in [7] and [8]. To overcome the generally high number of cost function evaluations required by optimization algorithms, the authors of these articles use fast modelling workflows, i.e. respectively a fully analytical modelling workflow and a surrogate model. In the present paper, in the context of computing power increase, the use of a more accurate finite element electromagnetic model makes it possible to take full advantage of the noise reduction possibilities offered by slight geometric variations.

However, the sensitivity can be so high that slight geometric deviations of the magnetic active parts within the manufacturing tolerances can lead to very high variations of the electromagnetic excitations spectral content and thus to the loss of the radiated noise reductions achieved by optimization. For such cases where deterministic optimization is not suited, a robust optimization method is presented. The probabilistic robust optimization methodology has been used for various applications in dynamics [9,10], but it is applied for the first time to the vibroacoustic optimization of electric motors. It ensures, when considering random deviation of the uncertain parameters, to converge towards a design with a low average noise level, and a low variability. After describing the simulation methodology, the deterministic and robust optimization methods are described and applied to minimize the noise radiated by automotive traction motors.

2 Multiphysical simulation of electric motors noise

The numerical simulation of the noise generation process in electric motors requires the modelling of phenomena belonging to different fields of physics. The noise generation process is summarized on figure 1.

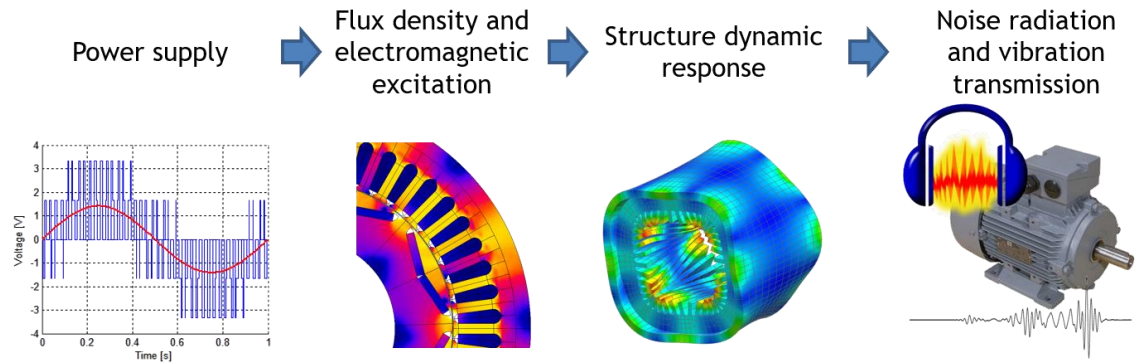


Figure 1: Overview of the noise generation process in electric motors.

It can be divided into four steps:

- The supply of the motor by Pulse Width Modulation (PWM) of the supply voltage leads to the appearance of high order harmonics in the currents.
- These current harmonics, combined with the stator and rotor geometry and with the windings distributions, result in harmonic contributions in the airgap flux density, and as a consequence to dynamic contributions in the radial and tangential Maxwell pressures, which constitute the prevailing electromagnetic excitation in electric motors, as stated in [11].
- The electromagnetic excitations apply to the stator and the rotor and cause vibrations, with an amplitude depending on the modal basis and damping of the powertrain structure, and on the amplitude, frequency and spatial distribution of the electromagnetic excitations.
- Depending on the operating deflection shapes and the vibration frequencies, the structure will prove to be more or less prone to radiating noise.

An overview of a 3-step multiphysical calculation scheme based on finite element models is given on figure 2.

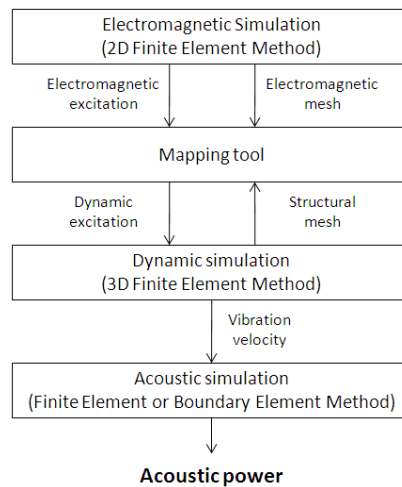


Figure 2: Basic principle of the multiphysical simulation methodology.

The motor is first modelled using the electromagnetic 2D finite element method. At this stage, the two first steps of the noise generation process depicted on figure 1 are considered, since the supply conditions, the geometric design, the material properties and potential defects such as eccentricity are modelled. From this simulation, the radial and tangential flux densities are calculated along the air gap (as illustrated by figure 3), for different positions of the rotor.

The Maxwell pressures applying to the stator all along the airgap can then be calculated using

$$\sigma_r = \frac{1}{2\mu_0} (B_r^2 - B_t^2), \quad (1)$$

$$\sigma_t = \frac{1}{\mu_0} (B_r B_t), \quad (2)$$

where σ is the surface force density, B is the magnetic flux density, μ_0 is the magnetic permeability of vacuum, and r and t denote radial and tangential components.

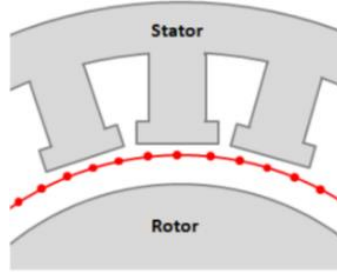


Figure 3: Calculation points of the Maxwell pressure inside the airgap.

After converting the Maxwell pressure results from time-domain excitations to frequency domain excitations, they are projected onto the structural mesh of the powertrain. This process is performed using a dedicated mapping tool, dealing with the electromagnetic and structural meshes of different sizes and converting the 2D excitations calculated using the electromagnetic simulation into 3D excitations. The dynamic response of the structure is then calculated by modal frequency response. The modal basis of the powertrain structure is first extracted, and the dynamic response of each mode under the effect of electromagnetic excitations is calculated. The operating deflection shape is then obtained by summing the contribution of each mode. Some guidelines on the modelling of laminated stators are given in [12].

The last step of the procedure is about the estimation of the noise radiated by the machine, caused by the interaction of the vibrating structure with the surrounding air. The noise can be estimated from the vibration velocities of the motor's outer skin, either by time consuming but accurate numerical methods, such as acoustic finite element method (FEM) or boundary element method (BEM), or by using much faster analytical methods.

3 Deterministic multi-criteria optimization approach

3.1 Description of the approach

An optimization approach can be implemented at each step of the noise generation process depicted in figure 1:

- Optimization of the power supply and control strategy [3],
- Optimization of the electromagnetic design (number of poles, number of slots, shape and position of the magnetic active parts) [3],
- Optimization of the structure design [3,13],
- Optimization of the machine integration to reduce the propagation of vibration and sound inside and out of the vehicle [3].

The optimization method presented in this paper focuses on the optimization of the electromagnetic design. It aims at changing the geometry of the active magnetic parts in order to reduce the level of some electromagnetic excitations contributions which appear to be the cause of high noise levels. The amplitudes of the Maxwell pressures contributions which are responsible for the noise in electric motors are very sensitive to electromagnetic design parameters such as the shape of the rotor poles or stator teeth. Therefore, a major benefit of this kind of optimization is that the geometrical changes applied to the design are small

from a mechanical point of view, and they do not imply any significant increase of the motor's mass or additional cost.

The principle of this method is to use a simulation workflow following the same weak coupling principle as that described in figure 2, enabling for the estimation of the noise radiated by an electric motor for a given set of input parameters. The noise level radiated by the motor, or another criterion which must be reduced to improve the vibroacoustic behavior of the motor, is defined as the cost function of an optimization algorithm. This algorithm aims at minimizing this cost function by modifying some design parameters in the electromagnetic model.

Moreover, it is essential to guaranty that the design modifications resulting in the vibratory or acoustic level reduction do not deteriorate the overall electromechanical performance of the motor. For that purpose, constrained optimization is carried out. As depicted on figure 4, from a single electromagnetic simulation, not only the vibroacoustic behavior of the motor, but also its efficiency, its thermal behavior or its torque performance can be computed. As a consequence, the noise radiated by electric motors can be optimized at the same level as the aforementioned performance criteria.

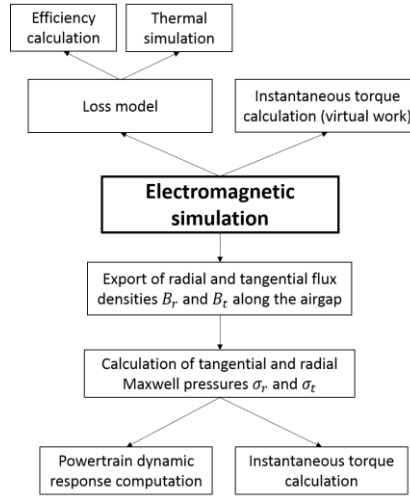


Figure 4: Objective and constraint function possibilities from a common electromagnetic simulation.

Most of the time, this optimization method is used to reduce the vibratory or acoustic levels of the motors without deteriorating the overall performance. However, they can equally be used to maximize the overall performance without increasing the vibratory or acoustic level, or to find a trade-off both improving the overall performance and decreasing the vibratory or acoustic level.

3.2 Applications

3.2.1 Optimization of a 10-pole permanent magnet synchronous motor

In the first practical case, the aim is to reduce the noise radiated by the automotive traction 10-poles interior permanent magnet synchronous motor (IPMSM) with V-shaped magnets depicted in figure 5. Because of their high torque density, high efficiency and good reliability, these motors are commonly used for automotive traction.

The objective of the optimization is to minimize the acoustic power level of the motor without decreasing its mean torque. The optimization should also ensure that torque ripple is not increased, as it can lead to noise and vibration issues because of the excitation of other components of the mechanical drive or the excitation of overall bending modes of the powertrain.

Before running the optimization, a diagnosis of the motor's dynamic behavior must be performed in order to identify the critical motor speeds at which the noise should be reduced. This is done using the workflow described in figure 2.

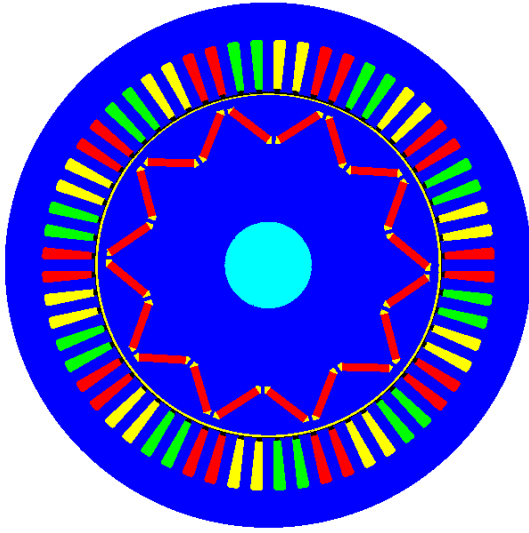


Figure 5: Geometry of the initial PMSM

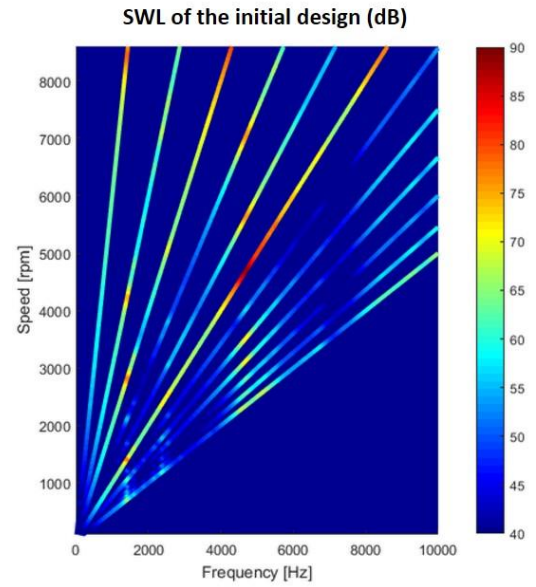


Figure 6: Campbell diagram of the initial IPMSM
Sound Power Level

Figure 6 shows a Campbell diagram of the initial IPMSM design's Sound Power Level (SWL). The engine orders involved in the noise generation process are multiples of 10. The SWL related to engine order 60 is emerging around 4700 rpm, because of the resonance of the stator's breathing mode under the effect of the Maxwell pressure contribution related to engine order 60.

This diagnosis leads to an optimization aiming at reducing the noise level at the speed where the noise and vibrations are prevailing, i.e. at 4700 rpm. For this purpose, the cost function is defined as the acoustic power level at the engine speed of 4700 rpm.

To ensure that the torque performance is not deteriorated, some inequality constraints are also defined, so that the mean torque produced by the motor is not reduced and torque ripple is not increased in comparison with initial design.

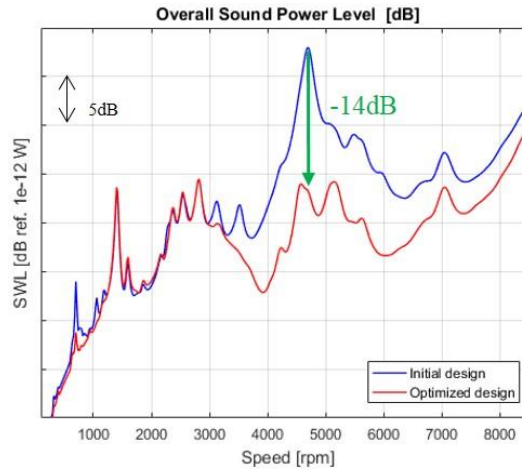


Figure 7: Comparison of the SWL of the IPMSM initial and optimized designs

On figure 7, the results show a very significant 14 dB decrease of the SWL at the critical speed of the motor. More generally the noise level is reduced over the full speed range from 3000 rpm to 8600 rpm, while it remains almost unchanged under 3000 rpm. This reduction was achieved by small changes on the shape of the rotor poles depicted on figure 8.

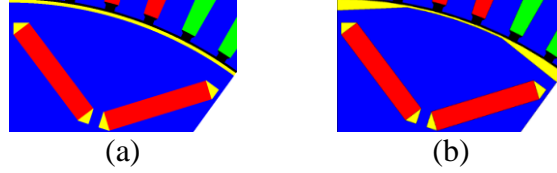


Figure 8: (a) IPMSM initial design, (b) IPMSM optimized design

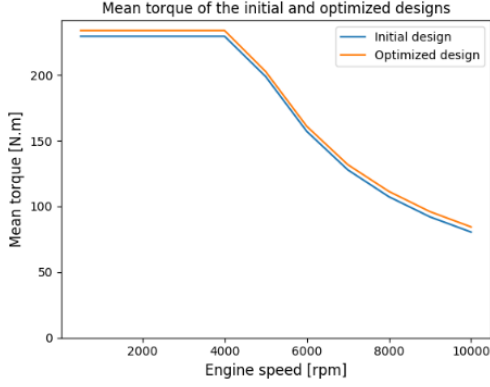


Figure 9: Comparison of the mean torque of the initial and optimized IPMSM at maximum power

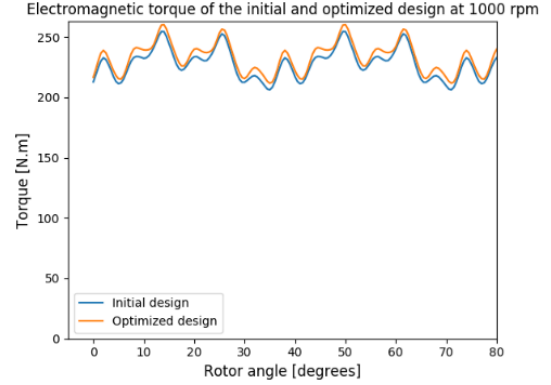


Figure 10: Comparison of the instantaneous torque of the initial and optimized IPMSM at maximum power at 1000 rpm

	Initial design	Optimized design
Mean torque (N.m)	228.7	233.7
Torque ripple (%)	10.5	10.4

Table 1: comparison of mean torque and torque ripple at 1000 rpm before and after optimization

The noise could also be reduced under 3000 rpm by performing multi-objective optimization aiming at reducing the noise at different motor speeds, at the risk of achieving lower reduction at the critical speed of 4700 rpm because a trade-off design must then be found.

Figure 9 and figure 10 show the mean torque and instantaneous torque curves for the initial and optimized designs.

Table 1v compares the mean torque and torque ripple values at 1000 rpm. The constraints are respected, because there is no decrease of the mean torque, and no increase of torque ripple. The optimization even brought some improvement regarding these two criteria.

3.2.2 Optimization of a 8-pole permanent magnet synchronous motor

In this case, a complete powertrain composed of an 8-pole 48-slot Permanent Magnet Synchronous Motor (PMSM), its housing and mounts, the gearbox housing and the power electronics unit must be optimized. The following issue is faced: torque ripple causes the resonance of a powertrain overall bending mode. This is a critical issue because this resonance occurs at low speeds, between 500 and 3000 rpm, where the electromagnetic noise radiated by the powertrain is prevailing in comparison with aerodynamic and rolling noise. Moreover, the modal frequency of the overall bending mode whose shape is prone to excited by torque ripple is located around 1000 Hz. When a resonance of this mode occurs, the powertrain structure radiates noise at 1000 Hz, a frequency to which the human ear is particularly sensitive.

As any periodic function, the instantaneous torque created by the motor can be expressed in the frequency domain using Fourier series decomposition. Engine orders 24, 48 and 96 mainly contribute to torque ripple, and they cause the resonance of the overall bending mode at different engine speeds. Another particularity of the motor is that its rotor is skewed. It is made of 4 parts of equal length along its axis: the first part being the reference, the second and third parts are identical and shifted by 3.75° while the fourth

one has the same orientation as the reference part. As a consequence, neglecting the side effects, the electromagnetic excitations are determined by using a 2D electromagnetic model for each section independently. To simplify the simulation process which must be performed at each cost function evaluation required by the optimization, the objective of the optimization is to directly minimize the torque ripple contributions related to engine orders 24, 48 and 96 at the engine speed at which they reach the frequency of 1000 Hz and provoke the resonance of the overall bending mode, i.e. at 2500 rpm for engine order 24, 1250 rpm for engine order 48 and 625 rpm for engine order 96. At the same time, attention must as always be paid to the mean torque of the motor so that it is not reduced during the optimization process. This is done by adding an inequality constraint guaranteeing that the mean torque of the optimized design, with no change of the supply currents, remains at the same level as that of the initial design.

Using the same optimization algorithms as for SWL reduction, significant torque ripple reductions can be achieved for the targeted engine orders at their critical speeds.

As a result, as depicted in figure 11, the optimized design produces a much smoother torque.

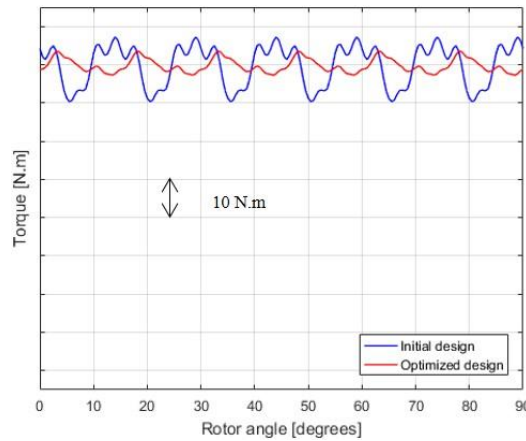


Figure 11: Instantaneous torque comparison for initial and optimized designs at 1250 rpm

The torque ripple is significantly reduced for the optimized design, while the mean torque is unchanged. The amplitude reductions of torque engine orders 24, 48 and 96 can be expressed in decibels using

$$R_{DB} = 20 \log_{10} \left(\frac{T_{h_{optimized}}}{T_{h_{initial}}} \right), \quad (3)$$

where R_{DB} is the reduction in dB, $T_{h_{optimized}}$ is the amplitude of the h^{th} torque engine order produced by the optimized design $T_{h_{initial}}$ is the amplitude of the h^{th} torque engine order produced by the initial design.

These torque ripple reductions are summarized in table 2. The abbreviation e.o. stands for engine order.

Engine order and critical speed	e.o. 24 at 2500 rpm	e.o. 48 at 1250 rpm	e.o. 96 at 625 rpm
Reduction of the torque harmonics (simulation)	9.1 dB	7.5 dB	11.2 dB

Table 2: Reductions of the numerical torque amplitude levels in comparison with the initial design

As the resonance of the overall bending mode due to torque ripple excitation is prevailing over the other phenomena between 500 and 3000 rpm, expressing the reductions achieved for each torque engine order in dB gives an accurate estimation of the SWL reductions to be expected. As a consequence, the SWL reductions achieved in this case should be close to the torque engine order 48 level reduction values presented in table 2.

The effect of these modifications on the motor's SWL is calculated using the complete simulation workflow described on figure 2 and validates the reductions expected when considering torque harmonics. On this basis, a prototype has been built. The experimental results provide the reductions synthesized in table

3. These reduction of the near field acoustic pressure overall level are even higher than those estimated by the simulations, and they validate the optimization method.

Motor speed	2500 rpm	1250 rpm	625 rpm
Reduction of the near field acoustic pressure (experimental overall level)	11 dB	18 dB	17 dB

Table 3: Reductions of the measured near field overall acoustic levels in comparison with the initial design

In this case, the experimental results show that the optimized design is probably robust, although several prototypes should be built or a numerical sensitivity analysis should be conducted to quantify the variability of the optimization cost function when considering geometric deviation.

However, several optimizations starting from different designs have been necessary to reach this optimized design. Many optimizations have converged towards designs achieving very high reductions of the torque engine order 48 level, which reveal to be non-robust minima. Performing robust optimization can ensure the convergence towards a robust minimum.

4 Robust optimization approach

4.1 Description of the approach

The aim of robustness in the case of electric motors acoustics is to minimize the impact of uncertainty sources which cannot be eliminated, i.e. mainly geometry and material properties deviation, as well as control inaccuracies, on the vibratory and acoustic behavior of the motor.

The two main forms of robust optimization are [14]:

- A worst case optimization, aiming at minimizing the cost function when the set of uncertain parameters maximizing this cost function is taken [15].
- A probabilistic optimization, considering the cost function as a random function subject to random uncertain parameters following given density functions [9,10]. The aim is then to minimize the mean value of this random cost function, as well as its variability.

The worst case optimization leads to conservative results, and it is rather intended to critical applications where no failure due to the uncertainty sources can be accepted. For the purpose described in this paper, the reduction of the noise radiated by the motor for a wide majority of the motors is targeted, but having a few manufactured motors for which the noise reduction is not as good as expected is not critical. The probabilistic approach is therefore adopted to robustly minimize the acoustic levels of the electric motors.

To evaluate the robustness of a given design using this probabilistic approach, the deterministic cost function is expressed as $f = f(x + \delta)$, where $x = (x_1, \dots, x_N)^T$ is the set of design parameters, which are fixed for the given design, and $\delta = (\delta_1, \dots, \delta_M)^T$ is the set of uncertain parameters, which are considered as random parameters.

A design of given parameters x , and for which all the M uncertain parameters $\delta_i = 0$ are zero, is called nominal design. However, no manufactured design perfectly respects the nominal design because they are all subject to deviations modelled by the uncertain parameters $\delta_i \neq 0$.

In this paper, the assumption is made that the uncertain parameters δ_i follow a normal distribution $\mathcal{N}(0, \sigma_i)$. Their expectation is set to zero, because systematic deviation can be considered by modifying the nominal design. Their standard deviations σ_i can be estimated from experimental data when measurements are available, or if not, by taking a value of the same order of magnitude as the tolerances, which are usually known.

Some Monte-Carlo samplings are then generated, providing different sets of uncertain parameters δ , and $f(x + \delta)$ is computed for each sample. The mean value μ_f and the standard deviation σ_f of f over all samples are the robustness indicators.

The function to minimize to perform robust optimization is then:

$$\alpha\mu_f + (1 - \alpha)\sigma_f, \quad (4)$$

where $\alpha \in [0,1]$ is a scalar weighting factor defining the trade-off to pursue between mean value and standard deviation minimization. In the rest of the paper, this function is called robust cost function

4.2 Application

The deterministic optimization of the 8-pole PMSM leads to the satisfactory results presented in table 2 and table 3. However, many optimizations have been run and some of them have converged towards designs providing very large but also non robust reductions of the torque engine order 48 level. The robustness of one of these non-robust designs is evaluated, and the robust optimization methodology is then applied.

The calculation of the output torque of this skewed PMSM is a relatively long process because of the size of the electromagnetic model and the necessity to model several sections of the motor to account for the skewing effect. This computation time limitation, as well as the fact that the torque engine order 48 is very significantly more variable than the other engine orders when uncertainties are considered, lead to the decision to focus on this engine order 48 at the engine speed of 1250 rpm for this example.

To quantify the robustness of the deterministically optimized non-robust design, the mean value μ_f and standard deviation σ_f of its torque engine order 48 level are calculated.

The number of samples of the Monte-Carlo sampling is limited by the time necessary to compute the torque for each sample. In this case, 200 samples are generated. This number seems appropriate, since the theoretically zero mean value of each parameter is within the range $[-\sigma_i/50, \sigma_i/50]$, while the maximum relative error between a standard deviation calculated over the 200 samples and its theoretical value is of 5%.

The results of the robustness analysis are presented in yable 4. While the nominal design achieves a reduction of 20 dB in comparison with the initial design, the 200 samples provide a mean reduction of 7.6dB. Moreover, the high standard deviation means that the torque engine order 48 level, and thus SWL, are very variable, and that while some manufactured motors are significantly less noisy than the initial design, a non-negligible amount of them are as noisy as the initial design or even louder.

e.o. 48 level reduction of nominal design with respect to initial design	e.o. 48 level mean reduction with respect to initial design	e.o. 48 level standard deviation
20.0 dB	7.6 dB	7.0 dB

Table 4: Results of the robustness analysis of the deterministic non-robust design

The robust optimization methodology presented in this paper can be useful to avoid such non-robust designs and to converge directly towards a robustly silent design. For this purpose, the robust cost function defined in (4) is minimized. The weighting factor α is set to 0.5, what means that the same importance is given to the reduction of the mean value and the standard deviation of the torque engine order 48 level. Moreover, an inequality constraint imposing no mean torque reduction must be performed. As the mean torque of the motor is significantly less sensitive to uncertainties than their vibroacoustic behavior, the inequality constraint only guarantees that the nominal optimized design is not subject to any mean torque reduction when compared with that of the initial design.

The results of this optimization are depicted in table 5. The design resulting from this optimization provides a much larger mean reduction of the engine order 48 level, with a much lower standard deviation.

Both mean value and standard deviation are significantly reduced in comparison with those of the deterministically optimized design which is not robust. The improvement of the robustness is further illustrated by the distributions of the engine order 48 levels reductions for each of the 200 randomly drawn samples of the deterministically and the robustly optimized designs, depicted respectively on figure 12 and figure 13.

	e.o. 48 level mean reduction with respect to initial design	e.o. 48 level standard deviation
Deterministically optimized non robust design	7.6 dB	7.0 dB
Robustly optimized design	15.0 dB	2.14 dB

Table 5: Comparison of the robustness analyses of the deterministically optimized non-robust design and the robustly optimized design

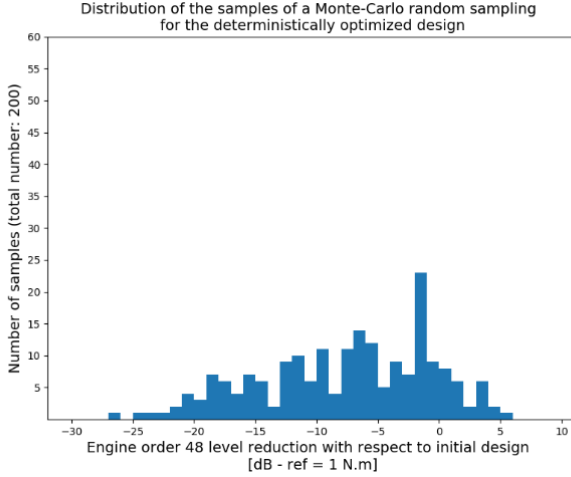


Figure 12: Distribution of the engine order 48 level reductions of the 200 random samples for the deterministically optimized design

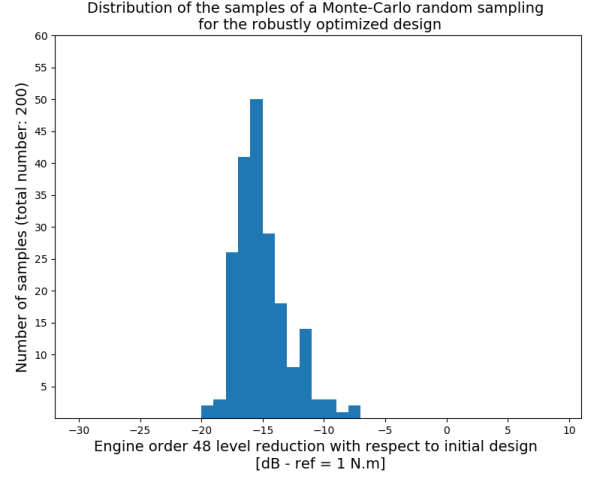


Figure 13: Distribution of the engine order 48 level reductions of the 200 random samples for the robustly optimized design

These results show that probabilistic robust optimization can be applied to optimize electric motors when deterministic optimization converges towards non-robust designs. This method has been applied to minimize only the torque engine order 48 at 1250 rpm, because it is the objective which is subject to the highest variability. The robust optimization method being time consuming, because computing the values of μ_f and σ_f requires several evaluations of the deterministic cost function f , performing a robust multi-objective optimization aiming at minimizing the torque engine orders 24, 48 and 96 at their respective critical engine speeds of 2500 rpm, 1250 rpm and 625 rpm would require a long computation time. An alternative could be to define a multiobjective optimization aiming at minimizing both mean value and standard deviation of the torque engine order 48 at 1250 rpm when uncertainties are considered, and at minimizing the torque engine orders 24 and 96, which are not subject to a high variability when uncertainties are considered, for the nominal design only.

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5 Conclusion

The multiphysical numerical modelling of electric motors, coupling electromagnetic, dynamic and acoustic models, enables for the accurate estimation of their vibroacoustic behavior, but can also be used to reduce their vibroacoustic disturbances using optimization algorithms. These optimizations can lead to large reductions of the vibratory or acoustic levels, while overall performance remains unchanged. In some cases, after performing a deterministic optimization minimizing the vibration or noise levels of a nominal design, the robustness analysis shows that the resulting optimized design has an acceptable variability when the deviation of uncertain parameters is considered. Otherwise, probabilistic robust optimization methods can be used. The efficiency of these methods, to reduce the mean value of acoustic or vibratory levels as well as their variability in an uncertain context, is demonstrated in this paper. They are however time consuming, and their use can be restricted to cases where no robust design can be found by deterministic optimization. Moreover, to reduce the time consumption computational load of the method, it is necessary to select only design parameters and uncertain parameters having a significant effect on the criteria to minimize.

6 Acknowledgements

This work has been achieved within a PhD thesis supported by ANRT (Association Nationale de la Recherche et de la Technologie) and the FUI project *eSilence* supported by BPI France and Région Auvergne-Rhône-Alpes.

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