

**EMR'12  
Madrid  
June 2012**



Universidad  
Carlos III de Madrid

**Joint Summer School EMR'12  
“Energetic Macroscopic Representation”**



# « Energetic Macroscopic Representation (EMR) »

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## **1. EMR basic elements**

- General principles
- Source, accumulation and conversion elements
- Coupling elements

## **2. EMR of a whole system**

- Action and tuning path
- Association rules
- Example

## **3. Conclusion**

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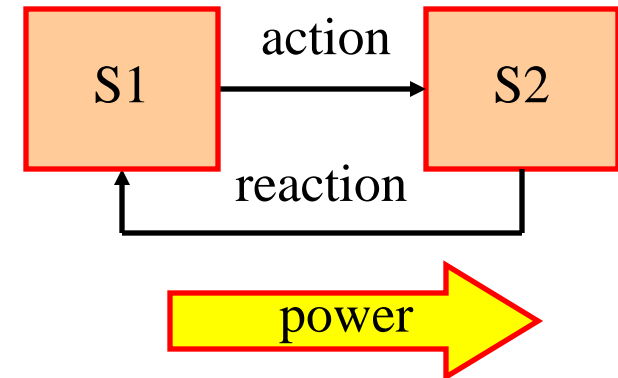
**Joint Summer School EMR'12**  
**“Energetic Macroscopic Representation”**

 **Université  
Lille1**  
Sciences et Technologies

**« EMR basic elements »**

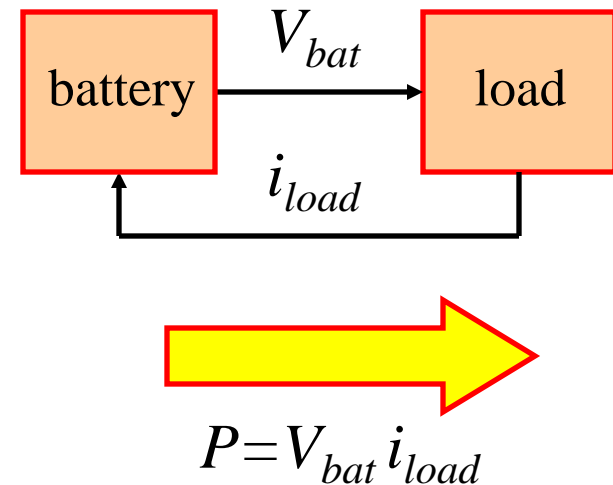
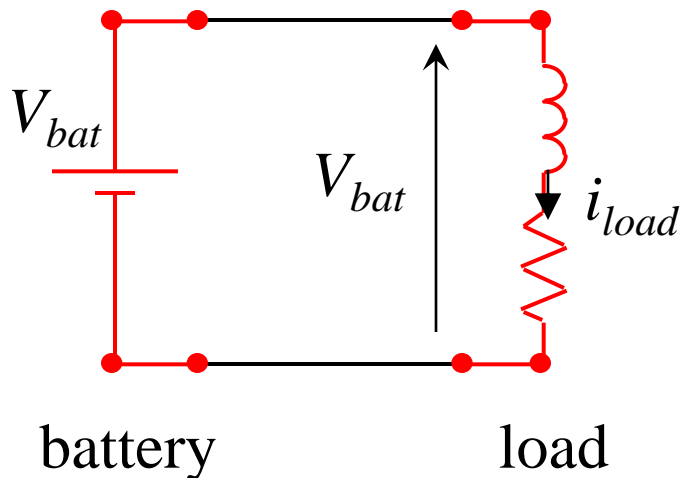
### *Interaction principle*

Each action induces a reaction

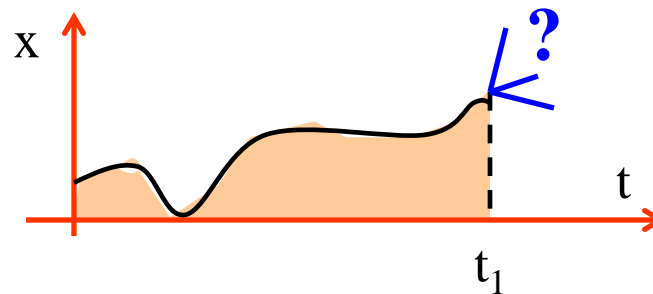


Power exchanged between S1 and S2 = action x reaction

### Example



*Principle of causality*  
physical causality is integral



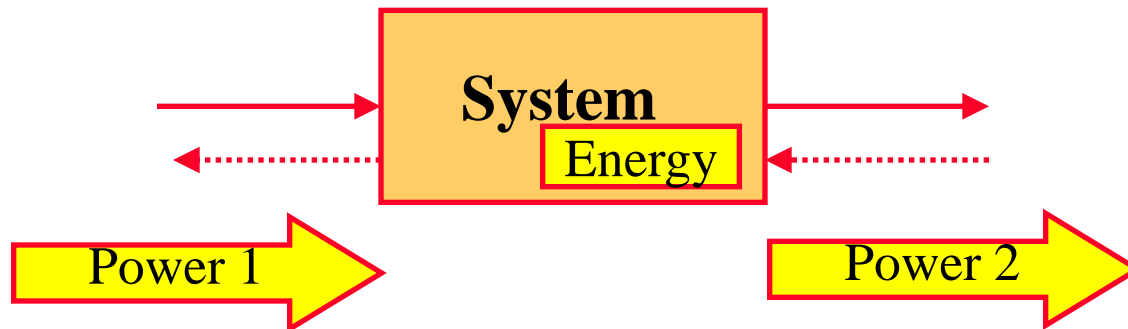
$\int x dt$   $\Rightarrow$  area  
**OK in real-time**  
 $\Downarrow$   
knowledge of past evolution

~~slope  $\leftarrow \frac{dx}{dt}$~~   
 $\Downarrow$   
**impossible in real-time**  
knowledge of future evolution

Energy is the integrative of power

$$Energie(t) = \int_0^t Power(\tau).d\tau$$

A system can store energy : in this case  $power1(t) \neq power2(t)$



Energy cannot vary instantaneously !

In fact, as :  $Power(t) = \frac{d}{dt} Energy(t)$  we would obtain  $Power(t) \rightarrow \infty$

→ Physically impossible

Energy varies thus « slowly », according to the charge and the discharge of the energy storage devices

*Examples :*

- *filling the tank of a car*
- *energy storage in the capacitors*
- *energy storage in flywheels*
- *thermal energy storage in a heater*
- *compressed air storage*
- ...

Variable linked to the stored energy

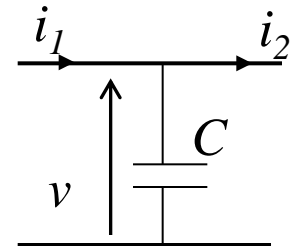
*Example :*

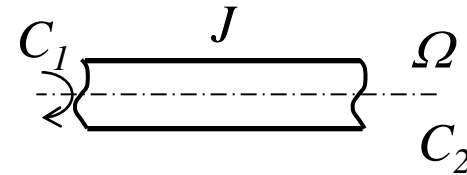
- *energy stored in a capacitor (value  $C$ ) :*

➔ *variable linked to energy = voltage  $V$*

➔ *the voltage  $V$  of a capacitor cannot vary instantaneously*

$$E = \frac{1}{2} C.V^2$$





Variable representing the stored energy

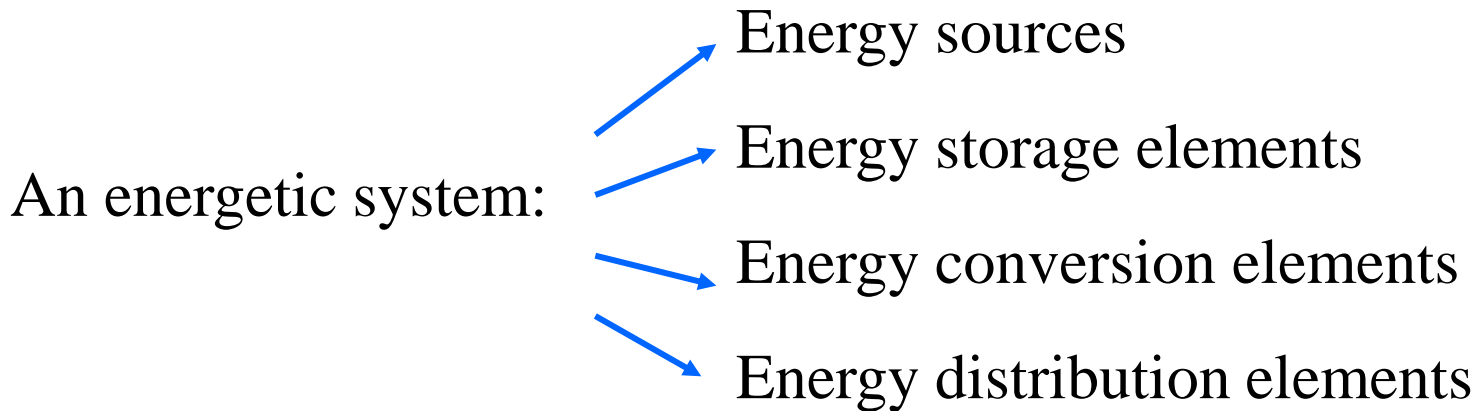
*Example :*

- energy stored in a flywheel (moment of inertia  $J$ ) :  $E = \frac{1}{2} J . \Omega^2$

- variable linked to the energy = angular speed  $\Omega$
- angular speed  $\Omega$  of a flywheel cannot vary instantaneously
- angular speed directly represents the energetic **state** of the flywheel system

State variable = Energy linked variable

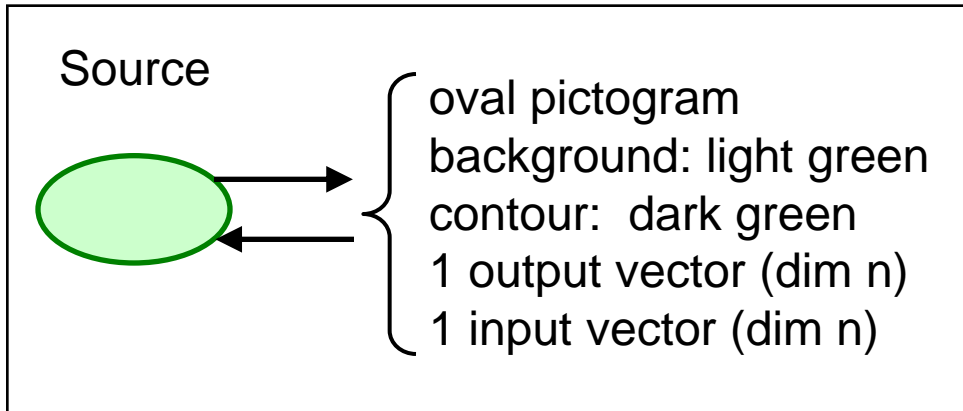




Energy storage element versus energy conversion element:

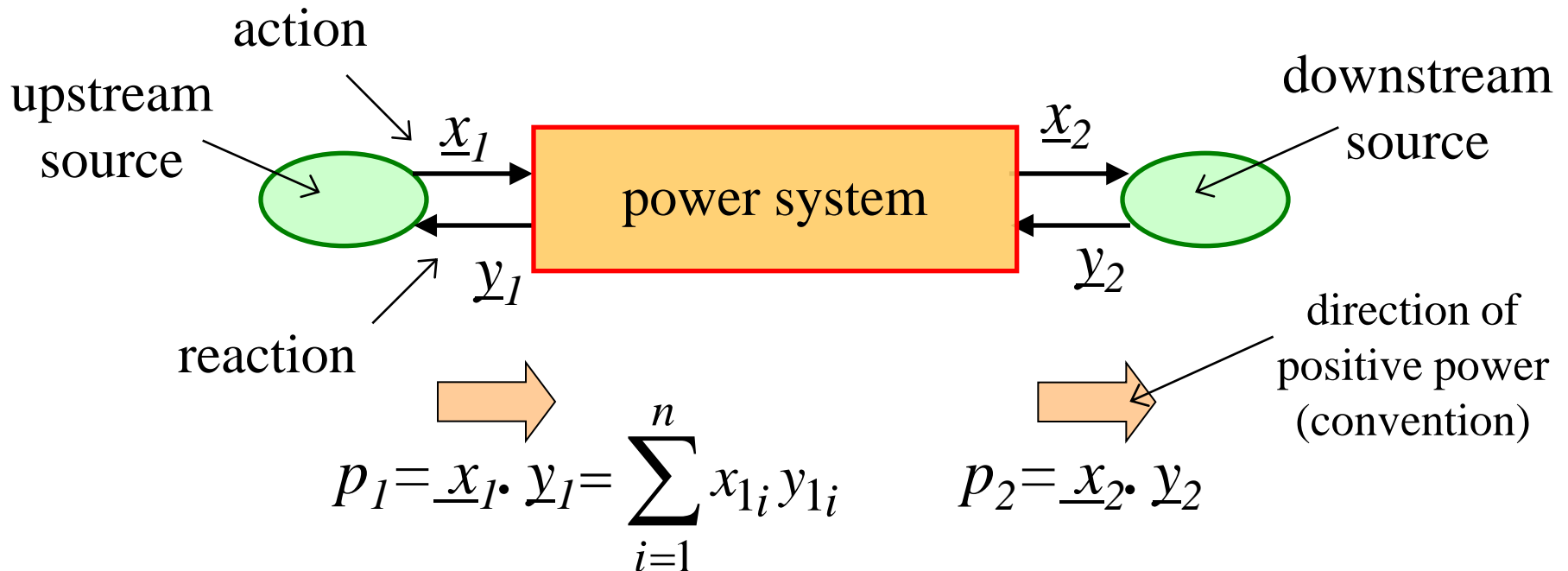
➡ Different in view of control – state variable control

➡ The state of a energy storage element can not change instantaneously

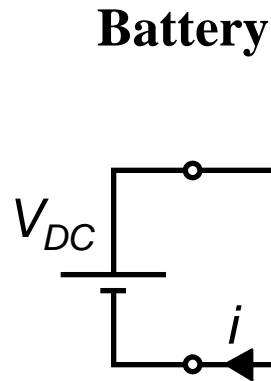


terminal elements which represent the environment of the studied system

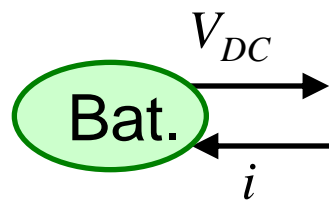
generator and/or receptor of energy



structural  
description

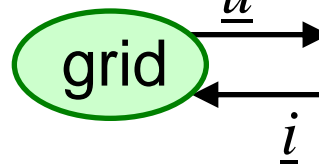
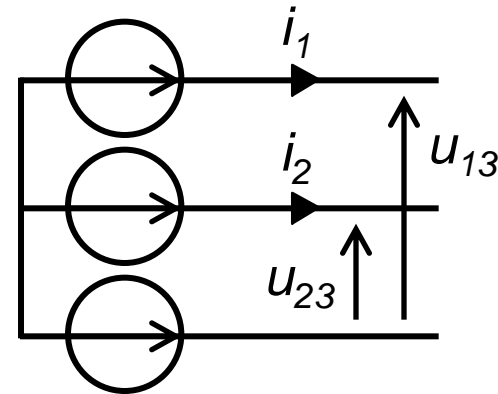


EMR  
(functional  
description)



$p = V_{DC} i$

**Electrical grid**



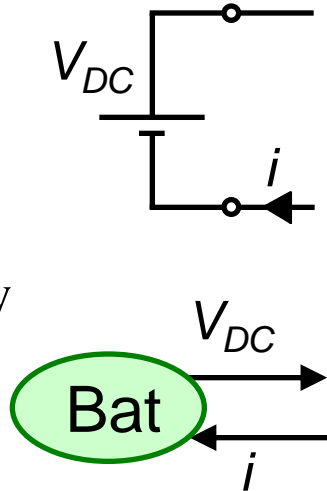
$p = \underline{u} \underline{i}$

$$\underline{u} = \begin{bmatrix} u_{13} \\ u_{23} \end{bmatrix} \quad \underline{i} = \begin{bmatrix} i_1 \\ i_2 \end{bmatrix}$$

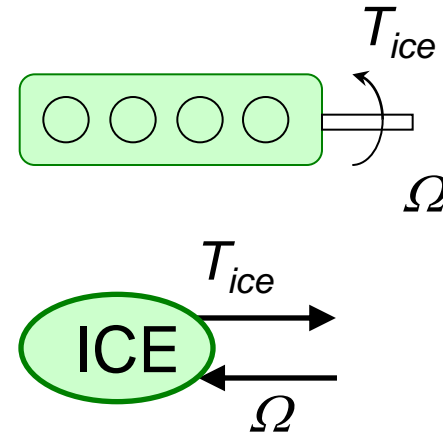
2 independent currents

2 independent voltages

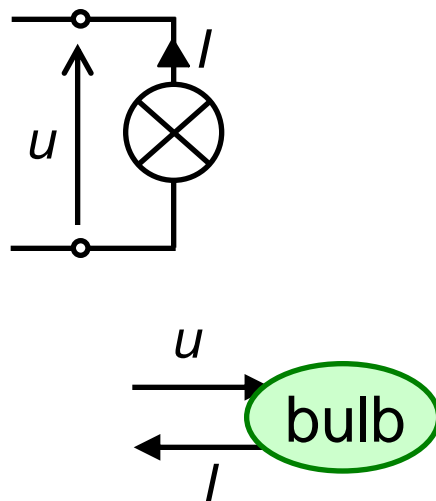
**Battery**  
(voltage source)  
generator and  
receptor of energy



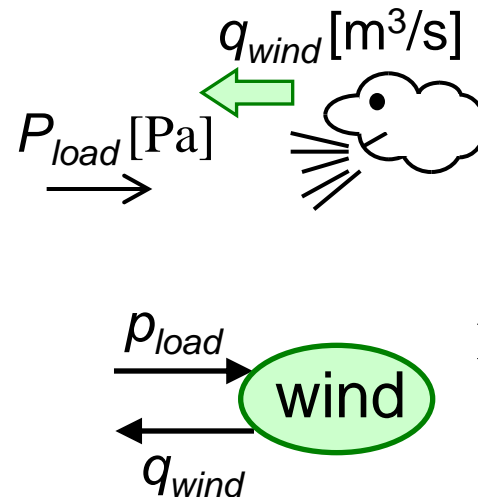
**IC engine**  
(torque source)  
Energy generator

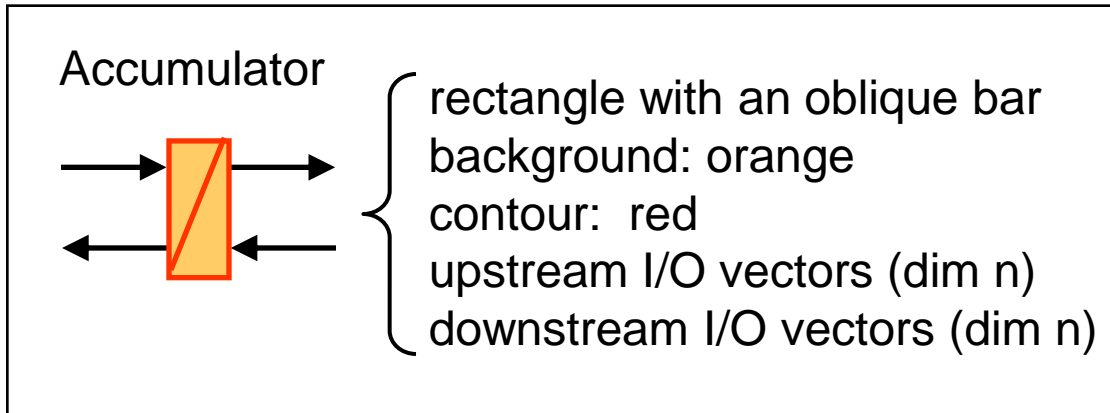


**Lighting bulb**  
Energy receptor



**Wind**  
(air flow source)  
Energy generator





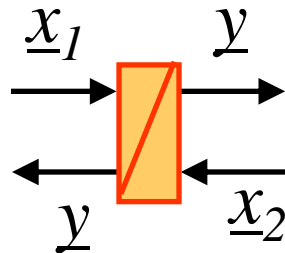
**internal accumulation of energy** (with or without losses)

**causality principle**

$$\text{output}(s) = \int \text{input}(s)$$

action

reaction



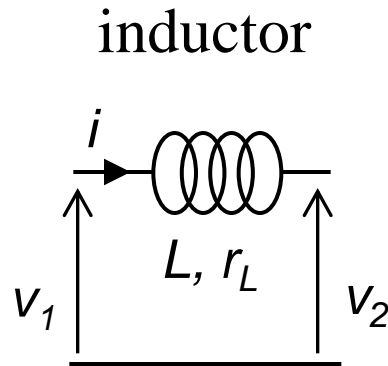
$$\underline{y} \propto \int f(\underline{x}_1, \underline{x}_2) dt$$

$\underline{y}$  = output, delayed from input changes

$p_1 = \underline{x}_1 \cdot \underline{y}$

$p_2 = \underline{x}_2 \cdot \underline{y}$

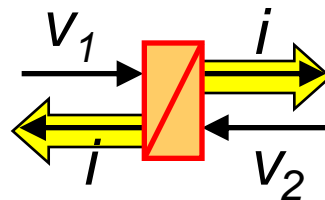
structural  
description



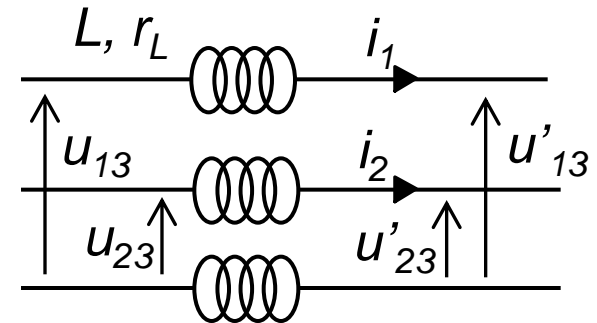
mathematical  
Model

$$L \frac{d}{dt} i + r_L i = v_1 - v_2$$

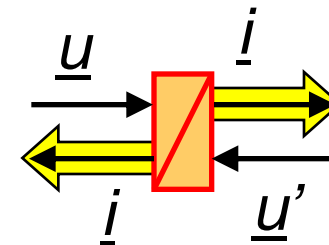
EMR (causal  
representation)

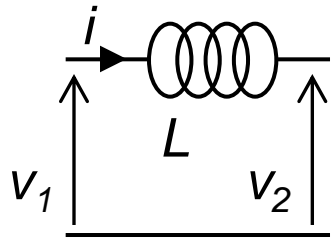


3-phase line



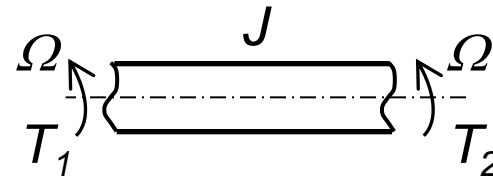
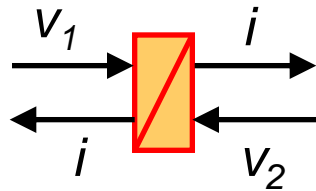
$$[L] \frac{d}{dt} \underline{i} + r_L \underline{i} = \frac{1}{3} \begin{bmatrix} 2 & -1 \\ -1 & 2 \end{bmatrix} (\underline{u} - \underline{u}')$$





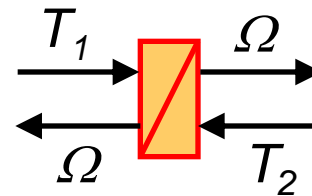
inductor

$$E = \frac{1}{2} L i^2$$



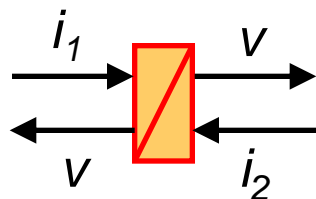
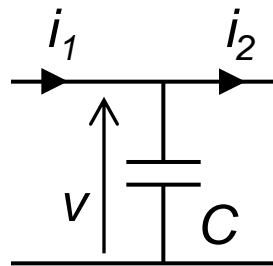
inertia

$$E = \frac{1}{2} J \Omega^2$$



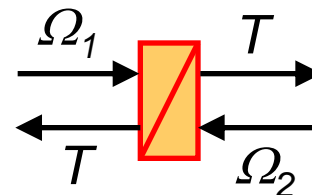
capacitor

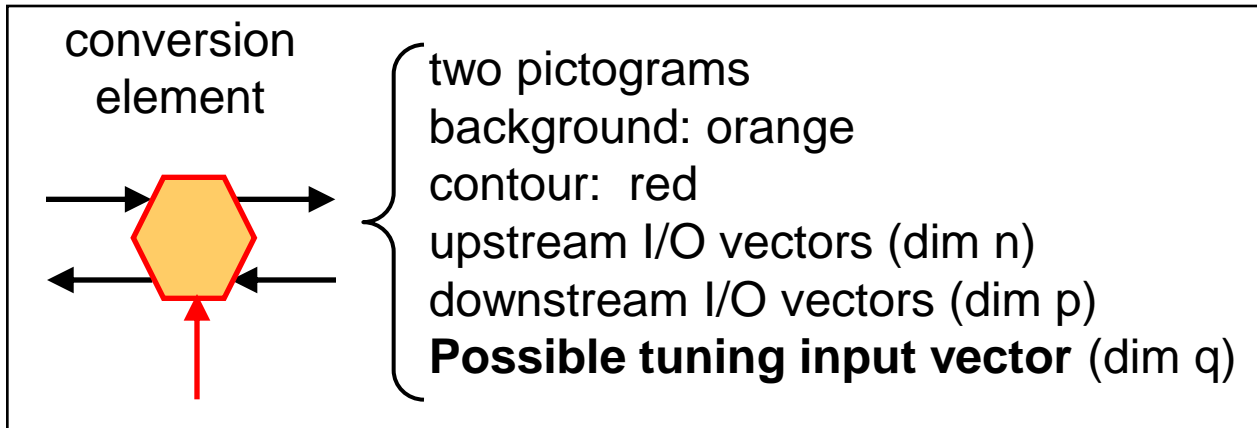
$$E = \frac{1}{2} C v^2$$



stiffness

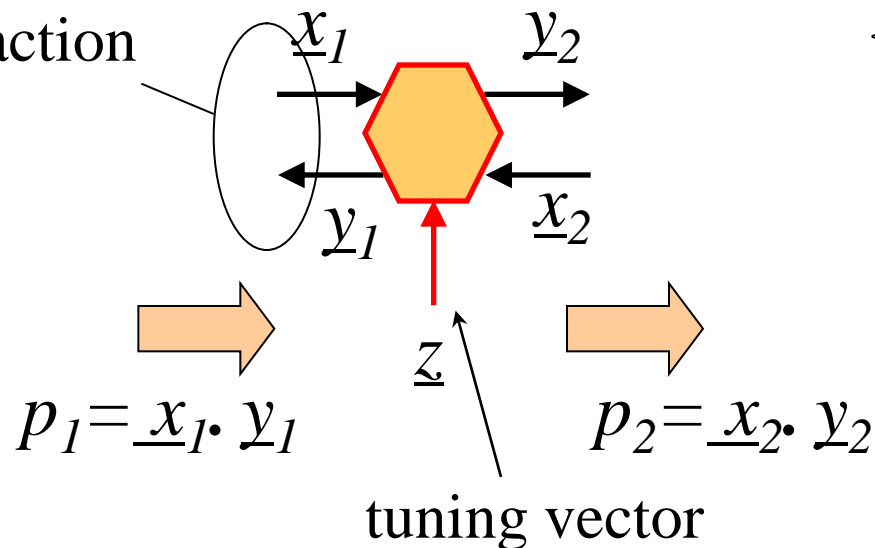
$$E = \frac{1}{2} \frac{1}{k} T^2$$





**conversion of energy  
without energy  
accumulation**  
(with or without  
losses)

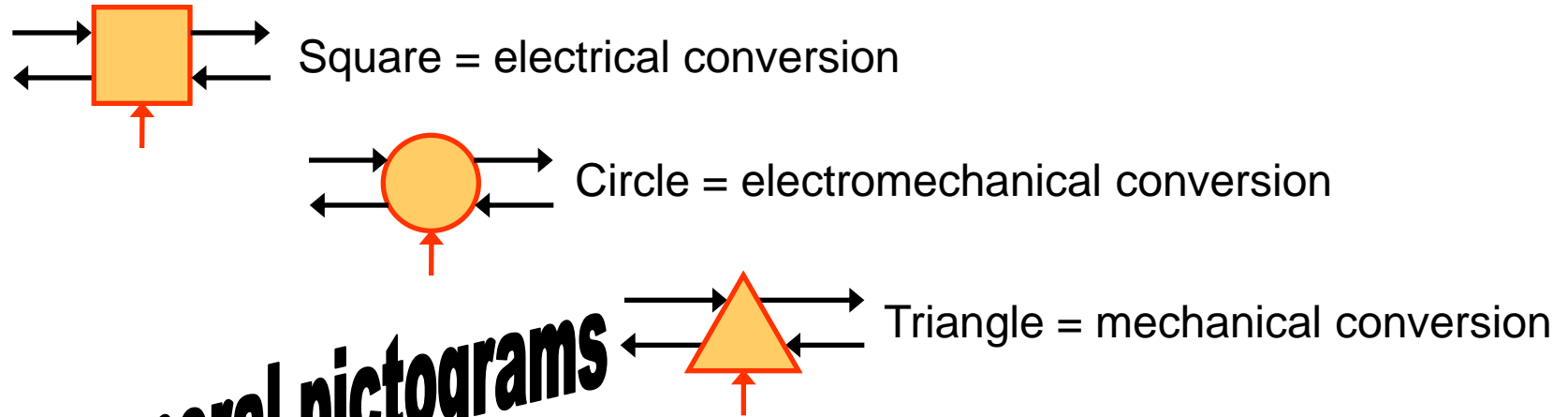
action /  
reaction



$$\begin{cases} \underline{y}_2 = f(\underline{x}_1, \underline{z}) \\ \underline{y}_1 = f(\underline{x}_2, \underline{z}) \end{cases} \text{ no delay!}$$

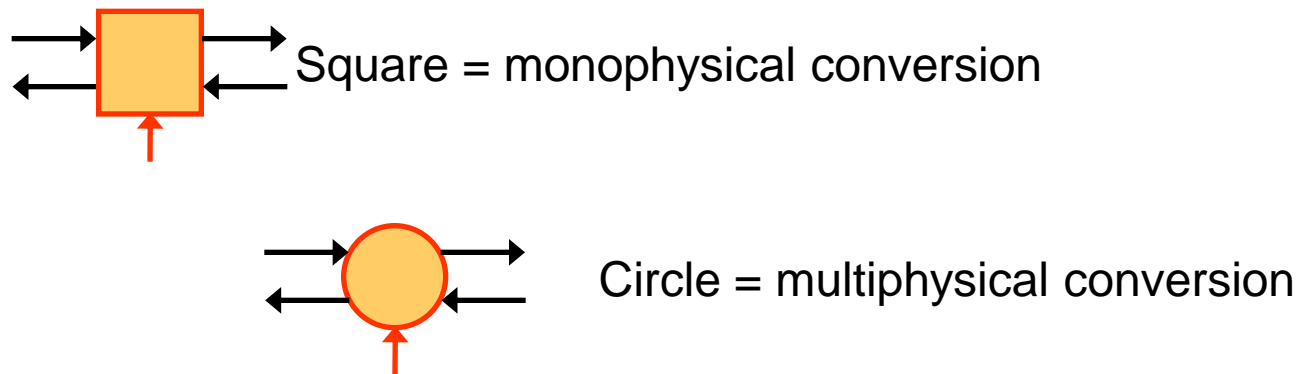
upstream and downstream  
I/O can be permuted  
(floating I/O)

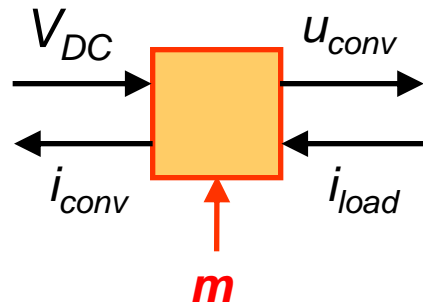
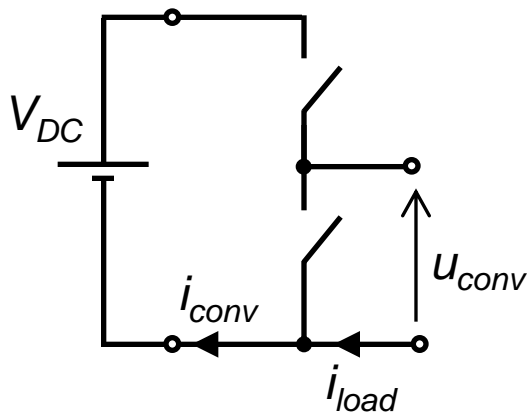
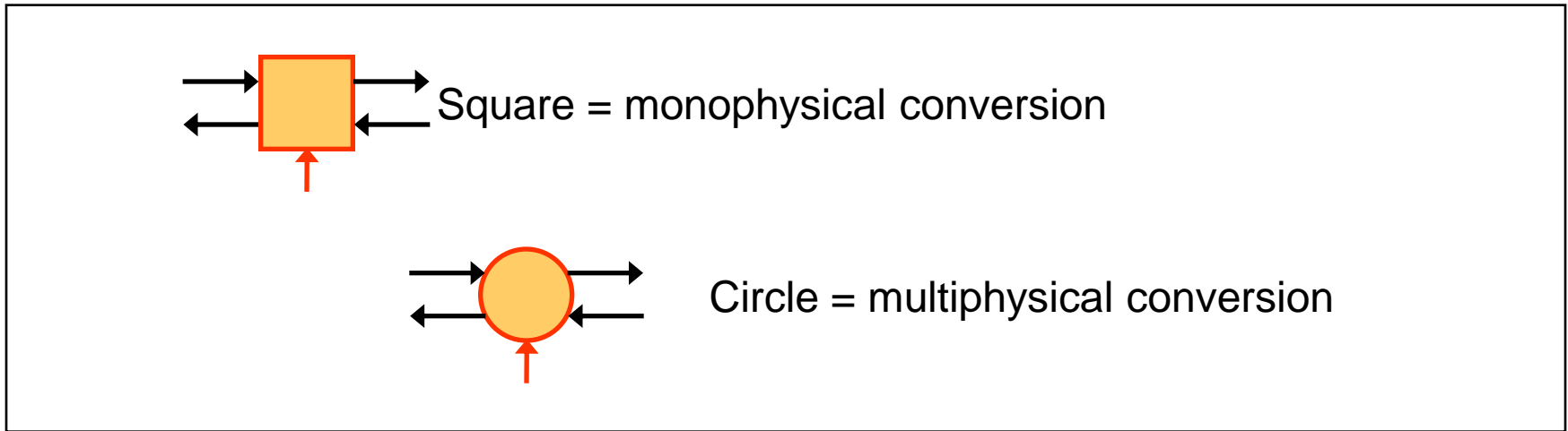




**More general pictograms**

**For multiphysical systems**

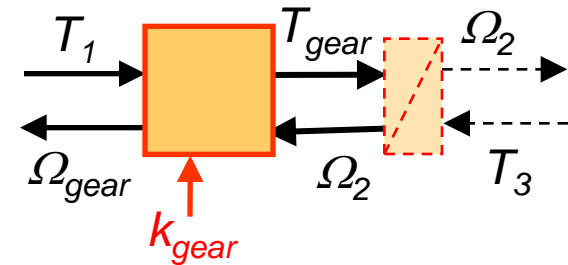
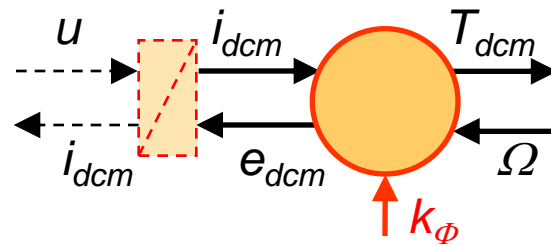
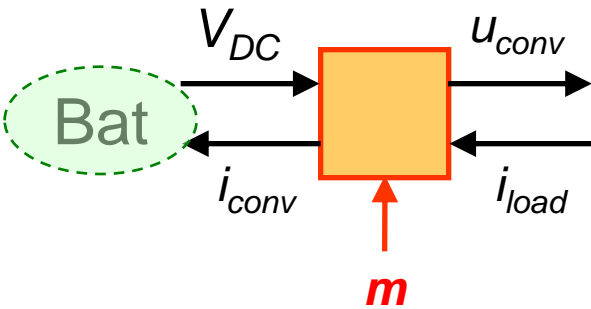
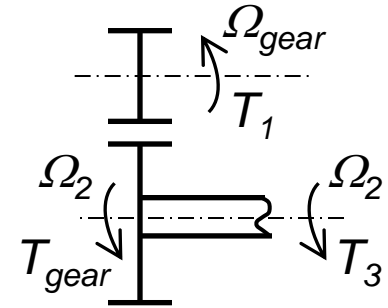
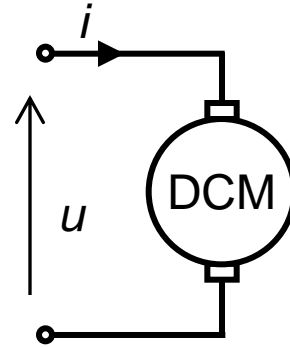
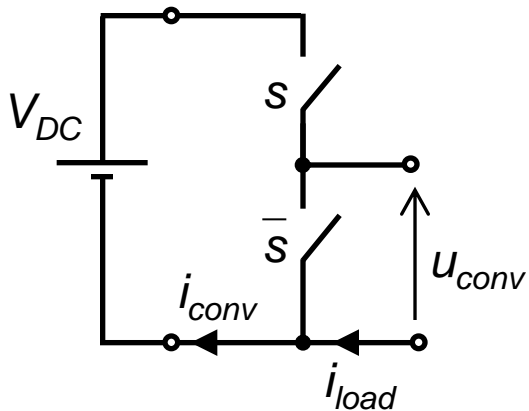




$$\begin{cases} u_{conv} = m V_{DC} \\ i_{conv} = m i_{load} \end{cases}$$

$m$ : modulation function of the converter

$$\langle m \rangle = D = \text{duty cycle}$$



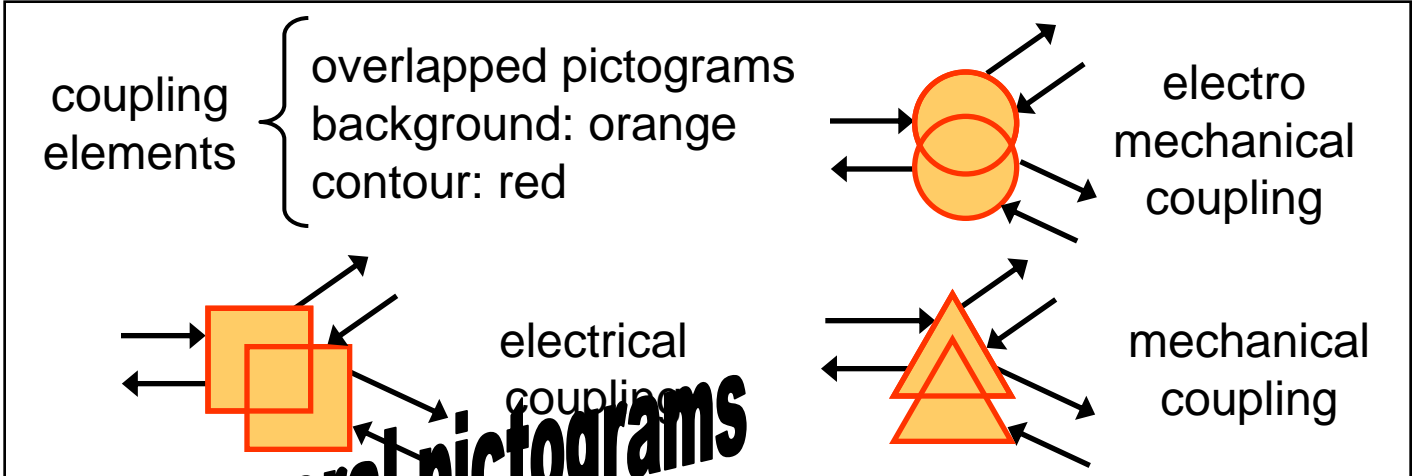
$$\begin{cases} u_{conv} = m V_{DC} \\ i_{conv} = m i_{load} \end{cases}$$

$$L \frac{d}{dt} i_{dcm} + r i_{dcm} = u - e_{dcm}$$

$$\begin{cases} T_{dcm} = k_{\phi} i_{dcm} \\ e_{dcm} = k_{\phi} \Omega \end{cases}$$

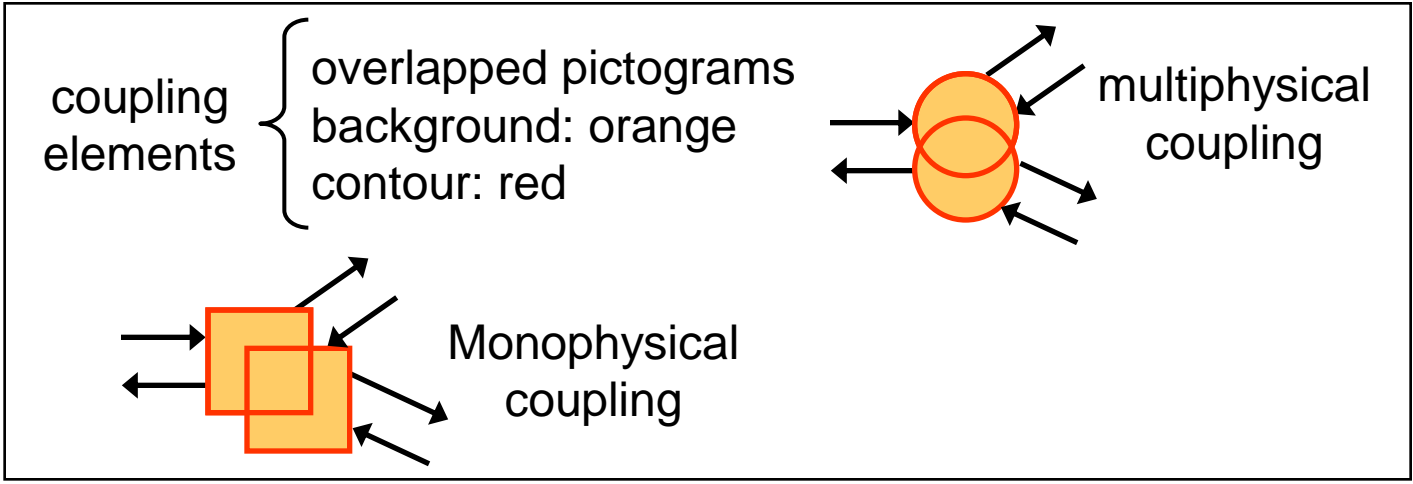
$$\begin{cases} T_{gear} = k_{gear} T_1 \\ \Omega_{gear} = k_{gear} \Omega_2 \end{cases}$$

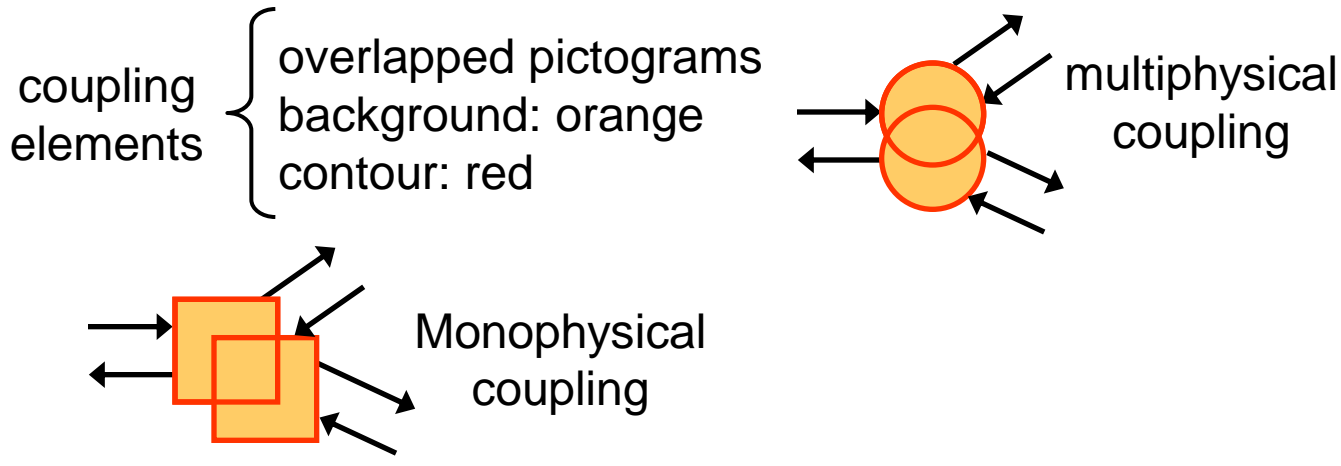
$$J \frac{d}{dt} \Omega_2 = T_{gear} - T_3$$



distribution  
of energy

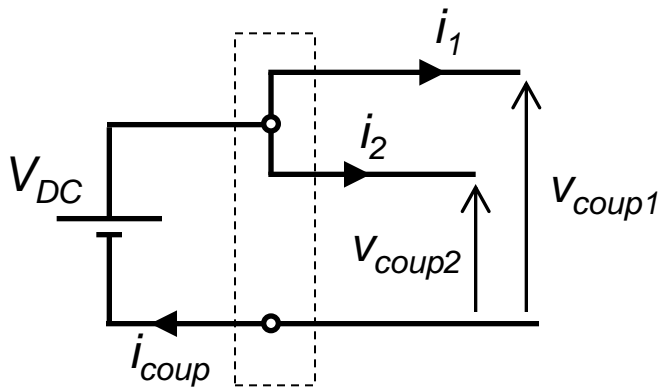
no tuning  
vector



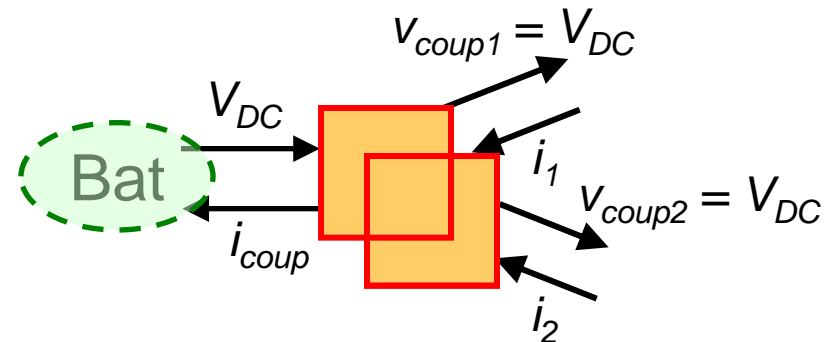


distribution  
of energy

no tuning  
vector

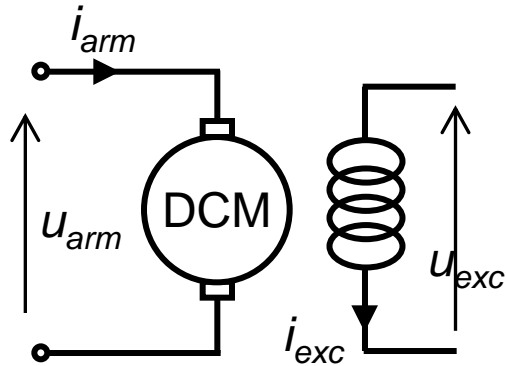


parallel connexion

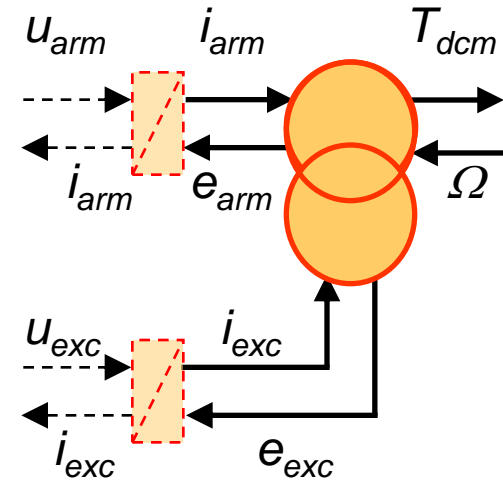


$$\begin{cases} V_{DC} \text{ common} \\ i_{coup} = i_1 + i_2 \end{cases}$$

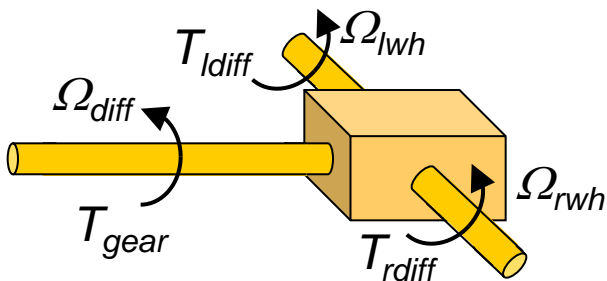
### Field winding DC machine



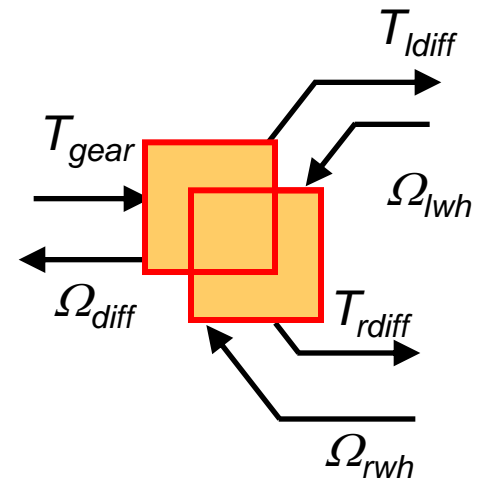
$$\begin{cases} T_{dcm} = k i_{exc} i_{arm} \\ e_{dcm} = k i_{exc} \Omega \end{cases}$$



### Mechanical differential



$$\begin{cases} T_{ldif} = T_{rdif} = \frac{T_{gear}}{2} \\ \Omega_{diff} = \frac{\Omega_{lwh} + \Omega_{rwh}}{2} \end{cases}$$



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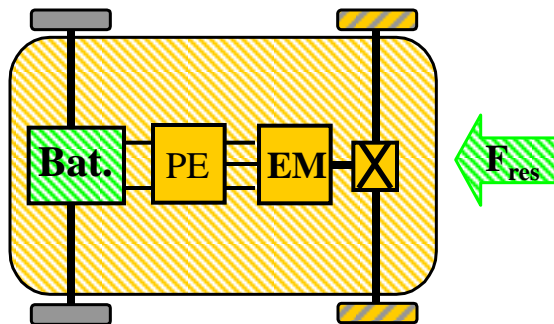
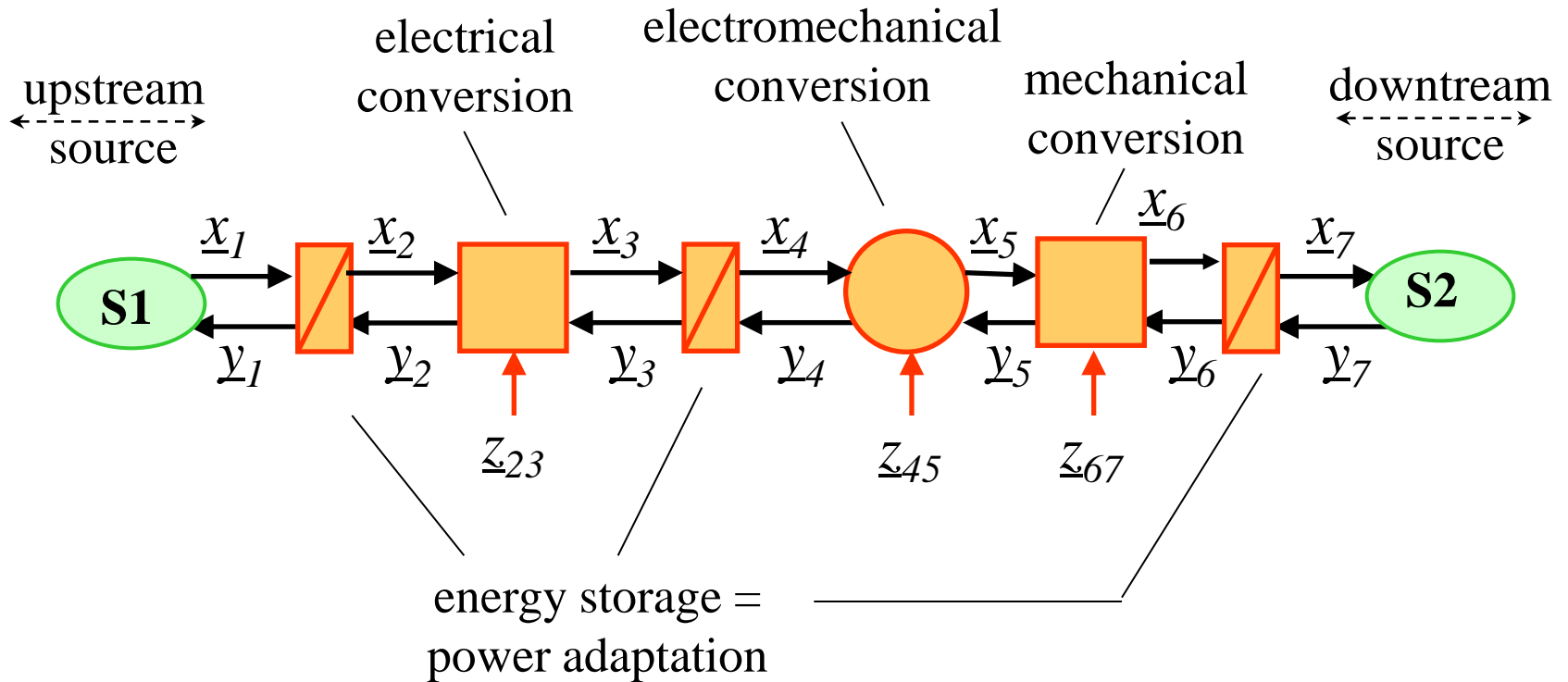
**« EMR of a whole system »**

# « Energetic Macroscopic Representation »

## - Example of an electromechanical conversion system -

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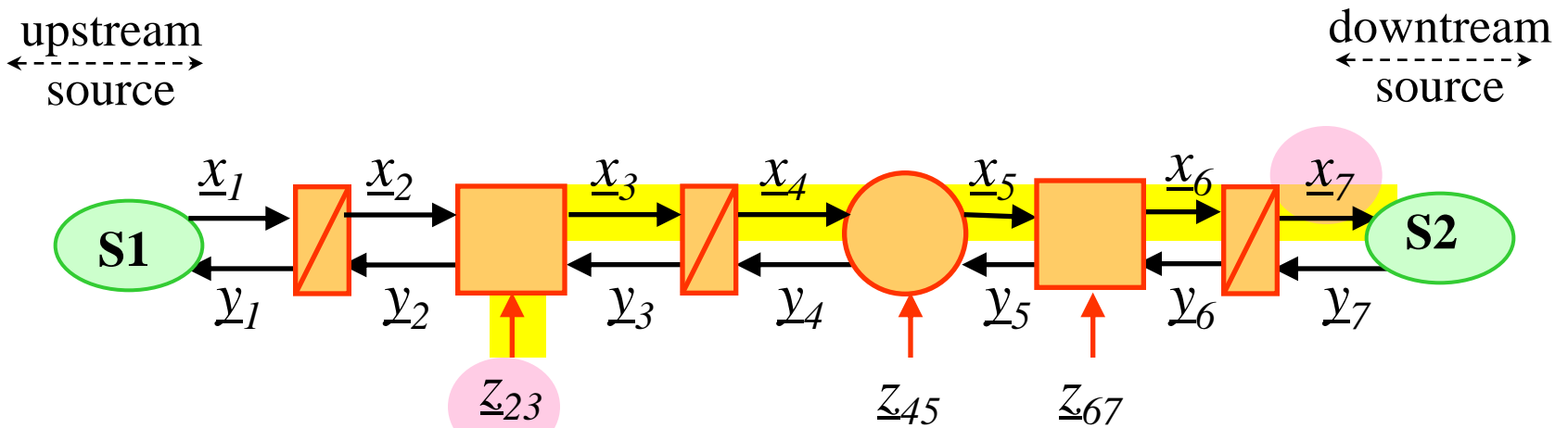
29



upstream source  $\longrightarrow$  downstream source

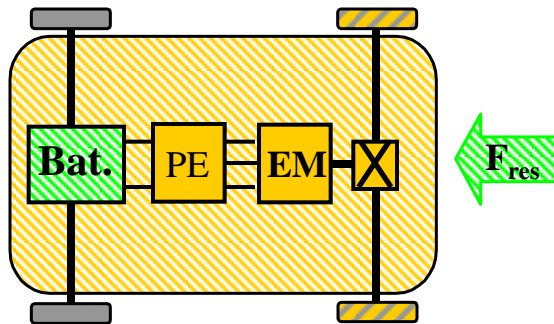
**Convention:** direction of positive power flow (could be negative for bidirectional system)





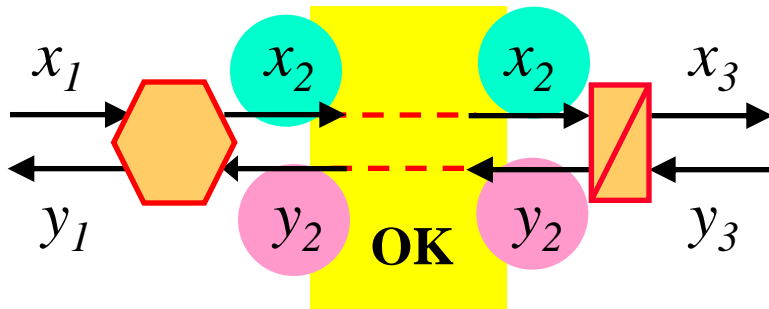
Technical requirements: action on  $z_{23}$  and  $x_7$  to be controlled

Tuning path:  $\begin{matrix} \rightarrow x_3 \rightarrow x_4 \rightarrow x_5 \rightarrow x_6 \rightarrow x_7 \\ \uparrow \\ z_{23} \end{matrix}$



The tuning path is **independent of the power flow direction**

(e.g. velocity control in acceleration AND regenerative braking)



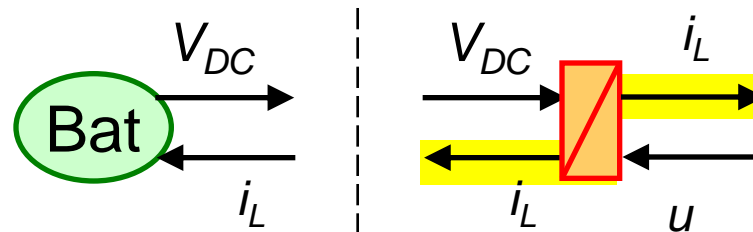
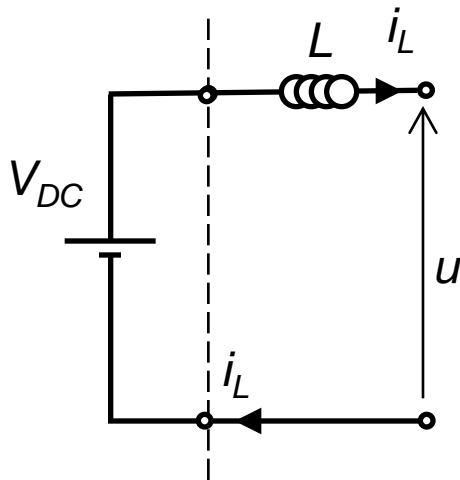
direct connection if:

$$\text{Out}(S1) = \text{In}(S2)$$

$$\text{In}(S1) = \text{Out}(S2)$$

S1 and S2 any sub-systems

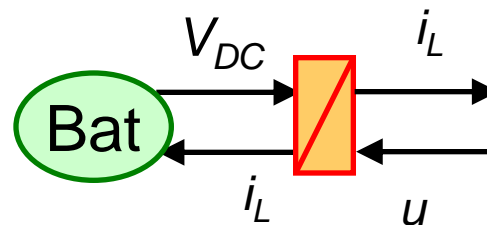
Example

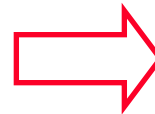
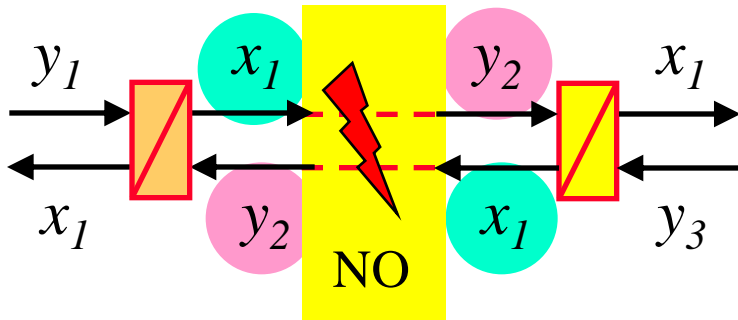


$$L \frac{d}{dt} i_L = V_{DC} - u$$

↓

**i state variable**

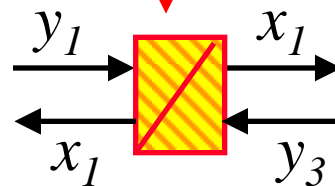




2 accumulation elements  
would impose the same  
state variable  $x_1$

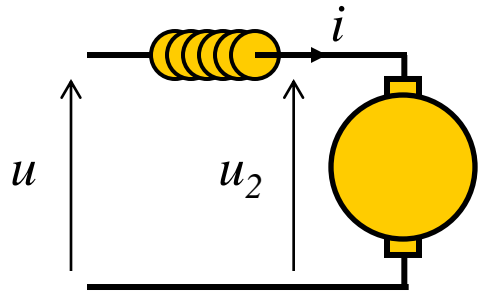
**Conflict of association**

*merging*

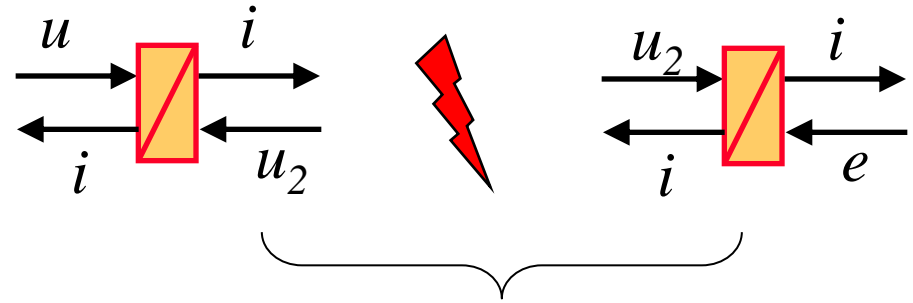
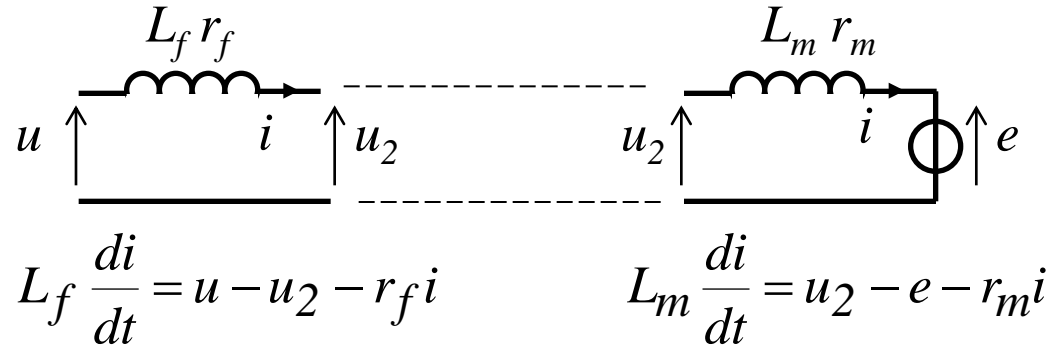


1 equivalent function for  
2 elements / systemic

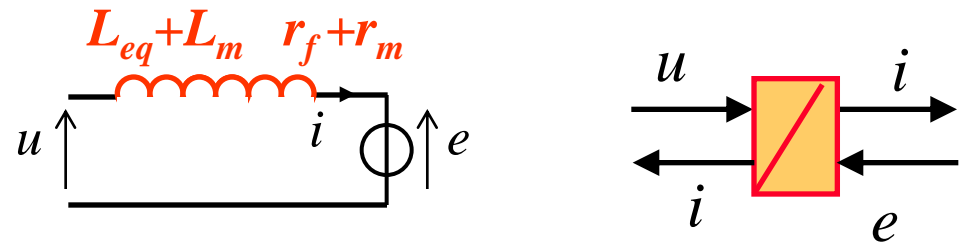
DC machine and smoothing inductor

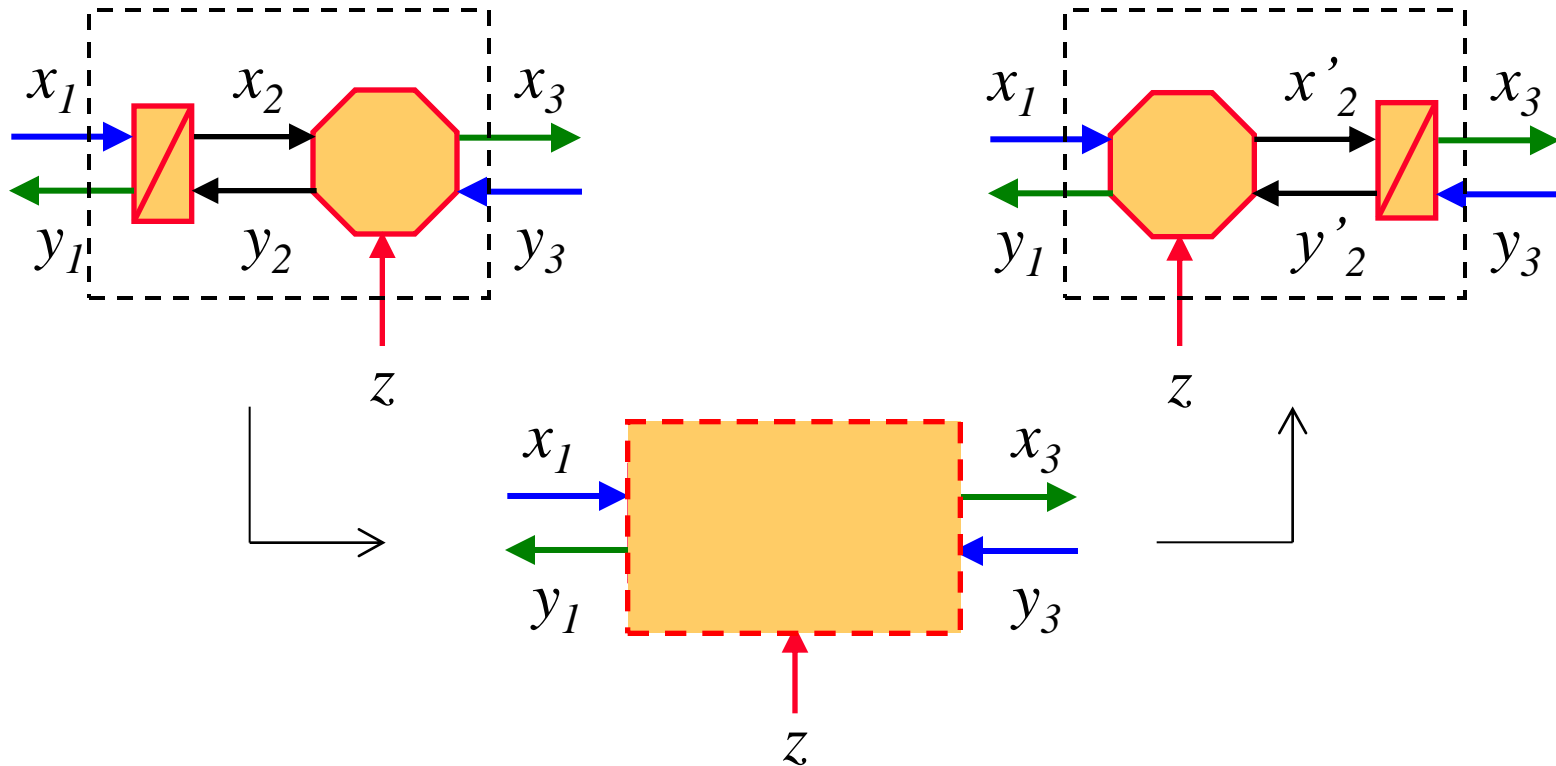


Assumption:  $L_f$   $L_m$  constant

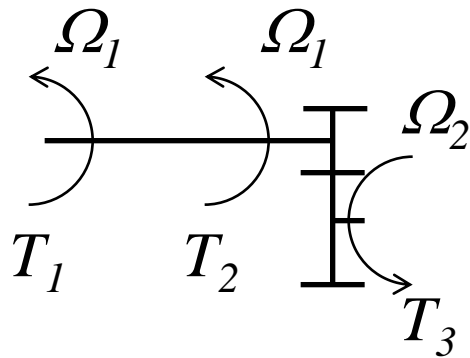


$$(L_f + L_m) \frac{di}{dt} = u - e - (r_f + r_m) i$$



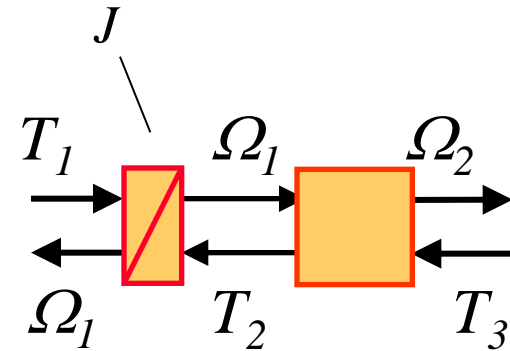


permutation possible if same global behavior:  
strictly the same effects ( $y_1$  and  $x_3$ ) from the same causes ( $x_1$ ,  $y_3$  and  $z$ )



$$J \frac{d}{dt} \Omega_1 = T_1 - T_2$$

$$\begin{cases} T_2 = k T_3 \\ \Omega_2 = k \Omega_1 \end{cases}$$



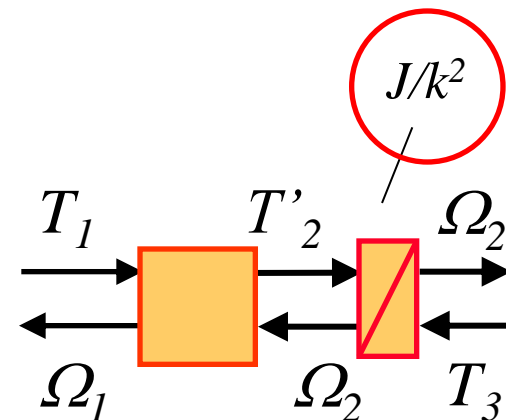
Shaft + gearbox

variable change

$$\frac{J}{k^2} \frac{d}{dt} \Omega_2 = T'_2 - T_3$$

$$\begin{cases} T'_2 = \frac{1}{k} T_1 \\ \Omega_1 = \frac{1}{k} \Omega_2 \end{cases}$$

no assumption  
strict equivalence  
(same model)



# « Energetic Macroscopic Representation »

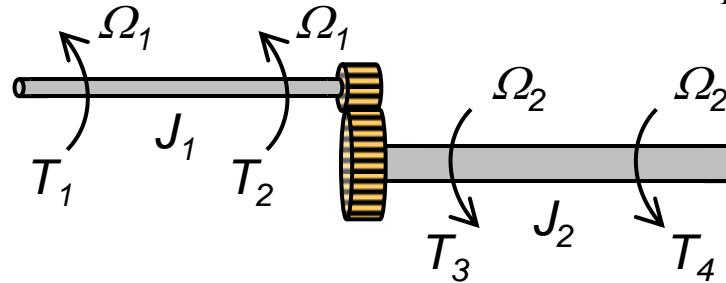
## - Interest of rules -

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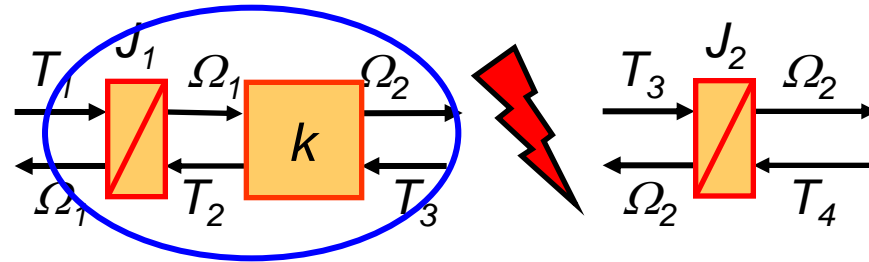
### Assumptions:

$J_1, J_2$  constant  
no backlash

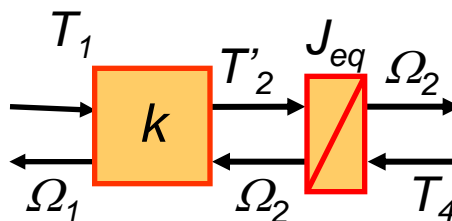
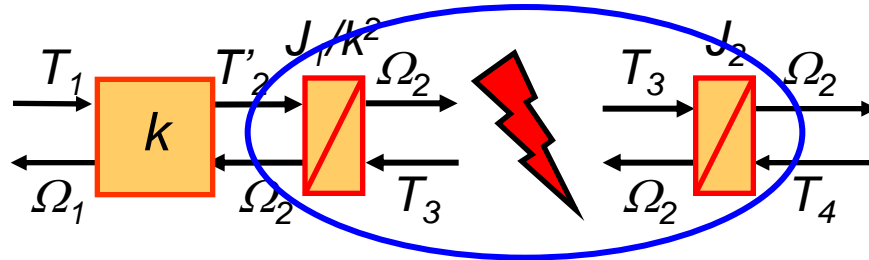


to solve conflict of association

permutation



merging



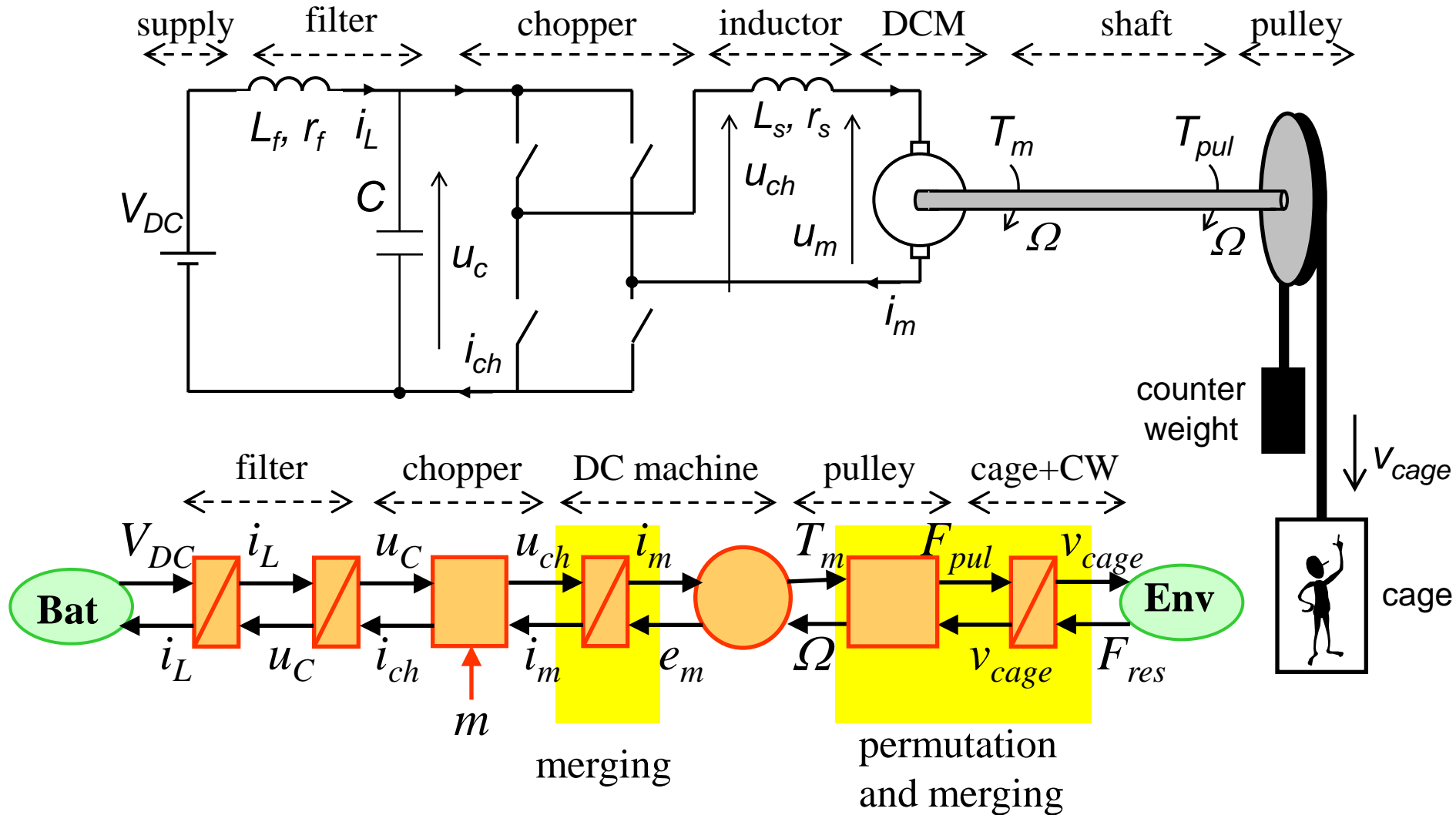
$$J_{eq} = \frac{J_1}{k^2} + J_2$$

# « Energetic Macroscopic Representation »

## - Lift example: EMR -

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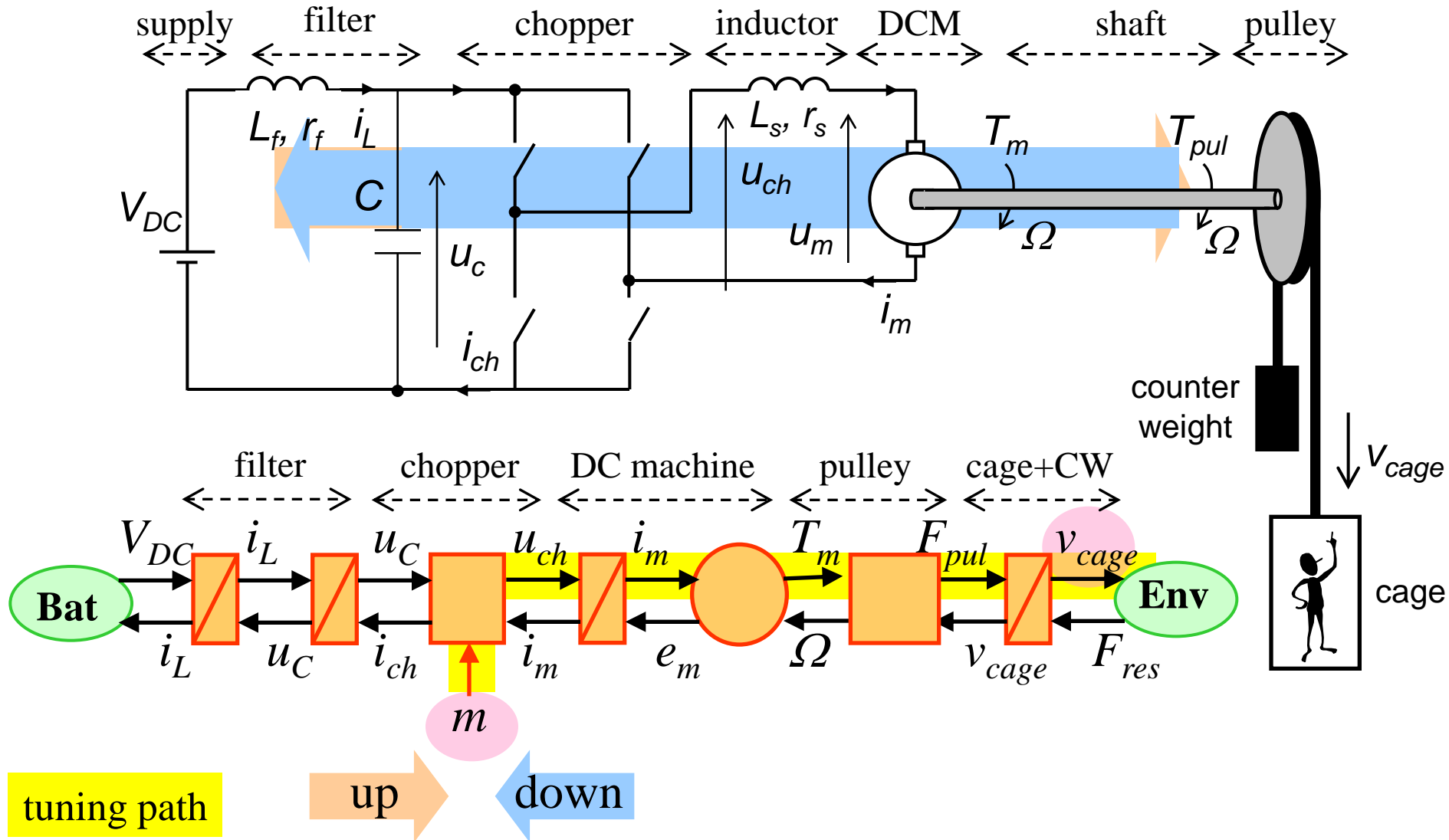


# « Energetic Macroscopic Representation »

## - Lift example: tuning path -

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**Madrid**  
**June 2012**

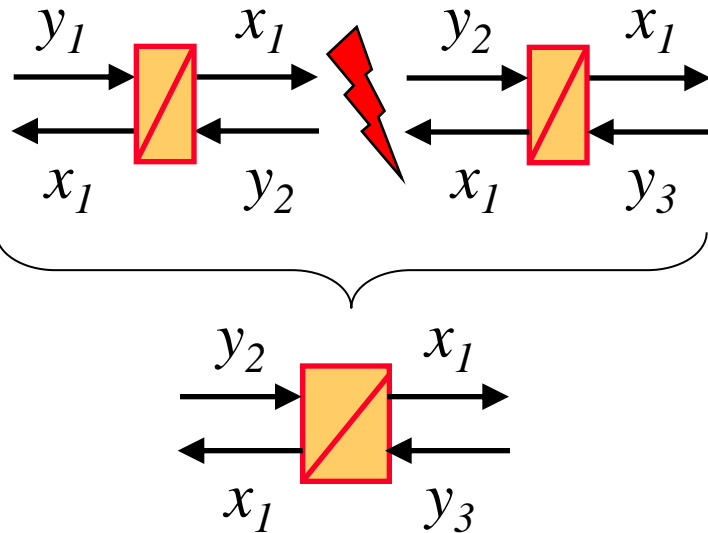


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**“Energetic Macroscopic Representation”**

 **Université  
Lille1**  
Sciences et Technologies

**« Conclusion »**



Priority to the function  
by keeping the physical causality  
(systemic)

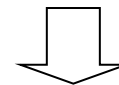
EMR describes energetic  
functions

EMR respects natural  
integral causality

I/O are independent  
of power flows

Tuning paths:

- defined by the technical requirements
- independent of the power flow direction



EMR is adapted for control design

**EMR'11**  
**Lausanne**  
**July 2011**



**Joint Summer School EMR'11**  
**“Energetic Macroscopic Representation”**



# « **BIOGRAPHIES AND REFERENCES** »

# « Energetic Macroscopic Representation »

## - Authors -

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