NUMERICAL SIMULATION AND EXPERIMENTAL VALIDATION OF GAP SUPPORTED TUBE SUBJECTED TO FLUID-ELASTIC COUPLING FORCES FOR HYBRID CHARACTERIZATION TESTS

Wissam BENMALEK  
EDF & CNRS FEMTO-ST Institute  
Clamart, France

Manuel COLLET  
CNRS FEMTO-ST Institute  
Besançon, France

Emmanuel FOLTETE  
CNRS FEMTO-ST Institute  
Besançon, France

Morvan OUISSE  
CNRS FEMTO-ST Institute  
Besançon, France

Mathieu CORUS  
EDF  
Clamart, France

ABSTRACT
Steam Generator (SG) tubes are subjected to fluid-elastic coupling forces and impacts against support plates & anti-vibration bars. Understanding their vibrations is crucial not only at the design stage, but also to optimize the SG maintenance policy and to lengthen the SG service life. The aim of our research is to provide a better understanding of the conjugate stabilizing effects of impacts and coupling with fluid-elastic forces. Since fluid-elastic forces are difficult to simulate and expensive to reproduce experimentally, the fluid coupling forces of our numerical model are represented using velocity dependent damping and stiffness matrices, both for the fluid and the tube. Their effect is experimentally reproduced having recourse to active vibration control in the frame of specifically designed “hybrid” experimental tests. In this paper, we present a method for modeling tube vibrations in order to estimate the conjugate effects of the coupling between the fluid elastic forces and impacts. This strategy lowers the costs and avoids the difficulties associated to the case of fluid in the experiments. Our numerical model will be implemented in the active control loop in the next step of the study.

NOMENCLATURE

- $b$: Influence vector
- $C$: Structural damping Matrix
- $C_{da}$: Dimensionless damping coupling coefficient
- $C_{ff}$: Added fluid damping Matrix
- $D$: Tube diameter
- $Ec$: Kinetic energy
- $Em$: Mechanical energy
- $Ep$: Potential energy
- $Epc$: Impact potential energy
- $F_{c}$: Impact force
- $F_{fe}$: Fluid elastic force
- $F_T$: Turbulence force
- $f$: Frequency vibration
- $f_R$: Rice frequency
- $g$: Gap distance
- $\mathcal{K}$: Structural stiffness matrix
- $K_{c}$: Impact stiffness
- $K_{ff}$: Added fluid stiffness
- $k_f$: Modal added fluid stiffness
- $M$: Structural mass matrix
- $M_c$: Mass Impact
- $M_f$: Added fluid mass
- $m_f$: Modal added fluid mass
- $q$: Generalized modal coordinates
- $T_c$: Impact duration
- $t$: Time
- $V$: Fluid velocity
- $V_r$: Dimensionless reduced fluid velocity
- $x_c$: Coordinate gap impact
- $\rho_f$: Mass density of the fluid
- $\rho$: RMS value
- $\omega_n$: Modal circular frequency (mode $n$)
- $\zeta_n$: Modal damping (mode $n$)
- $\varphi_n$: Eigenvector (mode $n$)
- $\phi$: Eigenvector matrix
- $(*)_n$: Mode $n$
- $(*)_{(n)}$: Iteration $n$
- $(*)_0$: Stagnant water ($V = 0$)
INTRODUCTION

Steam generators are heat exchangers used to convert water into steam from heat produced in a nuclear reactor core. They are used in pressurized water reactors between the primary and secondary coolant loops.

The studied structure Fig.2 is composed of a tube attached to a slender plate clamped in rigid block. At the middle height of the tube, two gap stops located at 0.5mm create punctual impacts depending on the vibration amplitude of the tube.

A finite element shell model was developed to generate the mass, damping and stiffness matrices. This model was updated in order to match the numerical behavior with experimental one. Two criterions were used to compare the numerical and experimental model: Modal Assurance Criterion (MAC) and frequency error criterion. Fig.3 & Tab.1 summarizes the results obtained for the 6 first modes.

It can be observed that there is a good agreement between the two models. The lowest values of MAC is 85% and the mean frequency error is lower than 4%.

Where $\ddot{q}, \dot{q}, q$ are generalized acceleration, velocity and displacement vectors. Because these mechanisms are complex and difficult to realize in an experimental set up, the main aim of our study is to develop a hybrid control loop to simulate this coupling effect in the frame of an experimental characterization test bench.

STRUCTURE & MODAL UPDATING

Experimental characterization test bench.

The lowest values of frequency error are 3% for the mode 2, 3% for the mode 5 and 8% for the mode 6. These mechanisms are complex and difficult to develop in a laboratory. Therefore, we have to simulate them with a hybrid control loop to match the numerical behavior with experimental one. Two criterions were used to compare the numerical and experimental model: Modal Assurance Criterion (MAC) and frequency error criterion. Fig.3 & Tab.1 summarizes the results obtained for the 6 first modes.

<table>
<thead>
<tr>
<th>Modes</th>
<th>Numerical modal frequency</th>
<th>Experimental modal frequency</th>
<th>Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>23.1</td>
<td>23.1</td>
<td>~0%</td>
</tr>
<tr>
<td>2</td>
<td>103</td>
<td>100</td>
<td>3%</td>
</tr>
<tr>
<td>3</td>
<td>305</td>
<td>318</td>
<td>4%</td>
</tr>
<tr>
<td>4</td>
<td>426</td>
<td>407</td>
<td>4.5%</td>
</tr>
<tr>
<td>5</td>
<td>774</td>
<td>798</td>
<td>3%</td>
</tr>
<tr>
<td>6</td>
<td>1300</td>
<td>1404</td>
<td>8%</td>
</tr>
</tbody>
</table>

Tab 1. Frequency error

It can be observed that there is a good agreement between the two models. The lowest values of MAC is 85% and the mean frequency error is lower than 4%.
EXPERIMENTAL IDENTIFICATION

Impact stiffness:

The only source of nonlinearity in our problem comes from the impact forces located at \( x_c \) (middle height of tube), which are computed in an explicit manner as the Eq.(4) shows.

\[
\begin{cases} 
F_c(t) = K_c (y(x_c,t) - g) & \text{if } |y(x_c,t)| > g \\
F_c(t) = 0 & \text{if } |y(x_c,t)| \leq g 
\end{cases}
\]

(4)

Where \( K_c \) is the impact stiffness. The value of the parameter \( K_c \) is identified through experimental measurements. Several impact tests were performed in which the impact forces where measured by using force sensor. Knowing the mass sensor \( M_c \) and measuring the duration of the impact \( 'T_c' \), we can deduce an estimation of the impact stiffness using the following approximation:

\[
T_c = \frac{\pi}{\omega_c} = \pi \sqrt{\frac{m_c}{K_c}}
\]

(5)

Figure 4. Impact stiffness identification

Figure 4 presents a histogram of the obtained results for 25 tests. \( K_c \) was estimated at \( 10^6 \)N/m on average (for \( T_c = 0.3 \)ms on average), which matches with the results found by P.Piteau [4] & T.Thenint[5].

Fluid-elastic forces parameters:

In order to model fluid-elastic forces, a significant research effort has been conducted over the last four decades. These researches led to several theoretical models. We can quote M.Paidoussis [6], S.Price [7] or S.Granger [8] models etc. In our study we have chosen the CEA one [9] which is semi-analytical model. In this approach, the parameters \( M_f, C_f \) and \( K_f \) are identified experimentally.

Referring to works carried out by CEA [4], the first mode is predominant in the tube response and the effects of higher modes are almost negligible, thus the fluid elastic force is projected only on the first mode and the other modes are not influenced.

\[
f_{f,e}(\dot{q}, \ddot{q}, q) = -(m_f \ddot{q} + c_f(V_f) \dot{q} + k_f(V_f)q)
\]

(6)

Therefore, the fluid-elastic effect can be finally modeled as fluid added mass, fluid added damping and fluid added stiffness. These last two coefficients are assumed depending on reduced fluid velocity \( V_f \) [4].

\[
\begin{bmatrix} m_1 + m_f & 0 & 0 \\ 0 & m_2 & 0 \\ 0 & 0 & 0 \end{bmatrix} \ddot{q} + \begin{bmatrix} c_1 + c_f(V_f) & 0 & 0 \\ 0 & c_2 & 0 \\ 0 & 0 & k_2 \end{bmatrix} \dot{q} + \begin{bmatrix} k_1 + k_f(V_f) & 0 & 0 \\ 0 & k_2 & 0 \\ 0 & 0 & 0 \end{bmatrix} q = f_t + f_c
\]

(7)

At this stage, in order to completely identify fluid-elastic forces we should determine the three parameters \( m_f, c_f(V_f) \) and \( k_f(V_f) \). The modal characteristics of the structure are assumed to be known in the air and the fluid-added mass \( m_f \) doesn’t depend on fluid velocity. This parameter is then identified through the measurement of the frequency of the first mode in stagnant water and by comparing it to the equivalent measurement in air \( m_f \). Concerning fluid added stiffness \( k_f \) and damping \( c_f \), we infer these coefficients by measuring for each fluid velocity first mode frequency and damping coefficient (see Eq.(6) & Eq.(7)).

\[
\begin{align*}
\omega &= \frac{k_1 + k_f}{m_1 + m_f} \\
\zeta &= \frac{c_1 + c_f}{2 \omega (m_1 + m_f)}
\end{align*}
\]

(8)

(9)

In the Fig.5 & Fig.6 we recall the results of measurements given by [4] for each value of fluid velocity.

Figure 5. Identified first modal frequency depending on fluid velocity (m/s)
As we can notice, the damping become negative from 2.1 m/s and the fluid elastic instability phenomenon appears. Nevertheless in non-linear case (with impacts), the structure remains stable because the gap stop limit the vibration amplitude of tube. In order to model this phenomenon, we have to introduce another dimensionless concepts, reduced velocity, coupling damping coefficient $C_d$ and coupling stiffness coefficient $C_k$. These dimensionless coefficients will help to explain the stabilizing effect of the impacts.

In his works, S.Caillaud [10] introduced the dimensionless coupling coefficient as follow:

$$C_d = 8\pi (m_1 + m_f) \frac{\zeta_o \cdot \frac{\omega_o}{\omega_f} - \zeta}{\rho_f \cdot D^2 L_e V_r}$$ (10)

$$C_k = 8\pi^2 (m_1 + m_f) \frac{\omega_o}{\omega_f} - 1 \frac{V_r}{D}$$ (11)

$$V_r = \frac{V}{D} f_{app}$$ (12)

$$L_e = \int_0^L \phi_1(x)^2 \, dx$$ (13)

Where $L_e$ is the modal equivalent length calculated from the first mode shape, $\zeta_o$ and $\omega_o$ are the modal damping coefficient and circular frequency in stagnant water.

When including impacts in the problem, the expression of the reduced fluid velocity in Eq.(1) becomes a little more complicated, since it depends on vibration apparent frequency of tube and not anymore on the first modal frequency (7).

There are different way to estimate this vibration tube frequency, we can quote for example zero-crossing method [11] & [12] and Rice frequency method $f_R$ [13]. This last method was chosen for our problem.

$f_R$ is proportional to velocity RMS over displacement RMS of the tube free end within sliding size windows $\tau$.

$$f_R(t, \tau) = \frac{\sigma_y(t, \tau)}{2\pi \sigma_y(t, \tau)}$$ (14)

The dimensionless coupling coefficients $C_d$ and $C_k$ can be inferred from $\zeta$ and $\omega$ already measured. In addition, as shown in Eq.(10) & Eq.(11), they depend on reduced velocity. Figure 7 presents the variation of dimensionless coupling coefficient depending on reduced velocity. It can clearly be seen that $C_d$ become completely negative from about 3.8.

**NUMERICAL SOLVER**

After determining experimentally all parameters, the next step is to create a numerical solver including all concepts we introduced to solve the nonlinear problem. The Newmark time integration solver has been implemented to get the tube response. Numerous studies have been conducted in linear as well as in nonlinear problems[14].
In our approach, a mechanical conservation energy criterion has been used in order to verify trustworthiness of the numerical results. $Em$ is constituted by sum of three terms: kinetic energy, potential energy and shocks potential energy. At each computation step, theses energy are evaluated as follows and the sum is divided by the initial mechanical energy in order to get the conservation in percentage.

$$Ec(n) = \frac{1}{2} (y(n))^T \cdot M \cdot (y(n))$$  \hfill (15)

$$Ep(n) = \frac{1}{2} (y(n))^T \cdot K \cdot (y(n))$$  \hfill (16)

$$Epc(n) = \frac{1}{2} (Kc)^T \cdot (Fc(n))^T \cdot (Fc(n))$$  \hfill (17)

First we applied this criterion on Newmark method alone without any correction algorithm taking in consideration the impact time. To avoid this behavior, a Newton-Raphson algorithm [15] slightly modified has been implemented in order to fit our tolerance requirement concerning the impact time. Figure 10 presents the energy conservation criterion after implementing Newton-Raphson algorithm for a computation step of $2.10^3$ s, we reached around 100% of energy conservation with less than 1% of error Fig. 11.

**IMPACTS STABILIZING EFFECT**

At this stage, the parameters describing the fluid elastic force are depending on reduced velocity. The later includes the effect of the impacts through apparent frequency $f_R$.

The impact stabilizing effect can be explained by the conjunction of two phenomena: The first one is the dissipation due to the higher orders modes of the structure. In fact, when impact occurs, many modes not excited by the turbulent flow are excited, and will then dissipate a part of energy increasing the stability of the tube. The second phenomenon is the increase of the stiffness of the structure by being in contact with a stiff obstacle. During contact, since the apparent stiffness is increased, apparent frequency of the structure should also increase, hence decreasing the reduced velocity (Eq.(12)), which makes the fluid elastic load dissipating. The numerical results in Fig. 9 illustrate well this phenomenon.
NUMERICAL VS EXPERIMENTAL RESULTS

In this part we compare our first numerical results to the experimental one [9] for gap equal to 0.5mm and flow velocity of 2.1m/s in order to validate our numerical approach. On the left side, a detailed plot of the free end displacement for numerical simulation and experimental measurement are shown. On the right, there associated histograms are presented.

The direct comparison of the detailed plots is not appropriate and results should be compared in a statistical sense, since turbulence forces are modeled by random excitation with a bandwidth of 40Hz. But through this plot we can highlight the displacement which is bounded at about double distance of the gap. This can be apprehended from the first mode shape. Concerning the histogram, the distribution is centered on zero, namely the initial equilibrium position. Also notice the good agreement of the estimated time between the two results.

ACTIVE CONTROL

In order to design the active part of the bench which simulates the fluid-elastic force effect, the characterization of each control loop component (shaker, accelerometer etc) must be performed. This stage is crucial because it allows complete mastering of the system. In this paper we do not give details about this modeling stage but we can refer to Dorf and Bishop works [16] for more details.

After this phase of modeling, our efforts were conducted on plant designing [17]. The aim is to impose a root for first pole (first mode) in such a way that the whole system fit as much as possible the evolution of both first modal frequency and modal damping coefficient previously measured for different value of the control gain G. In this way, by controlling the gain the corresponding reduced velocity configuration can be reproduced.

Figure 14 gives an example of a root locus of the system for a plant that we are still working on. As it can be noticed, the system becomes instable around the modal frequency of the tube in stagnant water for G = 0.25 and fluid elastic instability occurs. We are currently working on the experimental setup to validate these results before adding gap stops and studying the stabilizing effect of the impact.

CONCLUSION

A numerical model of the vibrations of a SG tube subjected to fluid-elastic and impact forces were obtained. This model was updated with experimental modal analysis results. The Newmark time integration method combined with Newton-Raphson algorithm provided an estimation of the response of the tube subjected to fluid excitation forces and impacts. The next step of our study is devoted to implementation of this controller experimentally to reproduce the fluid effect on the real structure and validate the numerical approach.

REFERENCES


